

1 **A Stochastic Collision-Attachment-Based Monte Carlo Simulation of Colloidal**
2 **Fouling: Transition from Foulant-Clean-Membrane Interaction to Foulant-**
3 **Fouled-Membrane Interaction**

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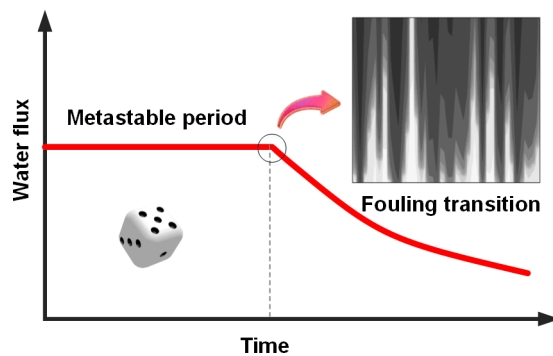
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23 **ABSTRACT**

24 The initial behavior of colloidal fouling is governed by foulant-clean-membrane
25 interaction (F-M), and its long-term behavior is determined by foulant-fouled-
26 membrane interaction (F-F). Nevertheless, the transitional fouling behavior from F-M
27 to F-F has not been fully understood. This study reports a novel collision attachment
28 (CA)-Monte Carlo (MC) approach, with the stochastic colloid-membrane collision
29 events modelled by MC and the probability of colloidal attachment to the membrane
30 determined by the interplay of flux and the energy barrier arising colloid-membrane
31 interaction (E_m for F-M and E_f for F-F). The long-term membrane flux remains stable
32 for large E_f , whereas severe fouling occurs when both E_m and E_f are small. Our study
33 reveals the existence of a metastable flux behavior for the combination of large E_m but
34 small E_f . The time evolution of flux behavior and colloidal deposition pattern shows a
35 nearly constant flux for an extended period, with the high energy barrier E_m retarding
36 initial colloidal deposition. However, accidental random deposition of a colloidal
37 particle could reduce the local energy barrier (towards the smaller E_f), seeding for
38 further colloidal deposition in its vicinity. This initiates an uneven patch-wise fouling
39 and eventually leading to a complete transition to F-F dominated behavior. The
40 metastable period can be effectively extended by increasing the energy barrier (E_m or
41 E_f) or lowering flux, which provides important implications to membrane design and
42 operation.

43

44 INTRODUCTION

45 Reverse osmosis (RO) and nanofiltration (NF) are widely used in desalination,^{1,2} water
46 reuse,^{3,4} and industrial wastewater treatment.^{5,6} However, their applications are often
47 restricted by membrane fouling. Colloidal particles, including organic macromolecules
48 such as humic acid (HA), proteins, and polysaccharides,⁷ are important foulants in RO
49 and NF processes.⁸ It has been generally agreed that colloidal fouling is governed by
50 the interplay of hydrodynamic forces and foulant-membrane interactions.⁸⁻¹⁰ As a
51 notable example, Field et al. and Bacchin et al.¹¹⁻¹⁴ studied the role of permeate flux
52 and formulated the concept of critical flux below which little fouling occurs. Solution
53 chemistry¹⁵⁻¹⁷ and membrane properties^{18,19} are equally important via their influence
54 on foulant-membrane interactions.²⁰⁻²² For example, membrane surfaces are often
55 designed to be more hydrophilic to impart better antifouling performance, thanks to the
56 suppressed foulant-membrane hydrophobic attraction.^{18,19}

57

58 An interesting phenomenon in fouling is the transition from foulant-clean-membrane
59 interaction (F-M) to foulant-fouled-membrane interaction (F-F). Although the initial
60 fouling of a clean membrane is governed by F-M, it transits into F-F upon the complete
61 coverage of the membrane surface by a foulant layer.^{8,23} Several experimental studies
62 performed under constant pressure conditions reveal that the water flux could remain
63 relatively stable for an extended period (hours to days) before the occurrence of a
64 substantial and continued flux decline.^{19,24-27} This metastable behavior appears to be

65 more salient for a membrane with smoother and more hydrophilic surface compared to
66 other membranes with poorer antifouling properties.²⁷ Considering a membrane with
67 an excellent antifouling surface, it would presumably maintain a relatively stable flux
68 behavior as a result of strong F-M repulsive interaction (i.e., greater energy barrier for
69 colloidal particle attachment).⁸ Nevertheless, any accidental deposition of foulant at a
70 particular location would condition the membrane surface locally, potentially shifting
71 the localized interaction into a less repulsive or even attractive F-F interaction.¹⁰ This
72 results in a reduction in the energy barrier to initiate the propagation of fouling, in a
73 way analogous to the role of nucleation to crystallization^{28, 29}.

74

75 Despite its fundamental importance and practical significance with respect to
76 membrane design, process operation, and fouling control, a theoretical framework on
77 such transitional fouling behavior is yet to be established. Due to the stochastic nature
78 of this transition, deterministic models based on traditional approaches (e.g., Navier-
79 Stokes equation³⁰ and force balance²²) may not work. In the current study, we report a
80 Monte Carlo (MC)-based approach to describe the random movements of colloidal
81 particles. Although MC has been successfully applied to simulate membrane pore
82 blocking,³¹⁻³³ cake formation/structure^{31, 34, 35} and phase transition,³⁶ it has been seldom
83 used to study the F-M to F-F transitional fouling behavior. To enable the simulation of
84 the random deposition of colloidal particles on a membrane surface, we further adopt
85 the collision-attachment (CA) model,³⁷ in which the frequency of particle collision

86 events is simulated by the MC approach and the probability for successful particle
87 attachment for any given collision event is assessed based on the classical Boltzmann
88 distribution theory³⁸. The coupled CA-MC approach is able to describe the fine details
89 of the transitional fouling behavior, underpinning the theoretical existence of
90 metastable flux and revealing its dependence on foulant-membrane interactions and
91 operational conditions. Our findings provide important guidelines and new directions
92 for fouling control.

93

94 **THEORY**

95 Membrane fouling can be idealized as a collision-attachment process: (1) colloidal
96 particles transport towards a membrane surface, leading to their collisions with the
97 surface, and (2) the attachment of the colloidal particles onto the surface.^{37, 39, 40} Based
98 on the classical CA theory, the rate of colloidal particle deposition is given by the
99 product of the frequency of colloidal particle collision events and the probability of
100 successful attachment for each collision event. The CA theory has been widely adopted
101 for modelling particle-particle attachment (e.g., in the field of coagulation ^{41, 42}). It has
102 been recently adapted for modelling membrane fouling, recognizing a membrane
103 surface as an infinitely large and stationary particle.³⁷ To model the stochastic process
104 of colloidal particle transport and attachment during membrane filtration under constant
105 pressure, a two-dimensional (2D) CA-MC simulation is used in this study. Specifically,
106 the CA-MC simulation involves the following key aspects: (1) colloidal particle

107 transport in the vicinity of the membrane surface (i.e., the MC simulation of the
108 transport and collision events); (2) colloidal particle attachment based on the interplay
109 between hydrodynamic conditions and foulant-membrane interaction (i.e., the CA
110 model); and (3) the response in permeate flux as a result of membrane fouling.

111

112 Since RO membranes are not designed to treat large particles (which are removed
113 during the pre-treatment steps), this study only considers colloidal particles whose sizes
114 are $\ll 100$ nm. In this case, the diffusion of the colloidal particles are mainly caused
115 by their Brownian motion,^{8, 43} while the effects of inertial lift and shear-induced
116 diffusion are negligible.^{9, 44, 45}

117

118 **MC simulation of colloidal particle transport.** A feed flow channel (with length L
119 and boundary layer thickness δ) is evenly divided into n segments along its length
120 (Supporting Information S1.1). Colloidal particle transport is governed by the
121 convection in the transverse direction (caused by the crossflow velocity u in the x
122 direction), the convection towards the membrane surface (caused by the localized
123 velocity v in the $-z$ direction), and their random diffusion (Supporting Information S1.2).
124 Therefore, the displacement of the colloidal particle in horizontal direction Δx and
125 vertical direction Δz within a short time step of Δt can be obtained by:

$$126 \quad \Delta x = u\Delta t + \sqrt{2 \times 2D\Delta t} \sin \theta \quad (1a)$$

$$127 \quad \Delta z = -v\Delta t + \sqrt{2 \times 2D\Delta t} \cos \theta \quad (1b)$$

128 where D is the diffusion coefficient that can be calculated by the Stokes-Einstein
 129 relationship,⁴⁶ with the term $\sqrt{2 \times 2D\Delta t}$ accounts for the colloidal particle diffusion in
 130 a 2D plane.⁴⁷ Furthermore, the term θ is a randomly generated angle ($0 - 2\pi$) for
 131 modelling of the “random walk” of the colloidal particle, which resolves the random
 132 walking distance into the horizontal and vertical components ($\sqrt{2 \times 2D\Delta t} \sin\theta$ and
 133 $\sqrt{2 \times 2D\Delta t} \cos\theta$, respectively). It is worthwhile to note that the vertical velocity v can
 134 be estimated according to the local water flux (Supporting Information S1.3).

135

136 **CA modelling of colloidal particle attachment.** The MC simulation can be used to
 137 determine the collision events. With the membrane placed at $z = 0$, a collision is
 138 recognized when the value of z turns to negative (Supporting Information S1.4). The
 139 probability of successful attachment can be described by the Boltzmann distribution:³⁷

$$140 \quad \frac{N_a}{N_b} = \frac{1}{\exp\left(\frac{\Delta E}{k_B T}\right)} \quad (2)$$

141 where N_a and N_b denote the fraction of attached and unattached colloidal particles,
 142 respectively, for the collision events; k_B and T are the Boltzmann’s constant and the
 143 absolute temperature, respectively. The term ΔE is the difference in potential energy
 144 between the attached vs. non-attached states. In the context of membrane fouling, ΔE
 145 is contributed by (1) the energy barrier ΔE_b arising from foulant-membrane interaction,
 146 and (2) the hydrodynamic interaction caused by the drag force exerted on the colloidal
 147 particle under the flux J .³⁷ Therefore, the probability of successful foulant attachment
 148 α is given by:³⁷

149
$$\alpha = \frac{N_a}{N_a + N_b} = \frac{1}{1 + \exp\left(\frac{\Delta E_b - \beta J}{k_B T}\right)} \quad (3)$$

150

151 Eq. 3 shows that colloidal particles need to overcome the energy barrier ΔE_b in order to
152 achieve a successful attachment. The value of energy barrier is given by F-M interaction
153 ($\Delta E_b = E_m$) for a clean membrane or F-F interaction ($\Delta E_b = E_f$) for a membrane
154 completely covered by foulants (also see Supporting Information S1.5 for the treatment
155 of partially fouled membranes). The value of ΔE_b is highly dependent on colloidal
156 characteristics, membrane properties as well as solution chemistry,⁸ and it can be
157 determined theoretically (e.g., using DLVO or XDLVO theory⁴⁸⁻⁵¹) or experimentally
158 (e.g., by interaction force measurement using atomic force microscope^{21, 52-54}). A
159 greater ΔE_b resists particle deposition, i.e., leading to smaller probability of particle
160 attachment. The term βJ in Eq. 3 arises from the effect of hydrodynamics drag
161 interaction acting on the colloidal particle, where β is a proportionality coefficient that
162 is governed by the drag coefficient.³⁷ A larger water flux J can provide greater permeate
163 drag to overcome the energy barrier, which promotes colloidal deposition.

164

165 As a result of a collision-attachment event, a colloidal particle may disappear from the
166 feed stream and attach to the membrane surface. In this case, the deposited colloidal
167 particle will modify the local permeability of the membrane (see the section “Permeate
168 flux model”) as well as change the localized energy barrier (see Supporting Information
169 S1.5). In the event of an unsuccessful attachment, the colloidal particle will remain in

170 the feed stream, in which case we assume an elastic bouncing (by resetting its new
171 vertical position as $|z|$, see Supporting Information S1.4).

172

173 **Permeate flux model.** The membrane water flux J can be described by:⁵⁵

$$174 \quad J = \frac{\Delta P}{\mu(R_m + R_f)} \quad (4)$$

175 where ΔP is the applied pressure; μ is the solution viscosity; and R_m is the hydraulic
176 resistance of the clean membrane. The foulant resistance R_f is related to the number of
177 attached colloidal particles N_f and the specific cake layer resistance α_N :

$$178 \quad R_f = \alpha_N N_f \quad (5)$$

179

180 By combining the permeate flux model with the CA-MC approach, the stochastic
181 process of colloidal transport and attachment as well as the membrane flux behavior
182 can be modelled. The detailed simulation procedures are presented in Supporting
183 Information S1.6, with the typical simulation parameters given in Table 1.

184

185 **Table 1. Simulation parameters**

	Parameters	Value	Remarks
Particle properties	Particle size, d_p	2.0×10^{-8} m	Ref. ³⁷
	Particle density, ρ	1.5×10^6 g/m ³	See note ^a
	Particle mass, m_p	$\rho\pi d_p^3/6$	In g/#
Solution properties	Absolute temperature, T	298.15 K (25°C)	Ref. ¹⁰
	Solution viscosity, μ	8.9×10^{-4} Pa.s	Ref. ¹⁰
	Foulant mass concentration, C_b	5.0 g/m ³	Ref. ¹⁰
	Particle number concentration, C_n	C_b/m_p	In #/m ³
Operation conditions	Applied pressure, ΔP	0.2-2.0 MPa	
	Crossflow velocity, u	0.2 m/s	Ref. ³⁷
	Membrane intrinsic resistance, R_m	4.5×10^{13} m ⁻¹	Ref. ³⁷
	Specific cake resistance, α_N	$\alpha_f \times m_p$	See note ^b
	Water permeate flux, J	$\Delta P / (R_m + \alpha_N \times N_f)$	Eqs. 4 & 5
Diffusion	Boltzmann's constant, k_B	1.38×10^{-23} J/K	
	Diffusion coefficient, D	$k_B T / 3\pi\mu d_p$	Ref. ⁴⁶
Energy	Unit energy, $k_B T$	4.11×10^{-21} J	
	Energy barrier, ΔE_b	0-12 $k_B T$	See note ^c
	Drag energy coefficient, β	$4.19 \times 10^{-9} \times d_p$	Ref. ³⁷
Channel dimension	Boundary thickness, δ	5.0×10^{-6} m	Ref. ^{10, 37}
	Boundary length, L	5.0×10^{-5} m	
	Length of each region, L_e	1.0×10^{-6} m	
Simulation time	Time step, Δt	5.0×10^{-3} s	
	Maximum particle lifetime, t_{max}	$D \times (\exp(\delta J / D) - 1) / J^2$	See Supporting Information S3

186 Notes:

187 a. The value of m_p was adopted according to the previous reports on particle density for humic acid
 188 (HA).⁵⁶

189 b. α_N (in m/#) was determined via α_f (also the specific cake resistance in m/g), and in this study $\alpha_f =$
 190 3.0×10^{13} m/g was applied according to Ref. ³⁷

191 c. The energy barrier is given by F-M interaction (E_m) for a clean membrane, F-F interaction (E_f)
 192 for a severely fouled membrane, and their hybrid during the fouling transition (see Supporting
 193 Information S1.5).

194

195 **MODEL VALIDATION**

196 In this study, we validate the CA-MC simulation by (1) comparing the particle

197 concentration polarization (CP) behavior obtained from our simulation with a
198 theoretical model,³⁷ and (2) comparing the simulated flux behavior with experimental
199 data.

200

201 The degree of CP at a distance of z away from the membrane surface is given by (see
202 Supporting information S2 and Ref.³⁷):

$$203 \frac{C_z - \alpha C_m}{C_n - \alpha C_m} = \exp\left(\frac{J}{D}(\delta - z)\right) \quad (6)$$

204 where C_n , C_m and C_z are the particle concentration in bulk flow, near the membrane
205 surface and at a distance z away from the membrane, respectively. Compared to the
206 classical CP model (e.g., $C_m/C_n = \exp(\delta J/D)$),^{46,57} Eq. 6 incorporates an additional term
207 αC_m to account for the loss of particles from the solution due to particle deposition on
208 the membrane (which is a depolarization mechanism often overlooked in traditional CP
209 models^{46,57-59}). Figure 1a presents the CA-MC model simulation (the discrete data
210 points) and the theoretical prediction based on Eq. 6 (the solid lines) at different values
211 of attachment coefficient ($\alpha = 0, 0.01, 0.1$ and 1). In general, the model simulation
212 agrees well with the theoretical CP lines. Specifically, severe CP occurs at $\alpha = 0$ (no
213 particle attachment, $C_m \gg C_n$). Increasing the value of α leads to less severe CP due to
214 the removal of particles from the solution phase, with a significantly reduced CP even
215 for an α of merely 0.01 . At $\alpha = 1$ (every collision leads to attachment), both the CA-MC
216 simulation and the theoretical model predict negligible CP. In Figure 1a, the scattering
217 of CA-MC simulation results is due to the random Brownian motion of individual

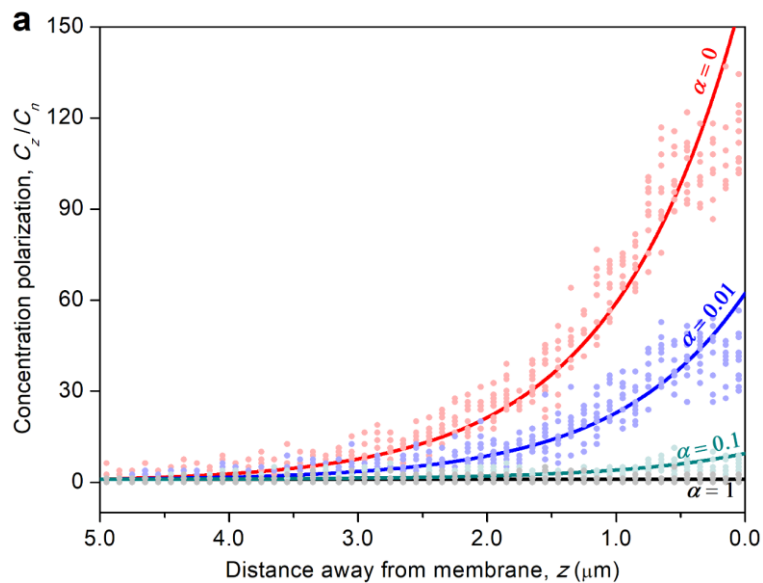
218 colloidal particles, confirming the ability of our approach for capturing the stochastic
219 nature of particle transport and deposition.

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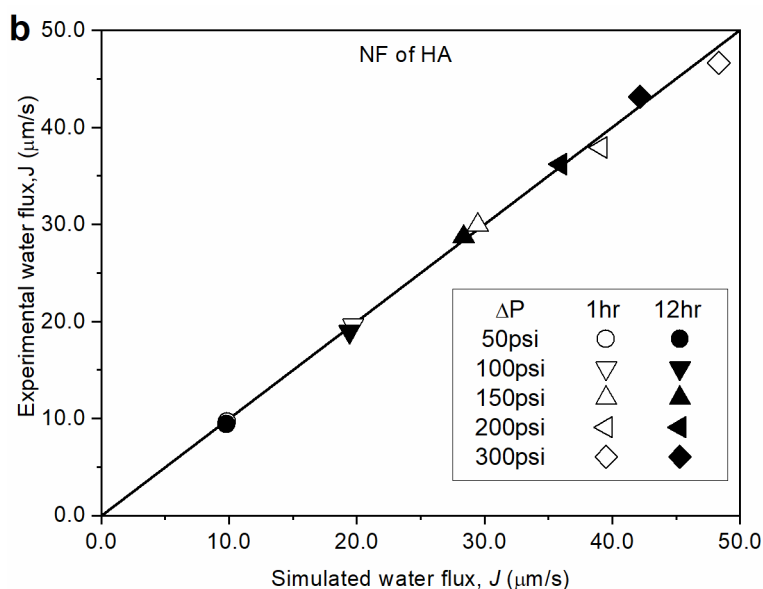
221 Figure 1b further compares the simulated water flux from the CA-MC approach with
222 the experimental results for an NF membrane fouled by HA under a wide range of
223 applied pressure (50 – 300 psi). In all cases, the simulation results agree well with the
224 experimental data. The simulation also correctly predicts the greater flux decline at
225 higher applied pressure (or higher initial flux), which is in good agreement with the
226 literature.^{8, 10, 27}

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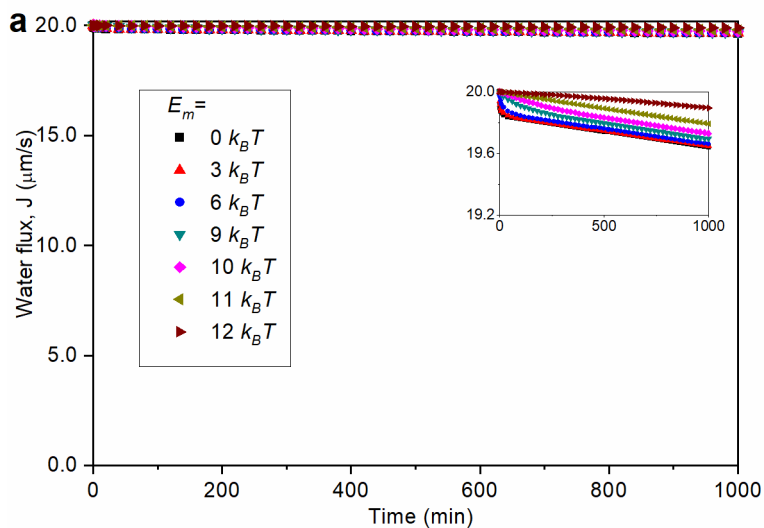
230 Figure 1. Model validation of (a) concentration polarization and (b) water flux decline.
 231 In part (a), the solid lines are based on Eq. 6. The scattered dots represent the simulated
 232 data based on ten runs of CA-MC simulations under a constant water flux ($J=25\mu\text{m/s}$).
 233 In part (b), fouling of an NF membrane by humic acid is simulated under constant
 234 pressure conditions (ranging from 50 to 300 psi, corresponding to initial flux of 10-50
 235 $\mu\text{m/s}$). The experimental data are obtained from Ref. ¹⁰, and the detailed experimental
 236 conditions are documented in our previous reports.^{10, 37} Detailed simulation conditions
 237 for part (b) can be found in Supporting Information S4.

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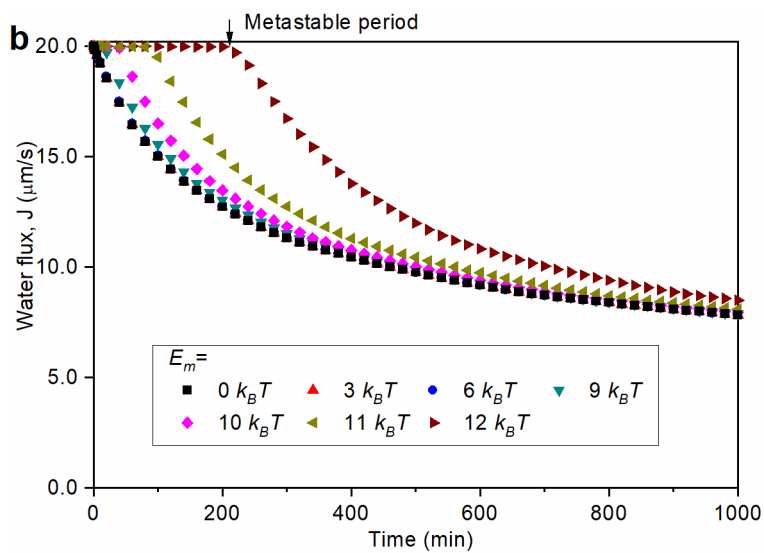
239 SIMULATION RESULTS AND DISCUSSION

240 **Flux behavior.** Colloidal fouling of a clean membrane is governed by the energy
241 barrier resulting from F-M interaction (E_m), while that of a severely fouled membrane
242 is governed by the energy barrier resulting from F-F interaction (E_f). According to Eq.
243 3, a higher energy barrier can lead to a greatly reduced probability of attachment and
244 thus slower fouling. Figure 2a shows the flux behavior at a relatively high E_f ($11 k_B T$)
245 for a wide range of E_m ($0-12 k_B T$). With an initial flux of $20 \mu\text{m/s}$, no obvious flux
246 decline ($<2\%$) occurred regardless of the value of E_m . Even for the case of $E_m = 0$ (i.e.,
247 the clean membrane presents no energy barrier against colloidal fouling), the membrane
248 surface will be coated by the foulant to result in a highly repulsive F-F interaction that
249 effectively slows down further foulant deposition, leading to a self-terminated fouling
250 behavior. One example of such scenario could be the use of a negatively charged
251 membrane for filtration of positively charged foulant. For example, Wang et al.⁶⁰
252 observed a relatively stable long-term flux after an initial slight flux decline for the
253 filtration of lysozyme by a NF membrane (NF270) thanks to the more repulsive F-F
254 interaction.
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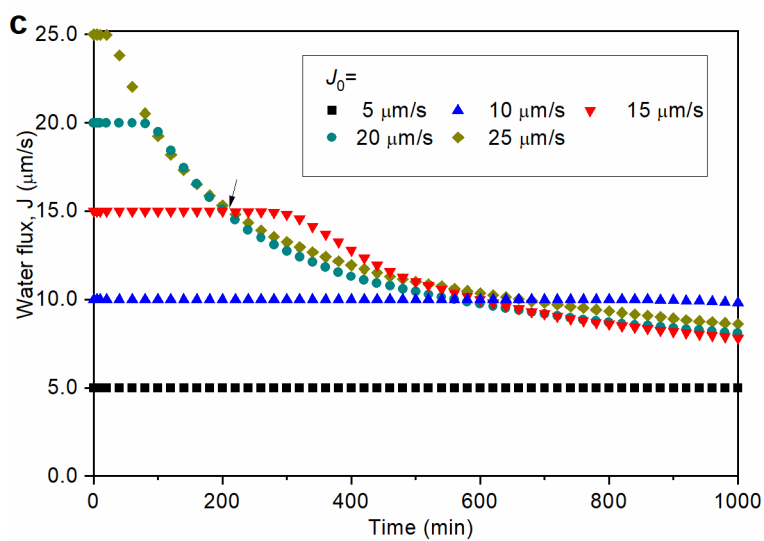
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258



259 Figure 2. Effect of energy barrier and initial flux on flux behavior. (a) Effect of E_m at E_f
 260 $= 11 k_B T$ and $J_0 = 20 \mu\text{m/s}$; (b) Effect of E_m at $E_f = 3 k_B T$ and $J_0 = 20 \mu\text{m/s}$; (c) Effect of
 261 J_0 at $E_m = 11 k_B T$ and $E_f = 3 k_B T$. See other simulation parameters in Table 1.

262

263 Much severer flux decline occurs for a lower E_f value of $3 k_B T$ (Figure 2b). At a long
264 filtration time of 1000 min, the decline in water flux is largely independent of E_m ($0-12$
265 $k_B T$). This result agrees well with the existing literature: the long-term fouling behavior
266 is independent of membrane surface properties once the surface is masked by foulant.⁸
267 ¹⁰ Nevertheless, our simulation clearly shows that the initial fouling behavior is strongly
268 dependent on E_m , with a greater E_m favorable in retarding fouling. A metastable flux
269 behavior appears for $E_m > 9 k_B T$. For example, at $E_m = 12 k_B T$, stable flux can be
270 maintained initially before the occurrence of an obvious decline at around 220 min.
271 This metastable period decreases for smaller E_m values and becomes barely noticeable
272 with a value of 17 min at $E_m = 9 k_B T$. These results underpin the critical importance of
273 developing antifouling membranes with more repulsive F-M interaction, which
274 prevents the fouling of clean membranes by minimizing the attachment coefficient α
275 (Eq. 3). Our results are also consistent with a recent experimental study reporting stable
276 flux for a superhydrophilic NF membrane over 60 h (attributed to strong repulsive acid-
277 base F-M interaction), yet the metastable period was less than 1h for other membranes
278 with less repulsive interactions.¹⁹ In Figure 2b, the flux decline accelerates after the
279 metastable period. This phenomenon can be explained by the conditioning of the
280 membrane surface by the deposited foulant, eventually transitioning into a F-F
281 dominated behavior.^{8, 10} Consequently, fouling in the later stage becomes nearly
282 independent of membrane surface properties.^{10, 22} In the current study, the metastable

283 fouling behavior resulting from the combination of high E_m and low E_f is somewhat
284 analogous to homogenous crystalization. The slow nucleation in crystalization (due to
285 the need to overcome the energy barrier for creating new surfaces) can result in
286 metastable conditions without crystal formation for supersaturated solutions.²⁵

287

288 The metastable fouling behavior is also strongly dependent on the initial water flux J_0 .
289 Figure 2c shows the flux behavior for various values of J_0 at fixed E_m ($11 k_B T$) and E_f
290 ($3 k_B T$). Reducing J_0 from 25 to 15 $\mu\text{m/s}$ not only makes fouling less severe but also
291 greatly extends the metastable period from 30 min (at 25 $\mu\text{m/s}$) to approximately 310
292 mins (at 15 $\mu\text{m/s}$). At lower J_0 of 10 and 5 $\mu\text{m/s}$, membrane flux remains stable over
293 the entire simulation period of 1000 min. The critical importance of initial water flux
294 has been well documented in the literature: higher water flux accelerates convection of
295 colloidal particles, promotes more severe CP, and exerts greater drag effects towards
296 the membrane surface.^{8, 10, 27, 37, 40, 61, 62} The current study reveals that the metastable
297 behavior is governed by the interplay between E_m and J_0 , with a longer metastable
298 period obtained at greater E_m (Figure 2b) and lower J_0 (Figure 2c). According to Eq. 3,
299 a combination of large E_m and low J_0 ensures a low probability of colloidal particle
300 attachment to the clean membrane, slowing down the membrane conditioning and thus
301 extending the metastable period.

302

303 Figure 2c also shows a flux crossover behavior. For the flux curve started with the

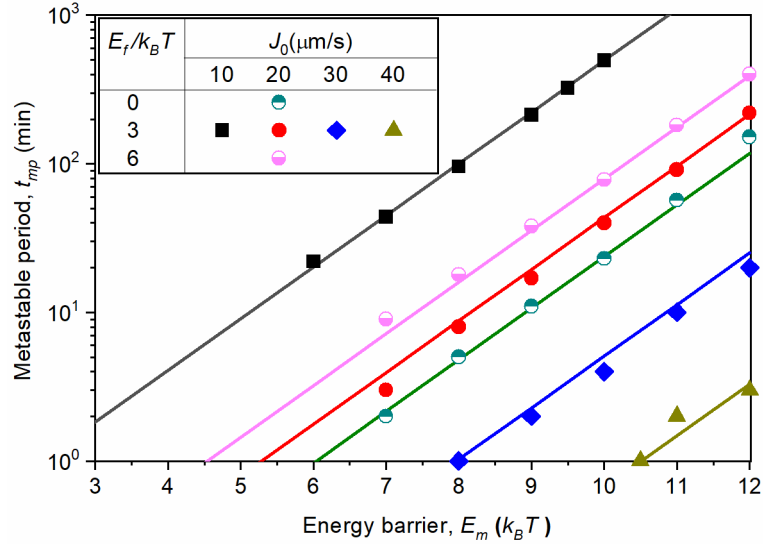
304 highest J_0 of 25 $\mu\text{m/s}$, fouling is so rapid that it quickly transits into a F-F dominated
305 region. This flux curve crosses over with one for $J_0 = 15 \mu\text{m/s}$ at around 200 min
306 (indicated by the arrow in Figure 2c). At this crossover point, the two fouling curves
307 have the same flux, but the one started with $J_0 = 25 \mu\text{m/s}$ continues with a rapid rate of
308 flux decline (due to the dominance of F-F interaction with $E_f = 3 k_B T$) and the one with
309 $J_0 = 15 \mu\text{m/s}$ remains metastable (due to the dominance of F-M interaction with $E_m =$
310 $11 k_B T$). Similar crossover also happens for $J_0 = 10 \mu\text{m/s}$ at longer duration. The current
311 study reveals that the use of a higher initial flux results in an earlier transition from F-
312 M ($E_m = 11 k_B T$) to F-F ($E_f = 3 k_B T$). This transition reduces the membrane's ability to
313 resist further foulant deposition, which is responsible for the flux crossover behavior.
314 Therefore, excessively high water flux should be strictly prohibited to avoid premature
315 occurrence of F-M to F-F transition.

316

317 **Metastable Period.** To achieve a better understanding of the metastable period, we
318 analyze a wider selection of flux-interaction energy combinations. Figure 3 plots the
319 metastable period t_{mp} as a function of E_m and J_0 , with the discrete data points obtained
320 from the CA-MC simulation. At each given J_0 , the logarithm of the metastable period
321 ($\ln t_{mp}$) appears to be linearly dependent on the F-M interaction energy E_m , with a
322 doubling in t_{mp} for every increase of E_m by 0.8-0.9 $k_B T$. Meanwhile, the metastable
323 period increases at lower J_0 (doubling in t_{mp} for every decrease of J_0 by approximately
324 $3 \mu\text{m/s}$). Although the metastable period has the strongest dependence on E_m and J_0 , we

325 also found that it has a weak dependence on E_f (with a larger E_f favoring extended
 326 metastable period).

327



328

329 Figure 3. Effects of energy barrier and initial flux on the metastable period. A threshold
 330 flux decline rate of 1‰ per minute is applied. The scattered dots represent the
 331 simulation results based on the CA-MC model. Simulation conditions: $E_m = 6-12 k_B T$,
 332 $E_f = 0-6 k_B T$, $J_0 = 10-40 \mu\text{m/s}$, and other conditions are shown in Table 1. The solid lines
 333 are fitting lines given by $\ln t_{mp} = 0.8E_m/k_B T + 0.2E_f/k_B T - 0.174J_0 - \ln(0.00159J_0) - 4.79$,
 334 with t_{mp} in min and J_0 in $\mu\text{m/s}$ ($R^2=0.9945$). The theoretical basis of the fitting lines is
 335 provided in Supporting Information S5.

336

337 **Transitional fouling behavior.** The CA-MC simulation is capable of resolving the
 338 fine details of transitional fouling behavior. Figure 4a-d presents the evolution of the
 339 foulant distribution pattern over time for different combinations of E_m and E_f at a fixed
 340 J_0 of $20 \mu\text{m/s}$, with the color scale representing the area number density of deposited
 341 colloidal particles (i.e., the number of particles deposited in each simulation grid with
 342 an area of $0.1 \mu\text{m}^2$ in the current study). As expected, the combination of high E_m (11
 343 $k_B T$) and high E_f (11 $k_B T$) results in very slow particle accumulation (Figure 4a), thanks

344 to the strongly repulsive F-M and F-F interactions. It takes approximately 400 min to
345 reach an average density of 100 particles per grid (#/grid), and the number is only about
346 250 #/grid over the entire 1000-min simulation (Figure 4e). Lowering E_m to $3 k_B T$ while
347 keeping E_f at $11 k_B T$ leads to an accelerated initial particle deposition (Figure 4b),
348 reaching 100 #/grid in approximately 2 min owing to the weaker F-M repulsion.
349 Nevertheless, the subsequent deposition of colloidal particles becomes much slower
350 (slightly over 400 #/grid) at 1000 min, Figure 4e), as a result of the rapid conditioning
351 of the membrane surface by the deposited foulant and the transition to a more repulsive
352 F-F interaction. The current study reveals that a high E_f ensures long-term stable
353 membrane operation regardless of the value of E_m (Figure 2a and Figure 4a,b),
354 underpinning the critical importance of pretreatment and adjustment of water
355 chemistry^{22, 60, 63, 64} for practical membrane operations. In contrast, the combination of
356 low E_m ($3 k_B T$) and low E_f ($3 k_B T$) results in almost instantaneous particle deposition as
357 well as severe long-term fouling (Figure 4d), reaching approximately 100 #/grid in the
358 first min and 37,000 #/grid by the end of the 1000-min simulation (Figure 4e).

359

360 The combination of high E_m ($11 k_B T$) and low E_f ($3 k_B T$) presents an interesting scenario
361 (Figure 4c). Owing to the highly repulsive F-M interaction, the initial particle
362 deposition is rather slow (Figure 4e), in good accordance with its initial metastable
363 water flux (Figure 2b). However, a sharp transition occurs during 90 - 200 min (Figure
364 4e), accompanied with greatly accelerated particle deposition with the transition of

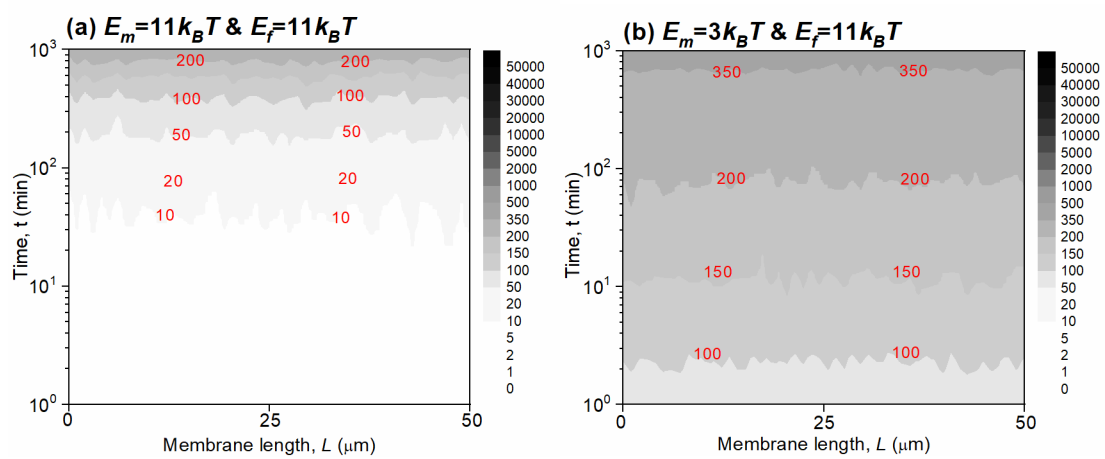
365 strongly repulsive F-M to an unfavorable F-F interaction. Indeed, its initial particle
366 deposition behavior is nearly identical to that for the case of $E_m = 11 k_B T$ and $E_f = 11$
367 $k_B T$ (indicating a F-M dominated behavior), while the long term behavior is nearly
368 identical to that for the case of $E_m = 3 k_B T$ and $E_f = 3 k_B T$ (suggesting a F-F dominated
369 behavior). In addition, the transitional window of 90 - 200 min in Figure 4e also agrees
370 well with the ending of the metastable period (90 min) for the corresponding flux curve
371 in Figure 2b.

372

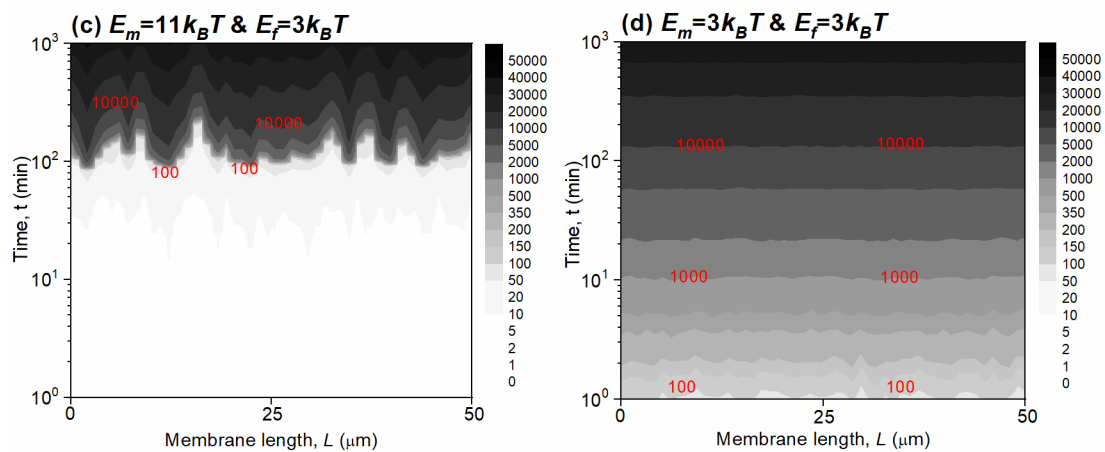
373 A closer examination of the foulant distribution pattern in Figure 4c reveals that it is
374 highly non-uniform (particularly during the transitional period) compared to other cases
375 (Figure 4a, b, d). This difference is also reflected by the larger standard deviation in
376 Figure 4e (represented by the shading) for the combination of high E_m and low E_f (see
377 further discussion in Supporting Information S7). During membrane filtration, colloidal
378 particles are transported towards the membrane surface under the permeate drag, which
379 is resisted by the energy barrier⁸. While the clean membrane with $E_m = 11 k_B T$ is highly
380 antifouling, an accidental deposition of foulant particle would modify the localized
381 surface properties. For the case of $E_f \ll E_m$, it leads to reduced energy barrier locally,
382 which serves as a seed to promote further particle deposition in the vicinity of the
383 existing foulant. Consequently, a patch-like “colonization” behavior is expected, where
384 the fouled patches serve as hot spots to accelerate further particle deposition (also see
385 Supporting Information S6). It is worthwhile to note that the time and location for the

386 occurrence of the patches are highly random due to the stochastic nature of particle
 387 transport and attachment. However, each patch will grow laterally over time to expand
 388 their coverage over the membrane surface, leading to an eventual complete coverage of
 389 the entire membrane. Upon this completion of the F-M to F-F transition, the energy
 390 barrier becomes entirely governed by E_f , rendering the later stage of fouling more
 391 uniform (Figure 4c and Figure 4e).

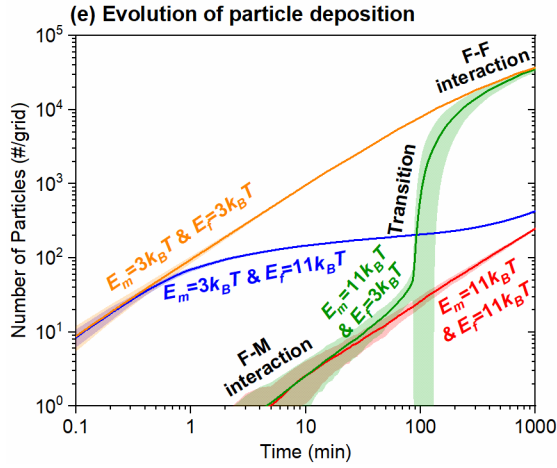
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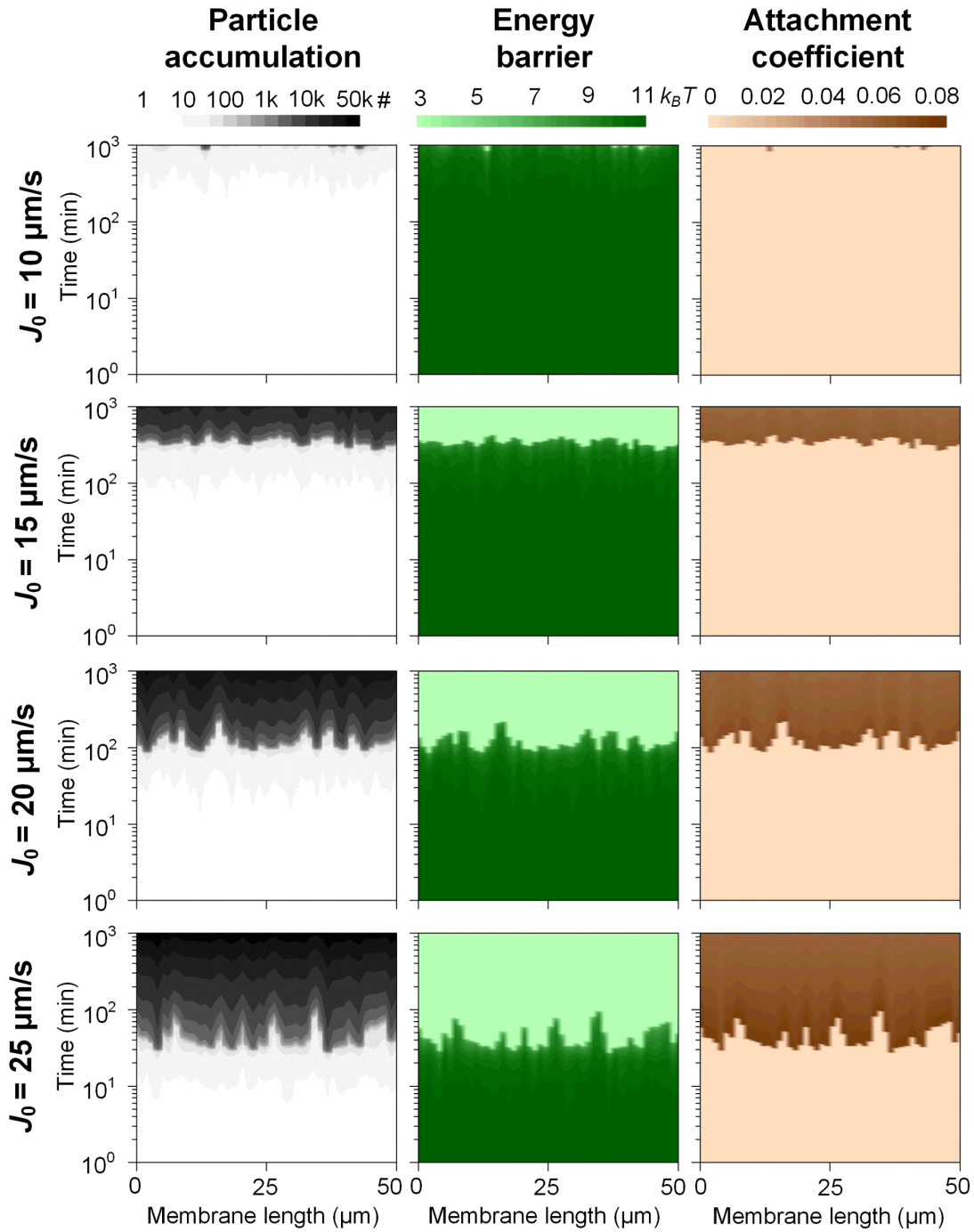
396 Figure 4. The role of energy barrier on the evolution of particle deposition. Parts (a-d)
 397 presents the particle deposition pattern over time for (a) $E_m = 11 k_B T$ and $E_f = 11 k_B T$;
 398 (b) $E_m = 3 k_B T$ and $E_f = 11 k_B T$; (c) $E_m = 11 k_B T$ and $E_f = 3 k_B T$; (d) $E_m = 3 k_B T$ and $E_f =$
 399 $3 k_B T$. The color scale represents the area number density of deposited particles in
 400 number of particles per simulation grid (i.e., the number of particles deposited in each
 401 membrane segment with $0.1 \mu\text{m}^2$ in area). An initial flux J_0 of $20 \mu\text{m/s}$ is used in the
 402 simulation, and other simulation parameters are given in Table 1. Part (e) presents the
 403 average area number density as a function of time for different combinations of E_m and
 404 E_f values. The solid lines represent the average values. The corresponding shadings
 405 represent the standard deviations, which can be used to characterize the uniformity of
 406 foulant deposition. For the case of $E_m = 11 k_B T$ and $E_f = 3 k_B T$, the deposition is so non-
 407 uniform during the transition such that some regions are heavily covered by colloidal
 408 particles while other regions are nearly free of particles. Accordingly, the coefficient of
 409 variation (i.e., the ratio of standard deviation over the average value, also see
 410 Supporting Information S7) for the spatial distribution of particle deposition can be
 411 greater than 1, causing the shading of the curve to cross the horizontal axis.

412

413 To further resolve the transitional fouling behavior, Figure 5 presents the evolution of
 414 particle accumulation, energy barrier, and attachment coefficient over time at different
 415 initial flux values for the case of high E_m ($11 k_B T$) and low E_f ($3 k_B T$). At J_0 of $10 \mu\text{m/s}$,
 416 particle deposition is very slow and the membrane remains largely clean with the
 417 exception of a few minor foulant patches towards the end of the 1000-min filtration
 418 period. This is in good agreement with its extended metastable period (Figure 2c).
 419 Increasing J_0 to $15 \mu\text{m/s}$ results in accelerated particle deposition, which is

420 accompanied with a drop of energy barrier from $11 k_B T$ (resulting from E_m) to $3 k_B T$
421 (resulting from E_f) and a corresponding shift in the attachment coefficient. Indeed, the
422 shape of these patterns largely mirror each other. Further increase in J_0 results in an
423 earlier occurrence of transitional behavior in particle deposition, energy barrier, and
424 attachment coefficient (Figure 5), in good agreement with their shorter metastable
425 period (Figure 2c).

426



427

428 Figure 5. Evolution of particle accumulation, energy barrier, and attachment coefficient
 429 over time at different initial flux values. Simulation conditions: $E_m = 11 k_B T$ and $E_f = 3$
 430 $k_B T$; other parameters given in Table 1.

431

432 **Implications.** For the first time, the current study systematically resolves the F-M to

433 F-F transitional behavior during colloidal fouling using a novel CA-MC approach that

434 captures the stochastic transport and attachment of foulant particles. Our simulation
435 provides the theoretical basis for the metastable flux behavior under the condition of
436 high E_m and low E_f , with the metastable period greatly extended at increased energy
437 barrier (E_m and E_f) and lower flux. This study provides critical implications for
438 membrane design and process operation. In view of the great impact of water chemistry
439 on both F-M and F-F, pretreatment of problematic feed water provides effective
440 protection to RO and NF membranes. Although a large E_f can effectively minimize
441 fouling, its value is often constrained by the characteristics of the feed water (e.g.,
442 foulant type and properties). For applications prevailed with unfavorable E_f values, the
443 development of membranes with high E_m values is essential to achieve antifouling and
444 to maintain a stable operation over extended periods.¹⁹ Nevertheless, it is important to
445 realize that even the best antifouling membrane may fail when it is subjected to
446 excessive flux (Figure 2c), due to the premature transition from F-M to F-F. Therefore,
447 operating below the threshold flux^{10, 11, 13, 37} is critical to prevent such premature
448 membrane failures. In practice, moderate flux is often applied (e.g., 12-17 Lm⁻²h⁻¹ for
449 seawater desalination and 12-45 Lm⁻²h⁻¹ for brackish water treatment).² The
450 combination of moderate flux and large E_m is of great practical significance to extend
451 the metastable period and thus to minimize the required cleaning frequency (e.g., into
452 months or even years).

453

454 Our study also reveals the critical role of initial foulant “colonization” in the

455 modification of the localized energy barrier (Figure 5). Therefore, upon the initial
456 occurrence of foulant patches, timely cleaning is critical to prevent severe propagation
457 of further particle deposition and to restore the unfavorable F-F interaction to the more
458 repulsive F-M interaction. While existing membrane cleaning studies generally focus
459 on cleaning chemistries and choices of methods (e.g., air scouring, backflushing, and
460 chemical cleaning^{63, 65, 66}), future studies also need to emphasize the timing of cleaning
461 in relation to the metastable fouling behavior and the onset of the F-M to F-F transition.
462 Our study also implies the critical importance of early fouling detection for effective
463 management of membrane operation and cleaning.

464

465 **ASSOCIATED CONTENT**

466 **Supporting Information**

467 The Supporting Information is available free of charge on the ACS Publications website.

468 S1. CA-MC model; S2. Concentration polarization model; S3. Derivation of maximum

469 particle lifetime; S4. Parameters used for model validation; S5. Derivation of

470 metastable period; S6. Colloidal particle deposition during fouling transition; S7.

471 Uniformity of colloidal particle deposition; S8. Role of cake compressibility on fouling;

472 S9. MATLAB code for the CA-MC simulation.

473

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480 **Notes**

481 The authors declare no competing financial interest.

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