

A New Restructuring Algorithm for the Classification-Tree Method *

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Abstract

The classification-tree method developed by Grochtmann and Grimm facilitates the identification of test cases from functional specifications via the construction of classification trees. Their method has been enhanced by Chen and Poon through the classification-tree construction and restructuring methodologies. We find, however, that the restructuring algorithm by Chen and Poon is applicable only to certain types of classification trees. We introduce a new tree-restructuring algorithm to supplement their work.

Keywords *Black Box Testing, Classification-Tree Method, Specification-Based Testing, Test Case Selection*

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1. Introduction

Motivated by the importance of test cases on the comprehensiveness and hence the quality of software testing [1, 2, 8, 9, 12, 14], numerous researchers have developed their own methods for constructing test cases from functional specifications (referred to as “specifications” in this paper). One of them is the classification-tree method [10, 11], which helps software testers construct test cases from specifications via the construction of classification trees. Although this method can be classified as a black-box testing approach, it differs from other black-box approaches in the following aspects:

- (a) Most black-box testing techniques construct test cases from the functions of a program, whereas the classification-tree method achieves this from the input domain of a program. In other words, the former are basically function-oriented, whereas the latter is data-oriented [7].

- (b) Most black-box testing techniques are only effective when the specification is written in a formal way, such as in the formal specification language Z. On the other hand, the classification-tree method can be applied to both formal and informal specifications.

Since the tree construction approach proposed in [10, 11] is rather *ad hoc*, the classification trees constructed from the same specification may vary according to the personal experience of software testers. This inspired Chen and Poon [4, 6] to develop a methodology for constructing a classification tree from a given set of classifications and associated classes via the notion of a classification-hierarchy table. This table captures the hierarchical relation for each pair of distinct classifications. An example of a hierarchical relation is that, when a classification X takes a particular class, classification Y can take none of its classes. Furthermore, Chen and Poon observed that

- (i) the quality of classification trees depends on the effectiveness of constructing legitimate test cases, and
- (ii) a major reason for a poor quality in classification trees is the occurrence of duplicated subtrees under different top-level classifications.

For (ii), the duplicated subtrees cause the classification tree to generate numerous illegitimate test cases. As a result, the effectiveness with respect to legitimate test cases is reduced. From these observations, they defined an effectiveness metric to measure the quality of classification trees, and developed a tree-restructuring algorithm *remove_duplicate* for removing duplicated subtrees from classification trees, thereby improving on the value of the metric [5].

After a close examination, however, we find that *remove_duplicate* can only be applied to certain types of classification trees. There are cases where *remove_duplicate* cannot be applied. Specifically, our examination of *remove_duplicate* reveals that:

- (a) The algorithm cannot handle subtrees that are duplicated within the same top-level classification.
- (b) For classification trees with more than one set of duplicated subtrees under different top-level classifications, *remove_duplicate* can only be used to remove *one* of these sets at any one time. Furthermore, this algorithm cannot be applied repeatedly.

This paper addresses the above two issues. The rest of the paper is structured as follows. Section 2 reviews the previous work on the classification-tree method. Section 3 describes in detail our new restructuring algorithm. Finally, Section 4 concludes the paper.

2. Previous work on the classification-tree method

2.1. Grochtmann and Grimm

The classification-tree method [10, 11] was developed by Grochtmann and Grimm as an extension to the category-partition method [1, 3, 13, 14]. It helps testers construct test cases from specifications via the concept of classification trees.

Classifications are defined as the criteria for partitioning the input domain of the program, whereas *classes* are defined as the disjointed subsets of values for each classification. Basically, a classification tree organizes the classifications and classes into a tree structure. The following describes the major steps of the classification-tree method:

- (1) Identify all the classifications and the associated classes from the specification.
- (2) Construct a classification tree from the classifications and classes.
- (3) Construct a test case table from the classification tree.
- (4) Identify all possible combinations of classes from the test case table. Each combination of classes represents a potential test case.

We shall use Example 1 to illustrate the concept.

Example 1

The software under test is the program *bonus* being developed for Number-One Airline. It calculates the bonus points earned by passengers from their trips. Passengers can then claim various benefits such as free accommodation in leading hotels using the bonus points awarded.

The program calculates the bonus points according to the following specification:

(1) Classes of Seats

There are three classes of seats, namely first, business, and economy.

(2) Upgrading of Classes

Passengers holding an economy-class ticket are eligible for upgrading their tickets to a business class free-of-charge, provided that:

- (a) there are vacancies in the business class,
- (b) the passengers are holding a frequent-flyer card, and
- (c) the total mileage for the trip is less than 1000.

Under no circumstances can an economy-class or business-class ticket be upgraded to the first class.

(3) Discounts

Discounts are only available to:

- (a) economy-class tickets, and
- (b) the total mileage for the trip is not less than 1000.

There are two types of discounts, namely staff discount and passenger discount.

For (2)(c) and (3)(b), any distance less than one mile will not be counted. The number of bonus points earned will be calculated from the combination above. [The detailed calculations will be beyond the scope of this paper.]

Suppose the classifications and classes for *bonus* are identified as in Table 1. As seen from the table, a class may correspond to a single value such as “First”, or a range of values such as “ ≥ 1000 ”. Because of the latter, even though the union of all classes for any classification should cover the whole input domain, the number of classes for a single classification is not necessarily large.

After identifying all the classifications and classes, an obvious approach is to select a class from each classification so that each combination of selected classes forms a test case. For Table 1, for instance, a total of $3 \times 2^4 = 48$ test cases will be produced. However, some of these test cases are invalid because of the coexistence of incompatible classes. For example, according to clause (2) of the specification for *bonus*, the class “First” in the classification “Class of Seat” cannot coexist with the class “Yes” in the classification “Upgraded Class”.

In order to reduce the number of invalid test cases, a classification tree is constructed. For instance, a classification tree for *bonus*, denoted by T_{bonus} , is depicted in Figure 1.

The small circle at the top of the classification tree is the *general root node*, representing the whole input domain. The classifications directly under the general root node, such as “Class of Seat” and “Total Mileage” in Figure 1, are called the *top-level classifications*.

In general, a classification X may have a number of classes x_i directly under it. X is known as the *parent classification* and each x_i is known as a *child class*. In Figure 1, for example, “Price of Ticket” is the parent classification of “Normal” and “Discounted”, whereas “Normal” and “Discounted” are the child classes of “Price of Ticket”.

Similarly, a class x may have a number of classifications Y_j directly under it. Then x is known as a *parent class* and each Y_j is known as a *child classification*. In Figure 1, for

Classifications	Associated Classes
Class of Seat	First, Business, Economy
Upgraded Class	Yes, No
Price of Ticket	Normal, Discounted
Type of Discount	Staff, Passenger
Total Mileage	$< 1000, \geq 1000$

Table 1. Possible classifications and classes for *bonus*

example, “Discounted” is the parent class of “Type of Discount”, whereas “Type of Discount” is the child classification of “Discounted”.

Test cases can be expressed in a test case table under the classification tree. The columns of the test case table correspond to the terminal nodes of the classification tree and therefore represent classes. Each row corresponds to a combination of classes and represents a potential test case. The test case table is constructed by the following steps:

- (1) Draw the columns of the test case table by drawing a vertical line downward from each terminal node of the classification tree.
- (2) Construct a potential test case in the test case table by selecting a combination of classes in the classification tree as follows:
 - (a) Select one and only one child class from each top-level classification.
 - (b) For every child classification of each selected class, recursively select one and only one child class.

For example, row 3 of the test case table in Figure 1 represents the potential test case such that:

- the “Class of Seat” is “Economy”,
- the “Price of Ticket” is “Discounted”,
- the “Type of Discount” is “Staff”, and
- the “Total Mileage” is “ ≥ 1000 ”.

We use P_i to denote a path in T_{bonus} . For example, P_2 denotes the path “Class of Seat” – “Business” – “Upgraded Class” – “Yes”. Thus, the potential test case corresponding to row 3 is formed by selecting P_5 and P_{10} . Only part of the test case table is shown in Figure 1. The complete

table produces a total of 30 potential test cases. Compared to the 48 test cases that would have been constructed by simply selecting and combining one class from each classification in Table 1, we find that 18 invalid test cases have been effectively filtered out. This elimination of invalid test cases has been achieved by capturing the hierarchical constraints among various classifications in T_{bonus} . ■

The classification-tree method has been used for testing various real-life systems, such as a control system for the airfield lighting of an international airport, an identification system for automatic mail sorting machines, and an integrated ship management system. The results of these applications are very encouraging [10, 11].

2.2. Chen and Poon

2.2.1. Systematic construction of classification trees

Obviously, once the classification tree has been constructed, the formation of potential test cases is straightforward. Chen and Poon have noted, however, that the construction of classification trees as described in [10, 11] is only *ad hoc*. It will be difficult, therefore, to apply the method when the specification is complex and involves a large number of classifications and classes.

This problem motivated Chen and Poon to develop a systematic tree construction method via the notion of a classification-hierarchy table [4, 6]. Basically, the table captures the hierarchical relation for every pair of distinct classifications. In the table for *bonus*, for example, we note that the classification “Type of Discount” cannot take any of its classes when the classification “Class of Seat” takes the class “First”. Once the classification-hierarchy table has been constructed, the corresponding classification tree can be formed using an associated tree construction algorithm. Readers may refer to [4, 6] for details.

2.2.2. Restructuring of classification trees

Occasionally, a classification tree may not be able to reflect all the constraints among classifications. Hence, all the potential test cases constructed from the classification tree should be verified with the specification. In this way, we can identify and remove the potential test cases that contradict the specification. Such potential test cases are known as *illegitimate test cases*. Others are known as *legitimate test cases*. For example, row 2 of the test case table in Figure 1 will produce an illegitimate test case because, according to clause (2)(c) of the specification for *bonus*, the class “Yes” in the classification “Upgraded Class” cannot coexist with the class “ ≥ 1000 ” in the classification “Total Mileage”. In fact, 25 out of the 30 potential test cases constructed from T_{bonus} are illegitimate. Only five potential test

cases are legitimate and therefore useful for testing.

In [5], Chen and Poon proposed that the ultimate purpose of the classification-tree method is to construct legitimate test cases, and the classification tree is merely a means for this construction. Given a classification tree T , let N_T^p and N_T^l be the number of potential test cases and legitimate test cases, respectively. Chen and Poon defined an *effectiveness metric* E_T for T as follows:

$$E_T = \frac{N_T^l}{N_T^p}$$

For example, since $N_{T_{bonus}}^p = 30$ and $N_{T_{bonus}}^l = 5$, $E_{T_{bonus}}$ is found to be $\frac{5}{30} = 0.17$. Obviously, N_T^l can only be known after removing all the illegitimate test cases from the set of potential test cases. On the other hand, even before the identification of potential test cases, N_T^p can be derived directly from T using the formulae presented in [5].

Obviously, a small value of E_T is undesirable, as effort will be wasted on illegitimate test cases. In [5], Chen and Poon observed that a major cause of a poor E_T is the existence of duplicated subtrees under different top-level classifications in a classification tree.

Let $S[X]$ denote a subtree with a classification X as its root, and $S[x]$ denote a subtree with a class x as its root. If X is a top-level classification, we will call $S[X]$ a *top-level subtree*.

In T_{bonus} of Figure 1, since “Price of Ticket” is related to both the top-level classifications “Class of Seat” and “Total Mileage”, the subtree $S[\text{Price of Ticket}]$ is duplicated in both the top-level subtrees $S[\text{Class of Seat}]$ and $S[\text{Total Mileage}]$. As a result, it is possible to construct an illegitimate test case containing the incompatible classes

(“< 1000” and “Normal”)
or (“< 1000” and “Discounted”)

by selecting

(P_7 or P_8) and (P_4 or P_5 or P_6).

Similarly, since “Upgraded Class” is related to both the top-level classifications “Class of Seat” and “Total Mileage”, the subtree $S[\text{Upgraded Class}]$ is also duplicated in both the top-level subtrees. These two duplications result in 25 illegitimate test cases, thereby reducing $E_{T_{bonus}}$ to a very small value.

From this observation, Chen and Poon developed a tree-restructuring algorithm *remove_duplicate* to improve on the value of E_T for classification trees with duplicated subtrees under different top-level classifications [5]. This improvement is achieved by removing the duplicated subtrees from the classification tree, thereby reducing the number of illegitimate test cases while preserving all the legitimate ones.

For example, $E_{T_{bonus}}$ can be increased from 0.17 to 0.40 after the application of *remove_duplicate*.

The restructuring algorithm *remove_duplicate* may, however, convert some legitimate test cases into illegitimate ones through the introduction of incompatible classes. Hence, all the potential test cases constructed from the *restructured* classification tree must be reformatted using the algorithm described in [5]. The reformatting algorithm will ensure that any newly introduced illegitimate test cases are converted back into legitimate ones.

3. A new restructuring algorithm

Despite the ability to improve on the value of E_T , we observe that *remove_duplicate* has two limitations:

- (a) The algorithm only deals with the removal of duplicated subtrees under different top-level classifications. Consider, for example, the classification tree in Figure 2. The subtree $S[C]$ with classification C as its root appears twice under the top-level classification B . The algorithm cannot remove such duplications.
- (b) The algorithm can remove only *one* set of duplicated subtrees from the classification tree at any one time, even if the classification tree contains more than one set of duplications. Furthermore, the follow-up reformatting algorithm will only work if *remove_duplicate* is run only once. Suppose that, in Figure 1,
 - τ_1 and τ_2 denote the top-level subtrees $S[\text{Class of Seat}]$ and $S[\text{Total Mileage}]$, respectively,
 - $S_{\tau_1}[\text{Upgraded Class}]$ and $S_{\tau_2}[\text{Upgraded Class}]$ denote the subtrees $S[\text{Upgraded Class}]$ within τ_1 and τ_2 , respectively, and
 - $S_{\tau_1}[\text{Price of Ticket}]$ and $S_{\tau_2}[\text{Price of Ticket}]$ denote the subtrees $S[\text{Price of Ticket}]$ within τ_1 and τ_2 , respectively.

In this case, the algorithm can be used to restructure T_{bonus} by removing only one (but not both) of the following sets of duplicated subtrees:

- $\{S_{\tau_1}[\text{Upgraded Class}], S_{\tau_2}[\text{Upgraded Class}]\}$
- $\{S_{\tau_1}[\text{Price of Ticket}], S_{\tau_2}[\text{Price of Ticket}]\}$

The improvement in $E_{T_{bonus}}$ would of course be larger if both of the above sets could be removed.

The above limitations motivated us to develop a new restructuring algorithm for improving on the value of E_T . The new algorithm, known as *remove_identical*, is described as follows:

Tree Restructuring Algorithm *remove_identical* for a Classification Tree with Duplicated Subtrees:

Suppose

- (a) the classification tree has w top-level subtrees denoted by τ_i , $i = 1, 2, \dots, w$, where $w \geq 2$,
- (b) $N(\tau_i)$ denotes the total number of combinations of classes for τ_i ,
- (c) $S_{\tau_i}[X]$ denotes a subtree of τ_i such that the root of $S_{\tau_i}[X]$ is the classification X ,
- (d) τ'_i denotes the top-level subtree formed from τ_i after pruning from it all the subtrees $S_{\tau_i}[X]$, and
- (e) $N(\tau'_i)$ denotes the total number of combinations of classes for τ'_i .

Suppose there are two or more top-level subtrees containing duplicated subtrees. Without loss of generality, let these top-level subtrees be $\tau_1, \tau_2, \dots, \tau_n$, where $n \geq 2$, and let the duplicated subtrees be $S_{\tau_1}[X], S_{\tau_2}[X], \dots, S_{\tau_n}[X]$.^a

Select a top-level subtree τ_k (where $1 \leq k \leq n$) such that, if we prune all the $S_{\tau_1}[X], S_{\tau_2}[X], \dots, S_{\tau_{k-1}}[X], S_{\tau_{k+1}}[X], \dots, S_{\tau_n}[X]$ from $\tau_1, \tau_2, \dots, \tau_{k-1}, \tau_{k+1}, \dots, \tau_n$, respectively, it yields the *smallest* value of

$$Q = \left(\prod_{j=1}^{k-1} N(\tau'_j) \right) \times N(\tau_k) \times \left(\prod_{j=k+1}^n N(\tau'_j) \right)$$

Replace the top-level subtrees $\tau_1, \tau_2, \dots, \tau_{k-1}, \tau_{k+1}, \dots, \tau_n$ by $\tau'_1, \tau'_2, \dots, \tau'_{k-1}, \tau'_{k+1}, \dots, \tau'_n$, respectively, but leave the selected top-level subtree τ_k unchanged. In case there are two or more distinct τ_k that produce the same smallest value of Q , then arbitrarily select any of them.

Repeat the above process until there are no duplicated subtrees $S_{\tau_j}[X]$ and $S_{\tau_k}[X]$ across any pair of distinct top-level subtrees τ_j and τ_k . Note, however, that $S_{\tau_k}[X]$ is allowed to occur more than once *within* a top-level subtree τ_k .

^aWe note the number of duplicated subtrees may be more than the number of top-level subtrees with duplications. This is because the same subtree may occur more than once within a top-level subtree. The original algorithm *remove_duplicate* by Chen and Poon did not cater for this type of duplication and cannot, therefore, be used for restructuring such classification trees.

In the above algorithm, $N(\tau'_j)$ and $N(\tau_k)$ can be derived using the formulae from [5]. Suppose T' denotes the classi-

fication tree after restructuring. According to the formulae for the computation of $N_{T'}^p$ in [5], the smaller the value of Q , the smaller will be the value of $N_{T'}^p$. Thus, by minimizing the value of Q , we can improve on the value of $E_{T'}$.

There are two important properties of *remove_identical*, as reflected in the two propositions that follow.

Proposition 1 (Convergence Property)

Suppose a classification tree T has been restructured using the algorithm *remove_identical* to form T' . The number of potential test cases constructed from T' will be no more than that from T .

Proof

As seen from the restructuring algorithm *remove_identical*, T' is equivalent to T with some duplicated subtrees pruned. Obviously, the proposition follows immediately. ■

Before we proceed to prove the second property of the restructuring algorithm *remove_identical*, we have to introduce a few concepts. We define a *feasible net* F in a classification tree as a collection of paths such that all the classes in these paths are selected *together* to form a whole potential test case. Thus, the number of distinct feasible nets in the classification tree is always equal to the number of potential test cases. For example, in the test case table of Figure 1, the potential test case corresponding to row 1 is formed by selecting the feasible net that contains the paths P_1 and P_8 . In most cases, a feasible net will contain more than one path because:

- (a) a typical classification tree contains more than one top-level subtree, and
- (b) at least one path within each top-level subtree must be selected to form a potential test case.

Let τ_i denote a top-level subtree in a classification tree. Given any feasible net F in the classification tree, a *feasible subnet* $F|_{\tau_i}$ is defined as the set of all paths P in F such that P is within τ_i . For example, suppose τ_1 denotes the top-level subtree in Figure 2 with classification A as its root. Then, $\{P_1, P_3\}$ is a feasible subnet within τ_1 . It is obvious that:

- (i) If every class in a classification tree has only one child classification, as in Figure 1, then all the feasible subnets in the tree will contain only one path.
- (ii) If some class in a classification tree has two or more child classifications, as in Figure 2, then some of the feasible subnets in the tree will contain more than one path.

Now, suppose a classification tree has two or more top-level classifications denoted by $\tau_1, \tau_2, \dots, \tau_w$. Suppose further that:

- (a) τ_i and τ_j (where $1 \leq i, j \leq w$) denote two distinct top-level subtrees containing duplicated subtrees $S_{\tau_i}[X]$ and $S_{\tau_j}[X]$, respectively, and
- (b) τ_k (where $k \neq i, k \neq j$, and $1 \leq k \leq w$) denotes a top-level subtree that does not contain a duplicated subtree $S_{\tau_k}[X]$.

The feasible subnets within τ_i can be classified as follows:

- (i) A feasible subnet $F|_{\tau_i}$ is in $F(\tau_i, X)$ if some path in the subnet contains the classification X .
- (ii) A feasible subnet $F|_{\tau_i}$ is in $F(\tau_i, \neg X)$ if no path in the subnet contains the classification X .

Let us illustrate this concept with the classification tree in Figure 2. Again, let τ_1 denote the top-level subtree $S[A]$. Then, $\{P_1, P_3\}$ is a feasible subnet in $F(\tau_1, C)$, and $\{P_5\}$ is a feasible subnet in $F(\tau_1, \neg C)$.

Having introduced the above concepts, we are now ready to prove the second property of the new restructuring algorithm *remove_identical*.

Proposition 2 (Preservation Property)

Suppose a classification tree T has been restructured using *remove_identical* to form T' . Any legitimate test case that can be constructed from T can also be constructed from T' .

Proof

We shall follow the notation used in the restructuring algorithm *remove_identical*. Without loss of generality, suppose that

- (a) the classification tree T has w top-level subtrees denoted by $\tau_i, i = 1, 2, \dots, w$, where $w \geq 2$,
- (b) $\tau_1, \tau_2, \dots, \tau_n$ (where $n \leq w$) contain duplicated subtrees of the form $S_{\tau_1}[X], S_{\tau_2}[X], \dots, S_{\tau_n}[X]$, respectively,
- (c) for any $1 \leq i \leq n$, τ'_i denotes the top-level subtree formed by pruning all the subtrees of the form $S_{\tau_i}[X]$ from τ_i , and
- (d) after the application of *remove_identical*, all the duplicated subtrees in (b) are removed, except for the subtree(s) $S_{\tau_k}[X]$ in one and only one top-level subtree τ_k for some $1 \leq k \leq n$.

Obviously, every feasible net F and the corresponding potential test case are formed by selecting one feasible subnet from every $\tau_i, i = 1, 2, \dots, w$. Any legitimate test case constructed from T can be classified into two types:

- (i) The legitimate test case is formed by selecting one feasible subnet from every $F(\tau_i, X)$, $i = 1, 2, \dots, n$, and one feasible subnet from every τ_i , $i = n + 1, n + 2, \dots, w$.

Obviously, all the feasible subnets in $\tau_{n+1}, \tau_{n+2}, \dots, \tau_w$ will remain intact after restructuring because $\tau'_{n+1} = \tau_{n+1}$, $\tau'_{n+2} = \tau_{n+2}, \dots, \tau'_w = \tau_w$.

Consider any feasible subnet $F|_{\tau_i}$ selected from $F(\tau_i, X)$. Some path in $F|_{\tau_i}$ must contain some class within the duplicated subtree $S_{\tau_i}[X]$. Consider any such class y . It will obviously be deleted after pruning all the subtrees $S_{\tau_i}[X]$ from the classification tree T . Since $\tau'_k = \tau_k$, however, y must still appear in some path of some feasible subnet in $F(\tau'_k, X)$. Thus, all the legitimate test cases of this type can still be formed from T' .

- (ii) The legitimate test case is formed by selecting one feasible subnet from every $F(\tau_i, \neg X)$, $i = 1, 2, \dots, n$, and one feasible subnet from every τ_i , $i = n + 1, n + 2, \dots, w$.

Such a test case will remain unchanged after restructuring because:

- every $F(\tau_i, \neg X)$ will be left intact, and
- $\tau'_{n+1} = \tau_{n+1}$, $\tau'_{n+2} = \tau_{n+2}, \dots, \tau'_w = \tau_w$.

We shall prove by contradiction that no third type of legitimate test case exists.

Suppose a legitimate test case is formed by selecting feasible subnets from a mixture of $F(\tau_i, X)$ and $F(\tau_j, \neg X)$ for $i, j = 1, 2, \dots, n$ (where $i \neq j$), and one feasible subnet from every τ_i , $i = n + 1, n + 2, \dots, w$. Consider any feasible subnet $F|_{\tau_j}$ selected from $F(\tau_j, \neg X)$. By definition, any path in $F|_{\tau_j}$ cannot contain the classification X , and hence cannot contain any of its child classes. In other words, this path must contain some child class y (in a classification Y) that cannot coexist with any child class in X . For any feasible subnet from $F(\tau_i, X)$, it must contain a child class x in X . This will contradict the fact that the test case is legitimate.

Thus, any legitimate test case that can be constructed from T can also be constructed from T' . ■

Let us use Example 2 to illustrate the application of the restructuring algorithm *remove_identical* and to show the improvement in E_T .

Example 2

Consider the classification tree T_{bonus} in Figure 1. Let τ_1 and τ_2 denote the top-level subtrees $S[\text{Class of Seat}]$ and $S[\text{Total Mileage}]$, respectively.

Consider the duplicated subtrees $S_{\tau_1}[\text{Price of Ticket}]$ and $S_{\tau_2}[\text{Price of Ticket}]$. There are two alternative ways of restructuring T_{bonus} using the algorithm *remove_identical*:

- (a) Prune $S_{\tau_1}[\text{Price of Ticket}]$ from τ_1 , or
- (b) Prune $S_{\tau_2}[\text{Price of Ticket}]$ from τ_2 .

Figures 3 and 4 depict the two classification trees after the above ways of restructuring, respectively. Let τ'_1 be the result of pruning $S_{\tau_1}[\text{Price of Ticket}]$ from τ_1 , and τ'_2 that of pruning $S_{\tau_2}[\text{Price of Ticket}]$ from τ_2 . Using the formulae presented in [5], $N(\tau'_1) \times N(\tau_2) = 20$ for Figure 3, and $N(\tau_1) \times N(\tau'_2) = 18$ for Figure 4. Hence, the restructured classification tree in Figure 4 should be chosen.

A close examination of the restructured classification tree in Figure 4 reveals that it still contains the duplicated subtrees $S_{\tau_1}[\text{Upgraded Class}]$ and $S_{\tau'_2}[\text{Upgraded Class}]$. The restructuring algorithm *remove_identical* should therefore be applied again to prevent duplication. The resultant classification tree T'_{bonus} after the second application is depicted in Figure 5.

From the preservation property of the restructuring algorithm *remove_identical*, we can guarantee that the five legitimate test cases constructed from T_{bonus} before restructuring can still be constructed from T'_{bonus} . Hence, $N_{T_{bonus}}^l = N_{T'_{bonus}}^l = 5$. On the other hand, $N_{T_{bonus}}^p$ is found to be 12 using the formulae in [5]. Thus, $E_{T'_{bonus}} = \frac{5}{12} = 0.42$. When compared with $E_{T_{bonus}} = 0.17$, the improvement is about 147% and therefore quite significant. ■

4. Conclusion

Chen and Poon [4, 6] provided a methodology for constructing a classification tree from a given set of classifications and associated classes via the notion of a classification-hierarchy table. They observed that (a) the quality of classification trees depends on the effectiveness of constructing legitimate test cases, and (b) a major reason for a poor quality is the occurrence of duplicated subtrees under different top-level classifications. From these observations, they defined an effectiveness metric for classification trees and developed a tree-restructuring algorithm *remove_duplicate* to improve on the value of the metric.

We have proposed in this paper a new restructuring algorithm *remove_identical* to supplement *remove_duplicate*. We have proved that our new algorithm not only preserves the legitimate test cases but is also converging.

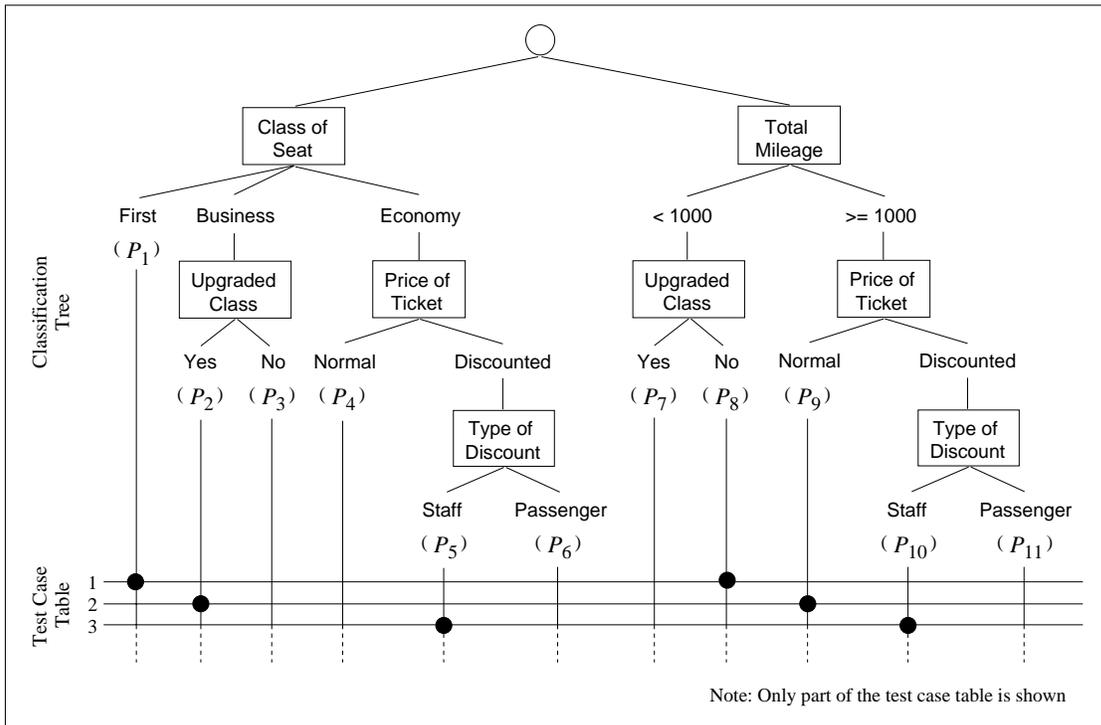


Figure 1. Classification tree for bonus point program and part of the test case table

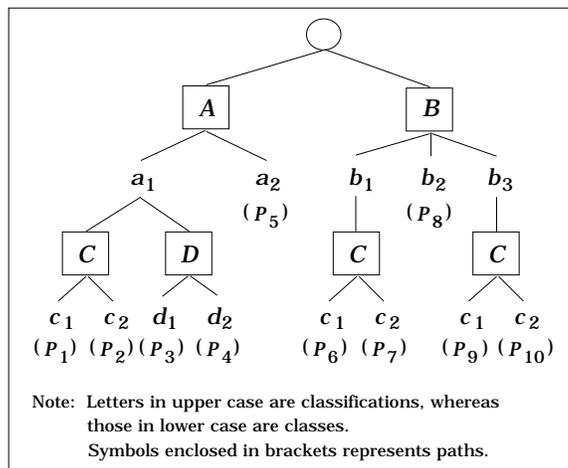


Figure 2. Duplicated subtrees under the same top-level classification

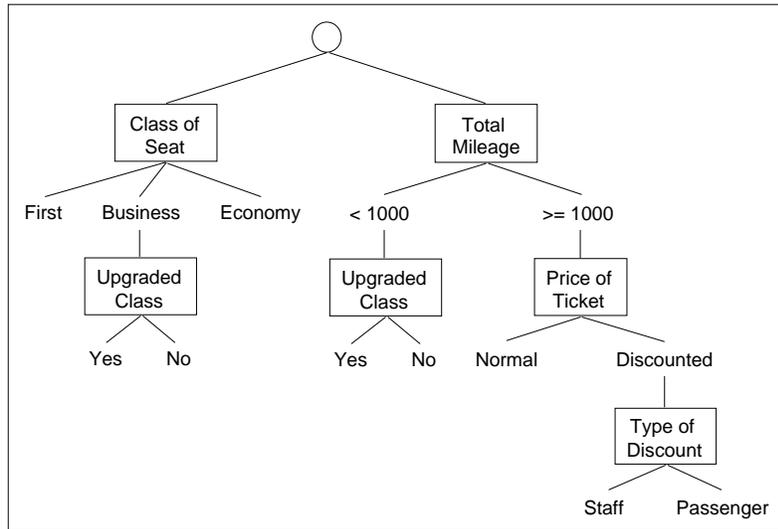


Figure 3. The resultant classification tree after pruning S_{t_1} [Price of Ticket]

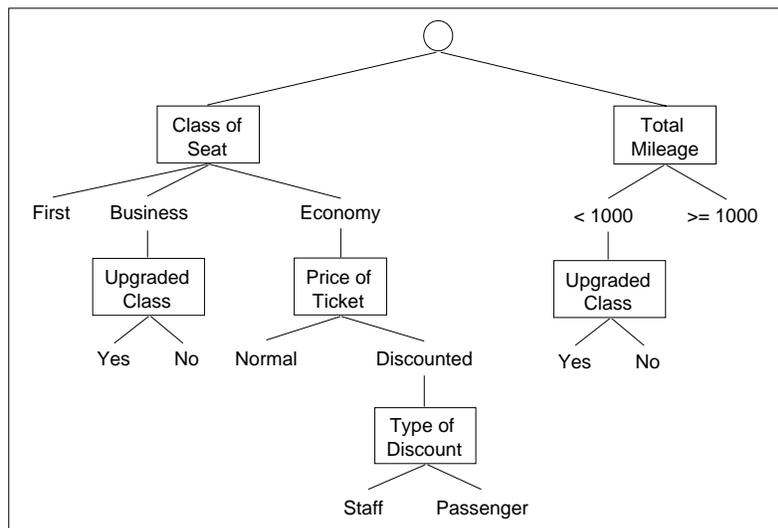


Figure 4. The resultant classification tree after pruning S_{t_2} [Price of Ticket]

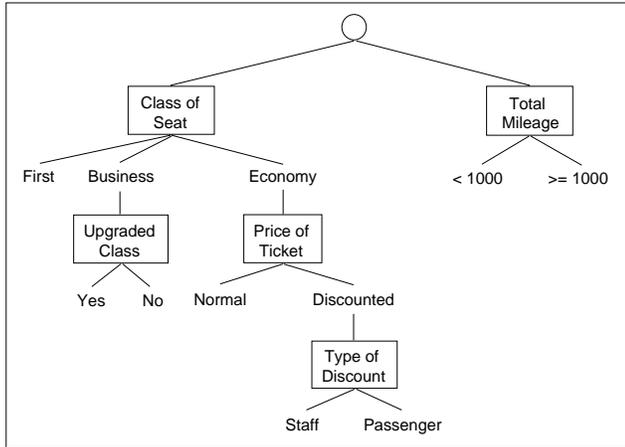


Figure 5. The final classification tree T'_{bonus} after restructuring

References

- [1] P. Ammann and J. Offutt. Using formal methods to derive test frames in category-partition testing. In *Safety, Reliability, Fault Tolerance, Concurrency, and Real Time Security: Proceedings of 9th Annual IEEE Conference on Computer Assurance (COMPASS '94)*, pages 69–79, June 1994. IEEE Computer Society Press, Los Alamitos, California.
- [2] R. Bache and M. Müllerburg. Measures of testability as a basis for quality assurance. *Software Engineering Journal*, 5(3):86–92, March 1990.
- [3] M.J. Balcer, W.M. Hasling, and T.J. Ostrand. Automatic generation of test scripts from formal test specifications. In *Proceedings of 3rd ACM Annual Symposium on Software Testing, Analysis, and Verification (TAV '89)*, pages 210–218, December 1989. ACM Press, New York.
- [4] T. Y. Chen and P.L. Poon. Classification-hierarchy table: A methodology for constructing the classification tree. In *Proceedings of 1996 Australian Software Engineering Conference (ASWEC '96)*, pages 93–104, July 1996. IEEE Computer Society Press, Los Alamitos, California.
- [5] T. Y. Chen and P.L. Poon. Improving the quality of classification trees via restructuring. In *Proceedings of 3rd Asia-Pacific Software Engineering Conference (APSEC '96)*, pages 83–92, December 1996. IEEE Computer Society Press, Los Alamitos, California.
- [6] T. Y. Chen and P.L. Poon. Construction of classification trees via the classification-hierarchy table. *Information and Software Technology*, 39(13):889–896, December 1997.
- [7] T. Y. Chen and P.L. Poon. Teaching black box testing. In *Proceedings of Software Engineering: Education and Practice Conference (SE:E&P '98)*, pages 324–329, January 1998. IEEE Computer Society Press, Los Alamitos, California.
- [8] T. Chusho. Test data selection and quality estimation based on the concept of essential branches for path testing. *IEEE Transactions on Software Engineering*, 13(5):509–517, May 1987.
- [9] R. Ferguson and B. Korel. The chaining approach for software test data generation. *ACM Transactions on Software Engineering and Methodology*, 5(1):63–86, January 1996.
- [10] M. Grochtmann and K. Grimm. Classification trees for partition testing. *Software Testing, Verification and Reliability*, 3(2):63–82, June 1993.
- [11] M. Grochtmann, J. Wegener, and K. Grimm. Test case design using classification trees and the classification-tree editor CTE. In *Proceedings of 8th International Software Quality Week (QW '95)*, 1995. Software Research Institute, San Francisco, California.
- [12] B. Korel. Automated test data generation for programs with procedures. In S.J. Zeil, editor, *Proceedings of 1996 ACM International Symposium on Software Testing and Analysis (ISSTA '96)*, pages 209–215, January 1996. ACM Press, New York.
- [13] A.J. Offutt and A. Irvine. Testing object-oriented software using the category-partition method. In R. K. Ege, M. Singh, and B. Meyer, editors, *Proceedings of 17th International Conference on Technology of Object-Oriented Languages and Systems (TOOLS 17)*, pages 293–304, August 1995. Prentice Hall, Englewood Cliffs, New Jersey.
- [14] T.J. Ostrand and M.J. Balcer. The category-partition method for specifying and generating functional tests. *Communications of the ACM*, 31(6):676–686, June 1988.