

25 **INTRODUCTION**

26 Evaluation of site response to earthquakes plays an important role in seismic design
27 of engineering structures. Most of site response analyses have concentrated on
28 horizontal ground motion, in which site response is regarded as the consequence of
29 the vertical propagation of shear waves in a horizontally layered system. Although it
30 has long been recognized that the ground is simultaneously subjected to shaking in
31 both horizontal and vertical directions during a real earthquake, vertical ground
32 motion, as compared with its horizontal counterpart, has received much less
33 attention. As a result, knowledge with regard to the characteristics of vertical ground
34 motion and, particularly, with regard to relating vertical and horizontal ground
35 motions is rather limited. The common procedure for generating vertical design
36 spectra, as documented in many seismic provisions and codes (e.g., UBC, 1997), is to
37 simply multiply a factor (typically a value of 2/3) to the horizontal design spectra
38 (Fig. 1). In other words, it is assumed that the response spectral ratio between vertical
39 and horizontal motions is a constant less than 1 over the entire period of interest and
40 for all site conditions.

41 However, several studies on ground motion records obtained in recent
42 earthquakes have shown that the constant (V/H) ratio is not a good descriptor (e.g.,
43 Yang and Sato, 2000; Elgamal and He, 2004; Yang and Lee, 2007). The response
44 spectral ratio (V/H) depends on a number of factors (e.g., site-to-source distance and
45 source mechanism), and can be significantly greater than 2/3 at short periods in
46 moderate and large earthquakes. In the most recent Wenchuan, China earthquake of

47 May 12, 2008, vertical ground acceleration as large as 0.633 g (g is the gravity) was
48 recorded in the epicenter zone.

49 From a geotechnical engineering perspective, it is of particular interest to
50 identify the influence of such factors as the intensity of earthquake motion, the
51 location of input motion (or control motion), the depth of water table, and the
52 damping property of soil on the behavior of vertical motion as well as its relation
53 with the horizontal motion. This is precisely the purpose of the present study. In an
54 earlier study by Yang and Yan (2009), a simple procedure was proposed for analysis
55 of the ground response under both vertical and horizontal earthquake loading;
56 validation of the analytical procedure against the downhole array records at the
57 Turkey Flat test site in California showed reasonably good agreement between
58 predictions and measurements. By using this newly developed procedure, a series of
59 analyses have been carried out for a hypothesized site with the aim to explore several
60 potential influencing factors. The main results derived from these analyses are
61 presented in this paper.

62

63 **HYPOTHESIZED SITE AND INPUT MOTION**

64 The hypothetical soil site is shown in Fig. 2. The soil profile is 30 m deep comprising a
65 surface sandy clay layer of 10 m and an underlying sand layer of 20 m. The water
66 table is located at the depth of 5 m below the ground level. The mass density of the
67 clay is assumed to be 1800 kg/m^3 and the density of the sand is 2000 kg/m^3 . The shear
68 wave velocity, V_s , varies from 170 m/s in the clay layer to 350 m/s in the sand layer.

69 Using the UBC site classification system, the site can be categorized to be a stiff-soil
70 site. On the other hand, the compressional wave velocity, V_p , is assumed to vary from
71 360 m/s in the clay above the water level, to 1561 m/s in the clay below the water level,
72 and to 1788 m/s in the sand. The location of bedrock is assumed to be at the depth of
73 30 m, with the shear wave velocity of 470 m/s and the compressional wave velocity of
74 2007 m/s.

75 The nonlinear behavior of the sandy clay in terms of the shear modulus
76 reduction curve and the damping ratio curve is described using the proposal by Sun
77 *et al.* (1988), while the nonlinear behavior of the sand is assumed to follow the curves
78 developed by Seed and Idriss (1970). The input motions used in this study are shown
79 in Fig. 3 in terms of acceleration time histories and response spectra at 5% damping.
80 They are the north-south and up-down components of the acceleration records
81 obtained at the Mount Wilson station during the 1987 Whittier Narrows earthquake
82 in California. The peak horizontal acceleration appearing at 2.84 s is 1.482 m/s², and
83 the peak vertical acceleration, 0.756 m/s², occurs at 3.08 s. As can be seen in Fig. 3(b),
84 the spectral accelerations in both directions take the maxima at periods of
85 approximately 0.16 s.

86

87 **INFLUENCE OF INPUT MOTION INTENSITY**

88 Among various measures of earthquake ground motion, peak acceleration has been
89 widely used in engineering practice to characterize the intensity of seismic loading.
90 To investigate its effect, the original horizontal and vertical acceleration records given

91 in Fig. 3 are scaled simultaneously by multiplying factors of 0.5 and 2, respectively, to
92 produce two more sets of acceleration records having different intensity levels. The
93 three sets of records are referred to as Level 1, 2 and 3 hereafter. Analyses have been
94 performed by subjecting the hypothesized soil profile to these three sets of
95 accelerations, which were all specified at the rock outcrop (see Fig. 2).

96 Figure 4 shows the influence of motion intensity on the transfer functions for
97 horizontal and vertical motions. It is clear that site frequencies in both components
98 decrease with increasing intensity level or increasing peak acceleration. For Level 1
99 earthquake motion (the weakest case), the fundamental frequency is at 2.5 Hz for the
100 horizontal component and 12.5 Hz for the vertical component. By comparison, they
101 are reduced to be 2.2 and 11 Hz in the case of Level 3 earthquake motion. In the
102 meantime, peak values of the spectral ratios in both components are reduced
103 substantially when the intensity of input motion increases. For example, the vertical
104 amplification at the fundamental frequency drops from approximately 25 at Level 1
105 motion to about 13 at Level 3; the horizontal amplification at the fundamental
106 frequency varies from approximately 17 at Level 1 to less than 10 at Level 3 input
107 motion.

108 The above observations are mainly attributed, as will be shown later, to the
109 following two effects. First, higher peak acceleration causes a higher hysteretic
110 damping and therefore a larger reduction of site amplification. Second, higher peak
111 acceleration results in larger strains and reduced moduli and thus lower frequency
112 response.

113 Site amplification has sometimes been simply examined in practice by a factor
114 which is defined as the ratio between the peak acceleration at the ground surface and
115 the peak acceleration at the base of soil deposit (e.g., Idriss, 1990) Following this
116 practice, the amplification factors for both horizontal and vertical motions are
117 calculated for the three cases of intensity levels and summarized in Table 1. It is noted
118 that the amplification factor for horizontal motion decreases with increasing intensity
119 level. The amplification factor for vertical motion, however, is found to be an
120 increasing function of the intensity level. This implies that the so-defined
121 amplification factor, as compared with the transfer function given in Fig. 4, is not an
122 appropriate indicator for soil nonlinearity involved with vertical motion.

123 As far as the ratio between peak vertical and horizontal accelerations (V/H) is
124 concerned, it is interesting to note that the ratio increases with increasing intensity at
125 the ground surface but decreases with increasing intensity at the base of the soil
126 deposit. Consequently, the surface-to-base (V/H) ratio is an increasing function of the
127 intensity of input motion.

128 The influence of the intensity of input motion on surface response spectra is
129 shown in Fig. 5 for both horizontal and vertical motions. Again, the influence is
130 observed to be significant on both components. In the case of Level 1 input motion,
131 the peak spectral acceleration in the horizontal direction is approximately 1/3 of that
132 under Level 3 input motion. Similarly, the peak spectral acceleration in vertical
133 direction at Level 3 is about 5 times the peak value at Level 1 input motion. It is worth
134 noting from Fig. 6 that, while the intensity of input motion has a profound influence

135 on both individual components, its impact on the response spectral ratio between the
136 vertical and horizontal motions (V/H) appears to be less significant. With increasing
137 the motion intensity, a slight increase in the (V/H) spectral ratio occurs for periods
138 lower than 0.2 s; for longer periods the influence becomes negligible and the (V/H)
139 ratio is generally less than 2/3. In the period range of 0.05-0.2 s, the (V/H) ratio
140 substantially exceeds 2/3 regardless of the intensity of input motion.

141 Shown in Fig. 7 are the variations with depth of peak accelerations in
142 horizontal and vertical directions for the three intensity levels. The influence of the
143 motion intensity on the profiles of peak stresses and peak strains is presented in Fig. 8.
144 Generally, higher intensity level causes larger response in both components. It is to be
145 noted that there is a dramatic variation in peak horizontal acceleration occurring at a
146 depth of 5 to 10 m, while a high gradient of peak vertical acceleration appears at a
147 depth of about 5 m. Significant variations in shear and normal strains are observed in
148 similar zones. Recalling the soil profiles given in Fig. 2, the observed variations are
149 considered reasonable.

150 Figure 9 presents the profiles of the degraded shear and constrained moduli
151 and the shear-strain compatible damping ratio (ζ_h) under different intensity levels of
152 input motion. It can be seen that the higher the input motion intensity, the smaller the
153 moduli and the larger the damping ratio. With respect to the shear modulus, the
154 influence of intensity tends to be appreciable in the sand layer below the depth of 10
155 m. The influence on the constraint modulus, however, becomes notable for soils
156 below the depth of 5 m. This is consistent with the previous observation on the

157 variation of normal strain, and is thought to be associated with the variation of the
158 compressional wave velocity and Poisson's ratio with depth.

159

160 **INFLUENCE OF LOCATION OF INPUT MOTION**

161 In site response analysis there are generally two options to input earthquake motion:
162 one is to specify the motion at a rock outcrop, as done in the above case analyses, and
163 the other is at the bedrock or soil-rock interface (Fig. 2). In the former case the
164 incident waves are equal in amplitude with the reflected waves at the rock outcrop,
165 as required by the free-stress condition. In the theoretical procedure used herein, this
166 case is handled by introducing a radiation dashpot at the soil-rock interface, with the
167 damping coefficients determined from the properties of the bedrock. For the later
168 case, the response of the site can be established directly by solving the displacement-
169 force equation as described by Yang and Yan (2009). Since there has been confusion
170 with the bedrock and outcrop inputs, an effort is made here to clarify this issue by
171 examining the difference in ground response for two cases: in one case the
172 earthquake motion is input at the rock outcrop and in the other case the same motion
173 is input at the bedrock.

174 Using the acceleration records given in Fig. 3 as the bedrock and outcrop input
175 respectively, the response spectra of ground surface motions were calculated and are
176 compared in Fig. 10. In both plots the curves for the case of outcropping input are
177 denoted as "outcropping" while the curves generated from the case of bedrock input
178 are labeled as "bedrock". Shown in Fig. 11 are the profiles of peak accelerations in

179 both directions for the two cases. The results for stresses and strains in the two cases
180 are presented in Fig. 12.

181 The overall observation on these figures is that, compared with the case of
182 outcropping input, the response of the site to the same earthquake motion but input
183 at the bedrock is stronger in both vertical and horizontal directions. Accordingly, in
184 the case of bedrock input more significant modulus reduction and higher damping
185 are observed (Fig. 13). These observations are reasonable because in the outcropping
186 case, perfect reflection occurs due to the free stress conditions (i.e. reflected waves are
187 equal to incident waves), whereas in the bedrock case part of the incident waves are
188 transmitted into the soils resulting in the reflected waves of being less than the
189 incident waves. More detailed discussion on the relation between bedrock motion
190 and outcropping motion can be referred to Yang and Yan (2009).

191 Moreover, the difference in the modulus reduction and damping ratio will
192 bring about changes in site frequencies in both horizontal and vertical components.
193 For example, the fundamental frequency of the vertical motion in the case of bedrock
194 input is about 94% of that in the case of outcropping input. It should be noted that the
195 change of input motion position will not cause difference in the transfer function for
196 either component if the nonlinear behavior of the soil is not taken into account.

197 With respect to the response spectral ratio (V/H) at the ground level, Fig. 14
198 shows that the ratio is substantially increased at short periods (less than 0.2 s) but
199 slightly decreased at periods longer than 0.2 s when the location of input motion
200 changes from rock outcrop to the base of the soil deposit.

201 Table 2 gives peak values of the horizontal and vertical surface accelerations in
202 the two cases of input motion position. Note that the influence of input motion
203 position is more significant for vertical motion than for horizontal motion; this is also
204 observed on Fig. 10. As for the ratio between peak vertical and peak horizontal
205 accelerations at the ground surface, the results show that it increases from 0.5 for
206 outcropping input to 0.98 for bedrock input.

207

208 **INFLUENCE OF WATER LEVEL**

209 The analysis of Yang and Sato (2000) on the downhole array records at a reclaimed
210 site in Kobe, Japan has indicated that the variation of water table plays an important
211 role in the amplification of vertical ground motion. To further investigate this effect,
212 three cases of water levels are examined in parallel in this section (Fig. 15): the first
213 case is for water level at the surface (i.e. WL=0 m), the second case is for water level at
214 5 m below the surface (i.e. the case discussed previously), and in the third case the
215 depth of water table is at 10 m. Note that in the three cases the profiles of the shear
216 wave velocity (V_s) are assumed to be identical but the profiles of the compressional
217 wave velocity (V_p) vary with the change of water table. In the case of WL=0 m, V_p is
218 assumed to vary from 1561 m/s in the clay layer to 1785 m/s in the underlying sand,
219 whereas in the case of WL=10 m, it is assumed to vary from 360 m/s in the clay to
220 1785 m/s in the sand layer.

221 The above assumption for the variations of V_p and V_s is based on the results of
222 the studies by Yang and Sato (2000) and Yang *et al.* (2004), which indicate that the

223 presence of ground water has a significant influence on the compressional wave
224 velocity but little influence on the shear wave velocity and that a dramatic change in
225 the compressional wave velocity may occur at the location of water table.

226 Figure 16 compares vertical ground surface motions computed for the three
227 water levels in terms of the acceleration time histories. Shown in Fig. 17 is the
228 influence of water level on the surface response spectra and the transfer function for
229 vertical motion. Clearly, the variation of water table brings about a profound effect on
230 the behavior of vertical motion. The transfer function will be shifted to the low
231 frequency end when the water table is lowered. For example, the fundamental
232 frequency is found to be at 13.4 Hz when the water table is at the ground surface, but
233 it drops to 7.4 Hz when the depth of water table becomes 10 m. In the meantime,
234 lowering water table brings about a much stronger amplification of vertical motion,
235 as can be seen from Fig. 17(a). The peak spectral acceleration in the case of WL=10 m
236 is about 3 times that in the case of WL=0 m.

237 With respect to the relation between vertical and horizontal motions, Fig. 18
238 shows that the variation of water table can also significantly affect the response
239 spectral ratio (V/H) at the ground surface. For water level at the surface, the (V/H)
240 spectral ratio is generally below the value of $2/3$ in the whole range of period. If the
241 water level is lowered to the depth of 10 m, the ratio will increase sharply for periods
242 shorter than about 0.2 s, with the peak value of as large as 2.3. On the other hand, the
243 influence of varying water table is found to be slight for the spectral ratio (V/H) at
244 periods longer than 0.6 s.

245 Shown in Fig. 19 are distributions with depth of the peak vertical acceleration
246 and vertical velocity under different water levels. High gradients are found to occur
247 at the depth that is close to the water table. Taking the case of WL=10 m as an
248 example, peak vertical acceleration is increased only by 26% when seismic waves
249 travel from the base to the depth of 10 m; but it is increased by 200% when the waves
250 further propagate from the depth of 10 m to the ground surface. This result highlights
251 the importance of varying water table in vertical site amplification, and is in
252 agreement with the observation on the downhole array records in the Kobe
253 earthquake (Yang and Sato, 2000).

254 For ease of reference, Table 3 summarizes the peak values of vertical surface
255 accelerations under different water levels. It is worth noting that the peak vertical
256 acceleration at WL=10 m is about 2.6 times that at WL=0 m. The peak acceleration
257 ratio (V/H) accordingly increases from 0.37 in the case of WL=0 m to 0.96 at WL=10 m.

258

259 **INFLUENCE OF DAMPING RATIO**

260 The damping property of soils associated with shear wave propagation has been
261 studied extensively (e.g., Sun *et al.*, 1988; Vucetic and Dobry, 1991; Ishihara, 1996).
262 Current knowledge of soil damping with respect to the propagation of compressional
263 waves is however very limited, although several attempts have been made to discuss
264 the combined loading effect (e.g., Zhang and Aggour, 2004). In the previous case
265 studies, the damping ratio for vertical motion (ζ_v) was assumed to be identical with
266 the damping ratio for horizontal motion (ζ_h), which was derived from the horizontal

267 site response analysis through iterations. It is necessary to examine the potential
268 effect of damping ratio, ζ_v , on the vertical site response. For this purpose, two more
269 cases of vertical damping, $\zeta_v = 0.5\zeta_h$ and $\zeta_v = 2\zeta_h$, are assumed for the reference soil
270 profile given in Fig. 2.

271 The surface response spectra of vertical motion under three damping ratios
272 are presented in Fig. 20(a). The transfer functions for vertical motion under the three
273 damping ratios are presented in Fig. 20(b). As expected, an increase in damping ratio
274 (ζ_v) results in a greater reduction in vertical amplification. In the case of low
275 damping ratio, i.e. $\zeta_v = 0.5\zeta_h$, the vertical amplification at the fundamental frequency
276 is as large as 37; but it is reduced to be less than 10 when $\zeta_v = 2\zeta_h$. On the other hand,
277 the influence of vertical damping ratio on the surface response spectra appears to be
278 minor for the entire range of periods. Accordingly, the surface response spectral ratio
279 (V/H) is not significantly affected by the variation of vertical damping (Fig. 21).

280 The influence of damping ratio on peak vertical acceleration and velocity at
281 ground surface is summarized in Table 4. It is noted that when the damping ratio is
282 decreased from $2\zeta_h$ to $0.5\zeta_h$, the peak acceleration ratio (V/H) is increased by 10%,
283 from 0.48 to 0.54.

284

285 **IMPLICATIONS FOR PRACTICE**

286 The results presented in the preceding sections indicate that the current practice to
287 produce vertical response spectra for seismic design is not adequate as the response
288 spectral ratio (V/H) is influenced by a number of geotechnical factors, in addition to

289 source mechanism and site-to-source distance. In particular, the behavior of vertical
290 motion can be significantly affected by the variation of water table or the associated
291 variation in compressional wave velocity, which may occur in certain circumstances
292 such as change of seasons. It is thus necessary to examine the water table conditions
293 in interpreting vertical earthquake motion recordings. A good example can be
294 referred to the study of Yang and Sato (2000).

295 The results presented here also have useful implications for the applications of
296 the site-evaluation technique known as (H/V), which is based on the interpretation of
297 recordings of microtremors or weak ground motions in both horizontal and vertical
298 components and has drawn an increasing interest in practice (e.g., Mucciarelli *et al.*,
299 2003),

300 Since there is possibility that vertical motion at the ground surface can become
301 comparable to or even larger than its horizontal counterpart in magnitude, it is
302 necessary to take into account a wider range of magnitudes of vertical motion in
303 seismic analysis and design of engineering structures. Several recent studies have
304 shown that the effect of vertical motion should not be simply disregarded (Ling and
305 Leshchinsky, 1998; Mylonakis and Gazetas, 2002; Yang, 2007).

306 Owing to the simplifications introduced in the present modeling procedure,
307 the effects on ground motions due to very strong nonlinear soil response, in
308 particular that associated with soil liquefaction (e.g., Yang *et al.*, 2000), may not be
309 well accounted for. In these situations more sophisticated procedures such as fully-
310 coupled, elasto-plastic, 2D or 3D finite element programs can be sought to investigate

311 the ground motion characteristics. However, it is to be recognized that these analyses
312 usually involve with great difficulty and uncertainty in determination of the
313 parameters of constitutive models for soils, rendering them unsuitable for routine
314 engineering practice.

315

316 **CONCLUSIONS**

317 An attempt has been made in this study, by using a simple analytical procedure
318 developed by Yang and Yan (2009), to investigate potential factors that may influence
319 ground response to vertical and horizontal earthquake loading. Particular attention
320 has been paid to the behavior of vertical ground motion and its relation with the
321 horizontal counterpart, on which current understanding is very limited. The main
322 results of the present study can be summarized as follows.

323 (a) Site frequencies for both vertical and horizontal motions decrease with
324 increasing the intensity of input motion, accompanied by a significant reduction
325 of site amplification at these frequencies. This is due primarily to high hysteretic
326 damping and reduced moduli associated with strong earthquake motion.

327 (b) While the intensity of input motion has a profound influence on the
328 characteristics of individual components of ground motions, its impact is
329 however less significant on the response spectral ratio between the vertical and
330 horizontal motions (V/H) at the surface.

331 (c) The amplification factor, simply defined as the ratio between peak accelerations
332 at the surface and at the base of soil deposit, is not an appropriate indicator for
333 soil nonlinearity involved with vertical ground motion.

334 (d) Compared with the case of rock outcropping input, the response of the site to
335 the same earthquake motion specified at the bedrock is stronger in both vertical
336 and horizontal directions. Vertical ground response appears to be affected more
337 significantly by the location of input motion than the horizontal one.

338 (e) The variation of water table can bring about a significant impact on vertical
339 ground response. When the water table is lowered, site frequencies for vertical
340 motion will be shifted to the low frequency end and the surface response spectra
341 will exhibit higher peak values.

342 (f) The surface response spectral ratio (V/H) increases substantially at low periods
343 with lowering the water table, but is not affected significantly at long periods
344 (greater than 0.6 s). The peak value of the spectral ratio (V/H) tends to largely
345 exceed the rule-of-thumb value 2/3 when the water table is lowered.

346 (g) The vertical amplification at site frequencies decreases with increasing the
347 damping ratio for vertical motion, but the influence of damping ratio appears to
348 be minor on the response spectra of vertical surface motion and on the response
349 spectral ratio (V/H) at the surface.

350

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355

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396

397 **List of Figures**

- 398 Figure 1. Schematic illustration of the common procedure for generating vertical design
399 spectra from the horizontal design spectra
400
401 Figure 2. A hypothesized site for analysis
402
403 Figure 3. Input motions used: (a) time histories; (b) response spectra
404
405 Figure 4. Transfer functions (surface-to-base) under various levels of motion intensity: (a)
406 horizontal component; (b) vertical component
407
408 Figure 5. Response spectra of ground surface motions under various levels of motion
409 intensity: (a) horizontal component; (b) vertical component
410
411 Figure 6. Influence of the intensity of input motion on the response spectral ratio between
412 vertical and horizontal surface motions (V/H)
413
414 Figure 7. Influence of the intensity of input motion on distributions of peak accelerations
415 with depth: (a) horizontal component; (b) vertical component
416
417 Figure 8. Influence of the intensity of input motion on distributions of stresses and strains
418 with depth: (a) peak shear stress; (b) peak shear strain; (c) peak normal stress; (d) peak
419 normal strain
420
421 Figure 9. Influence of the intensity of input motion on distributions of degraded moduli
422 and damping with depth: (a) shear modulus; (b) constrained modulus; (c) damping ratio
423
424 Figure 10. Influence of input motion position on the response spectra of ground surface
425 motions: (a) horizontal component; (b) vertical component
426
427 Figure 11. Influence of input motion position on distributions of peak accelerations with
428 depth: (a) horizontal component; (b) vertical component
429
430 Figure 12. Influence of input motion position on distributions of stresses and strains with
431 depth: (a) peak shear stress; (b) peak shear strain; (c) peak normal stress; (d) peak normal
432 strain
433
434 Figure 13. Influence of input motion position on distributions of (a) shear modulus
435 reduction and (b) damping ratio
436
437 Figure 14. Influence of input motion position on the response spectral ratio between
438 vertical and horizontal surface motions (V/H)
439
440 Figure 15. Three cases of water levels under investigation: (a) WL=0 m; (b) WL=5 m; (c)
441 WL=10 m

442
443 Figure 16. Vertical ground surface accelerations under various water levels: (a) WL=0 m;
444 (b) WL=5 m; (c) WL=10 m
445
446 Figure 17. Influence of water level on vertical ground motion: (a) surface response spectra;
447 (b) transfer function (surface-to-base)
448
449 Figure 18. Influence of water level on the response spectral ratio between vertical and
450 horizontal surface motions (V/H)
451
452 Figure 19. Influence of water level on distributions of (a) peak vertical acceleration and (b)
453 peak vertical velocity
454
455 Figure 20. Influence of damping ratio on vertical ground motion: (a) surface response
456 spectra; (b) transfer function (surface-to-base)
457
458 Figure 21. Influence of damping ratio on the response spectral ratio between vertical and
459 horizontal surface motions (V/H)
460

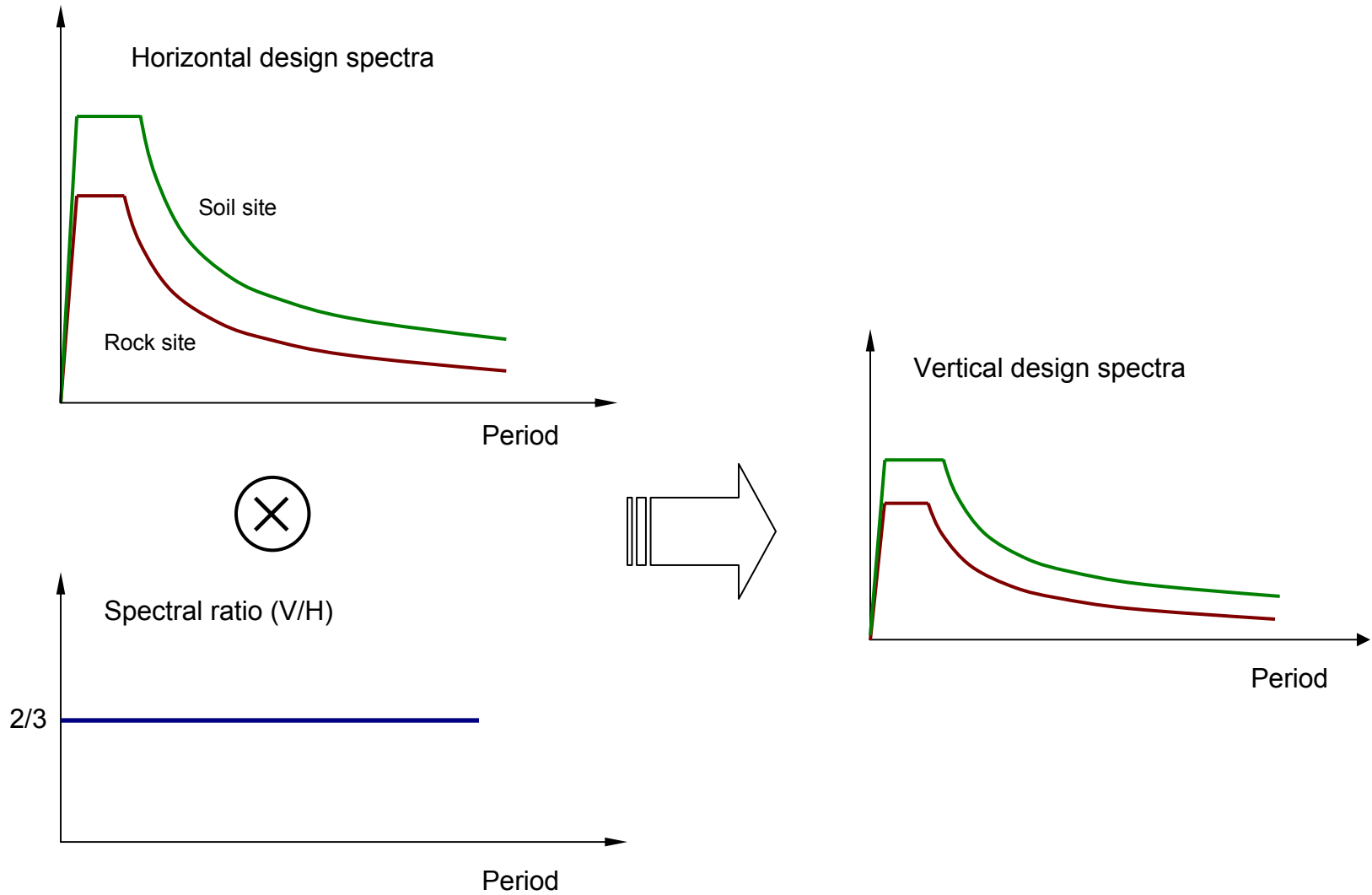


Figure 1. Schematic illustration of the common procedure for generating vertical design spectra from the horizontal design spectra

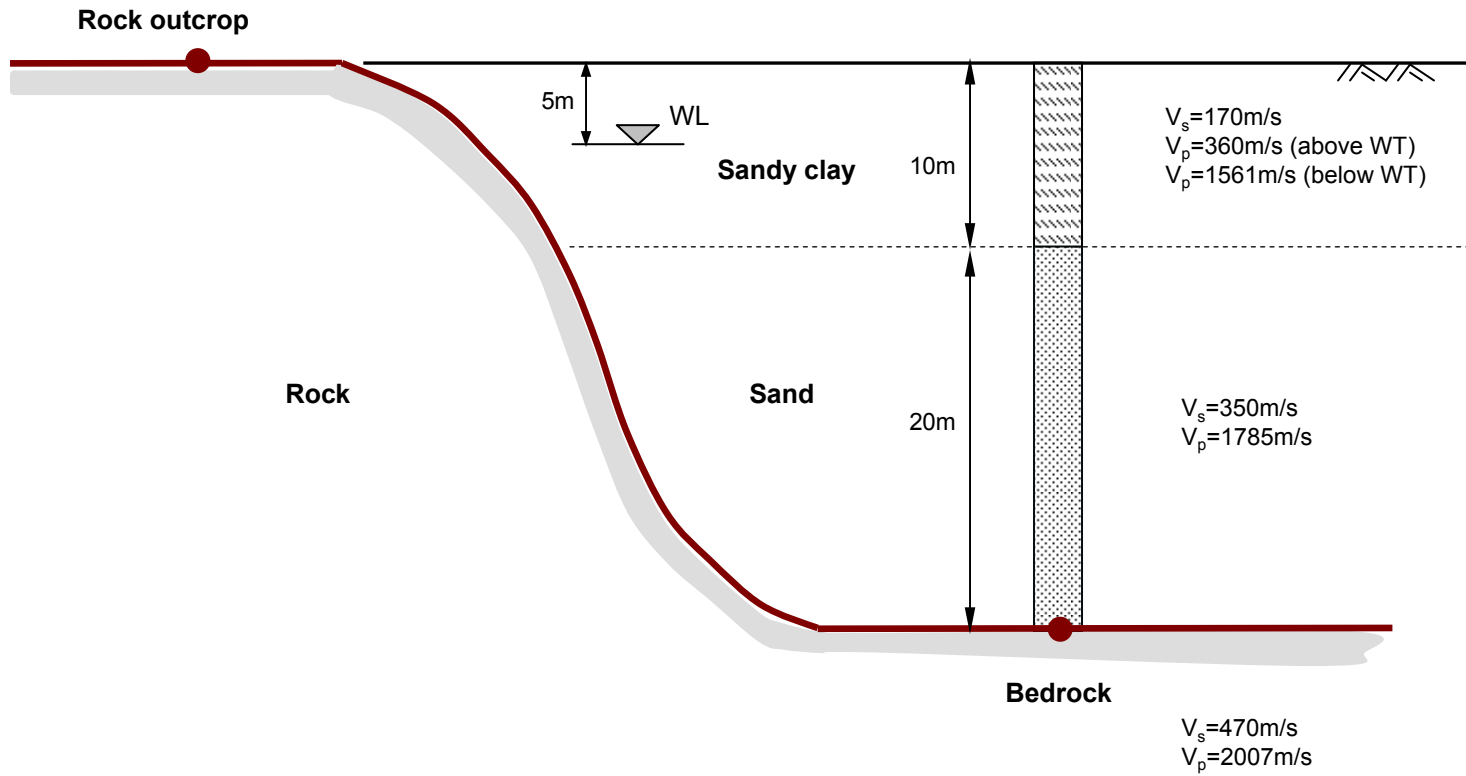
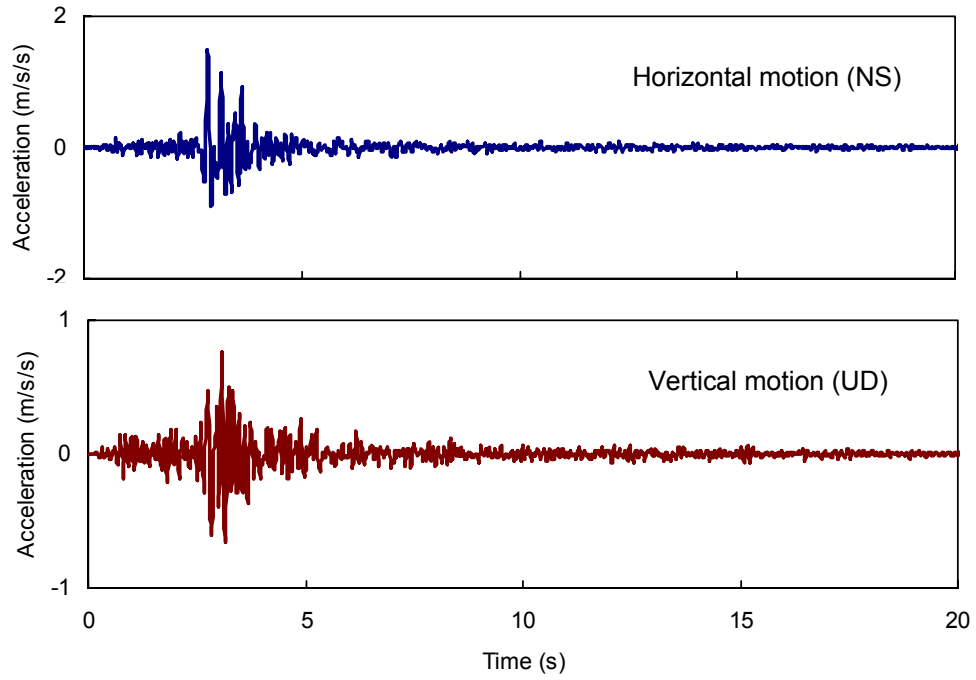
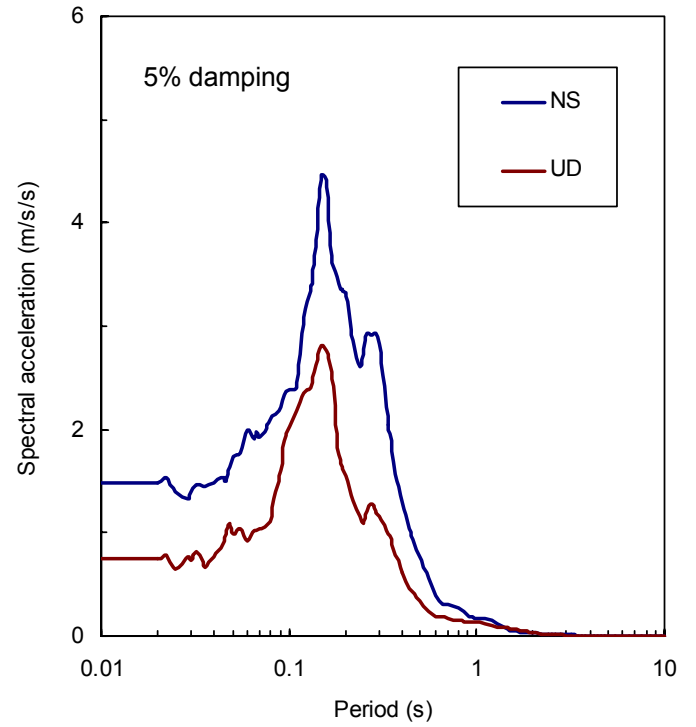


Figure 2. A hypothesized site for analysis

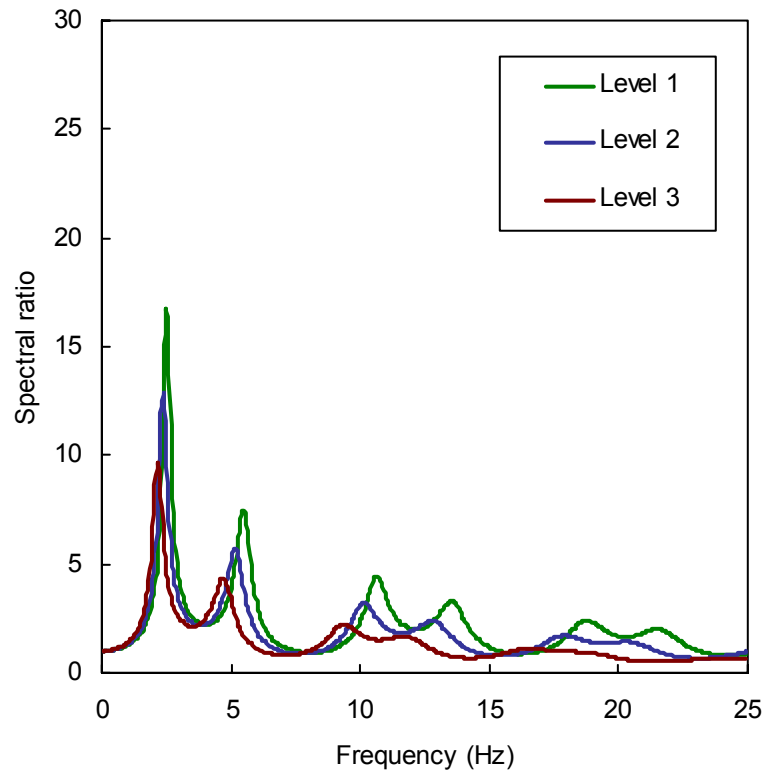


(a)

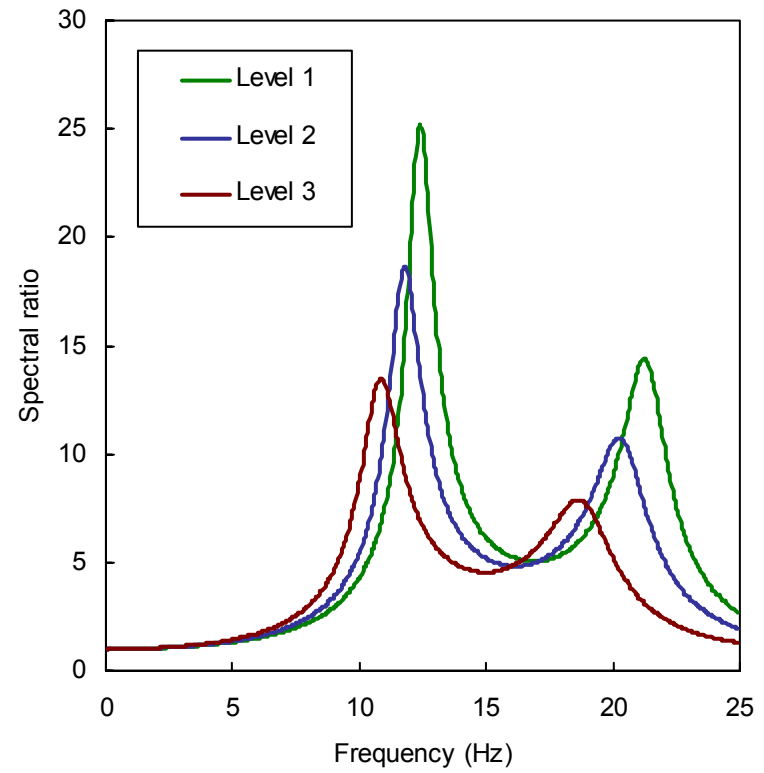


(b)

Figure 3. Input motions used: (a) time histories; (b) response spectra

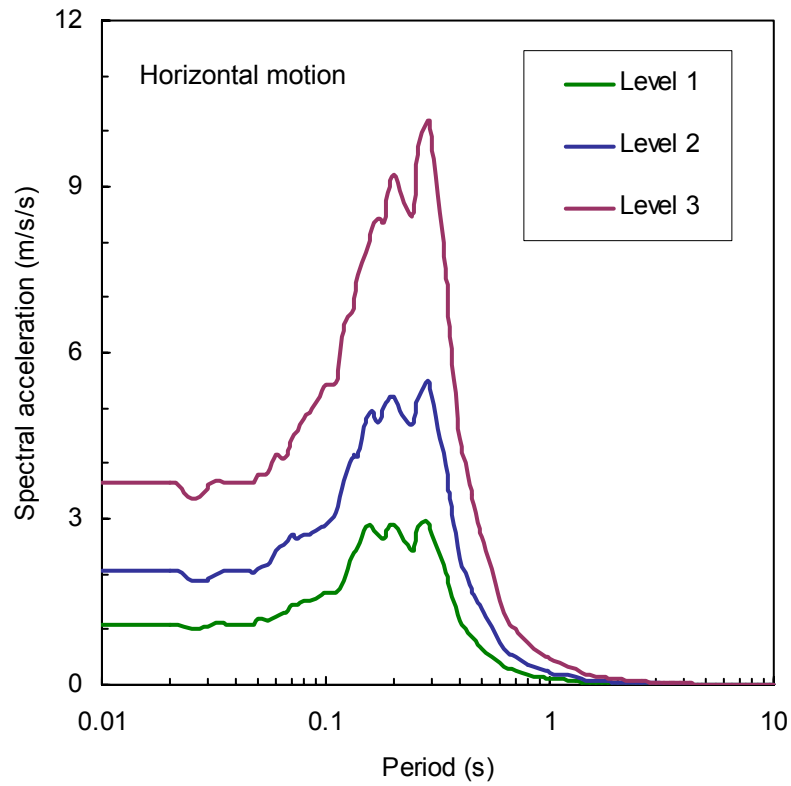


(a)

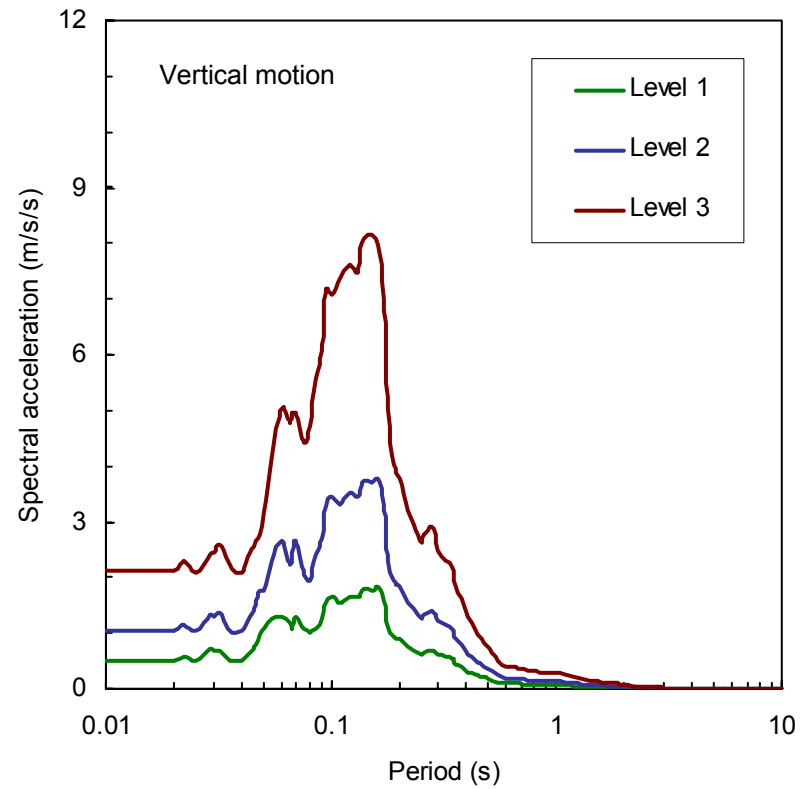


(b)

**Figure 4. Transfer functions (surface-to-base) under various levels of motion intensity:
 (a) horizontal component; (b) vertical component**



(a)



(b)

**Figure 5. Response spectra of ground surface motions under various levels of motion intensity:
(a) horizontal component; (b) vertical component**

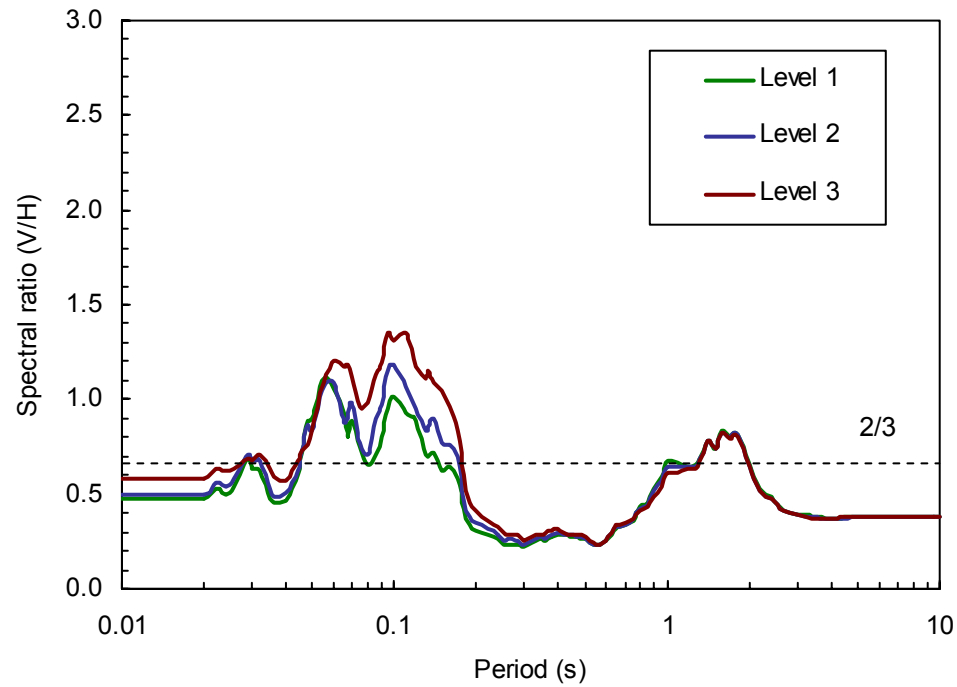
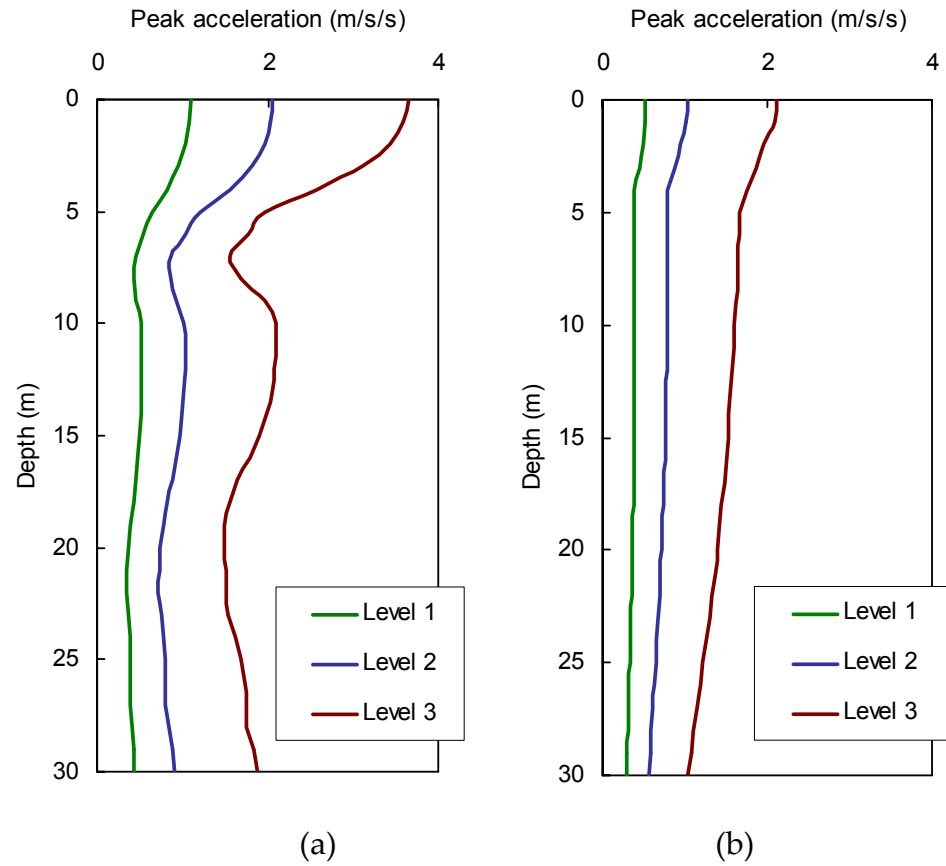


Figure 6. Influence of the intensity of input motion on the response spectral ratio between vertical and horizontal surface motions (V/H)



**Figure 7. Influence of the intensity of input motion on distributions of peak accelerations with depth:
(a) horizontal component; (b) vertical component**

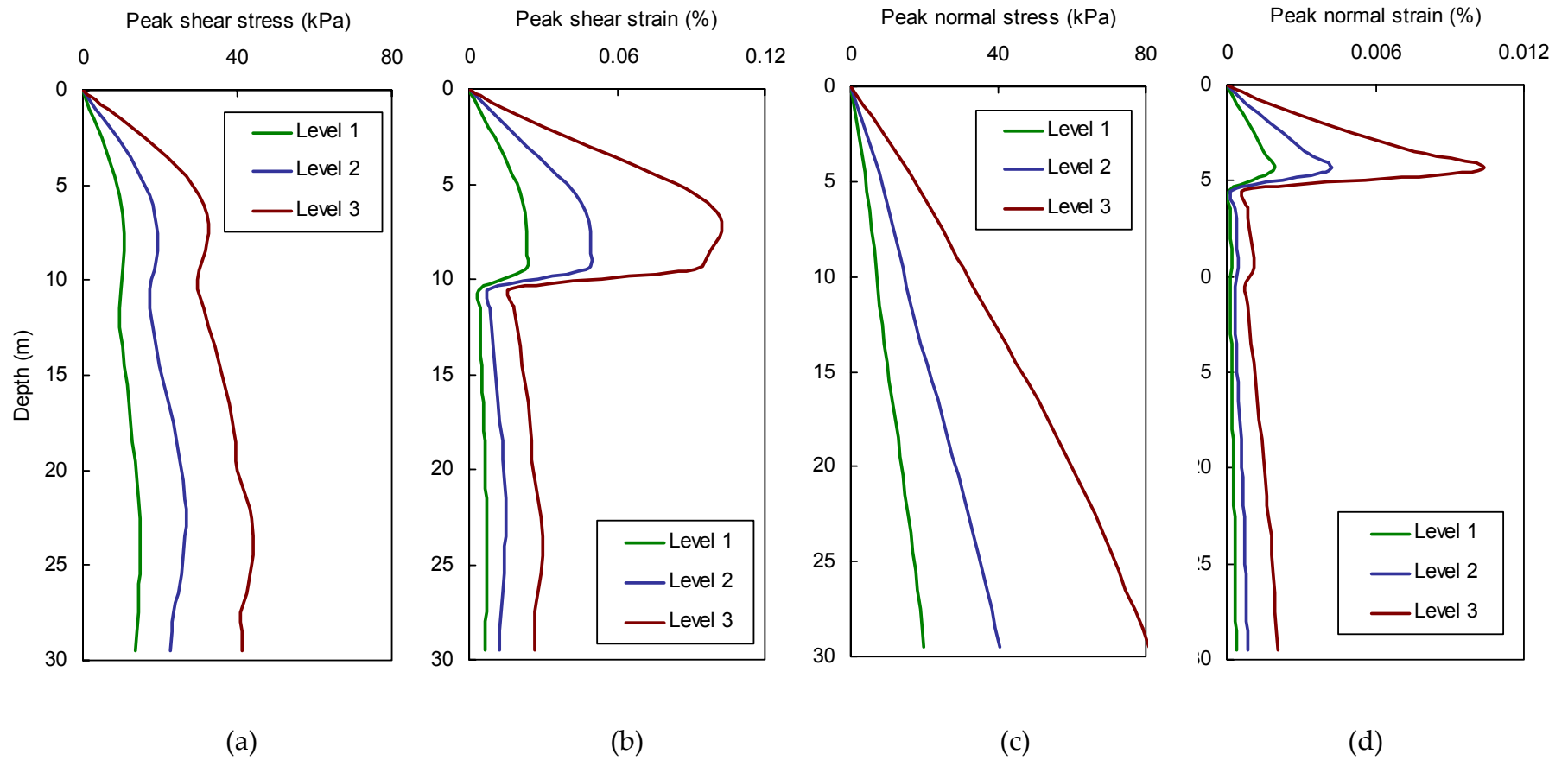


Figure 8. Influence of the intensity of input motion on distributions of stresses and strains with depth: (a) peak shear stress; (b) peak shear strain; (c) peak normal stress; (d) peak normal strain

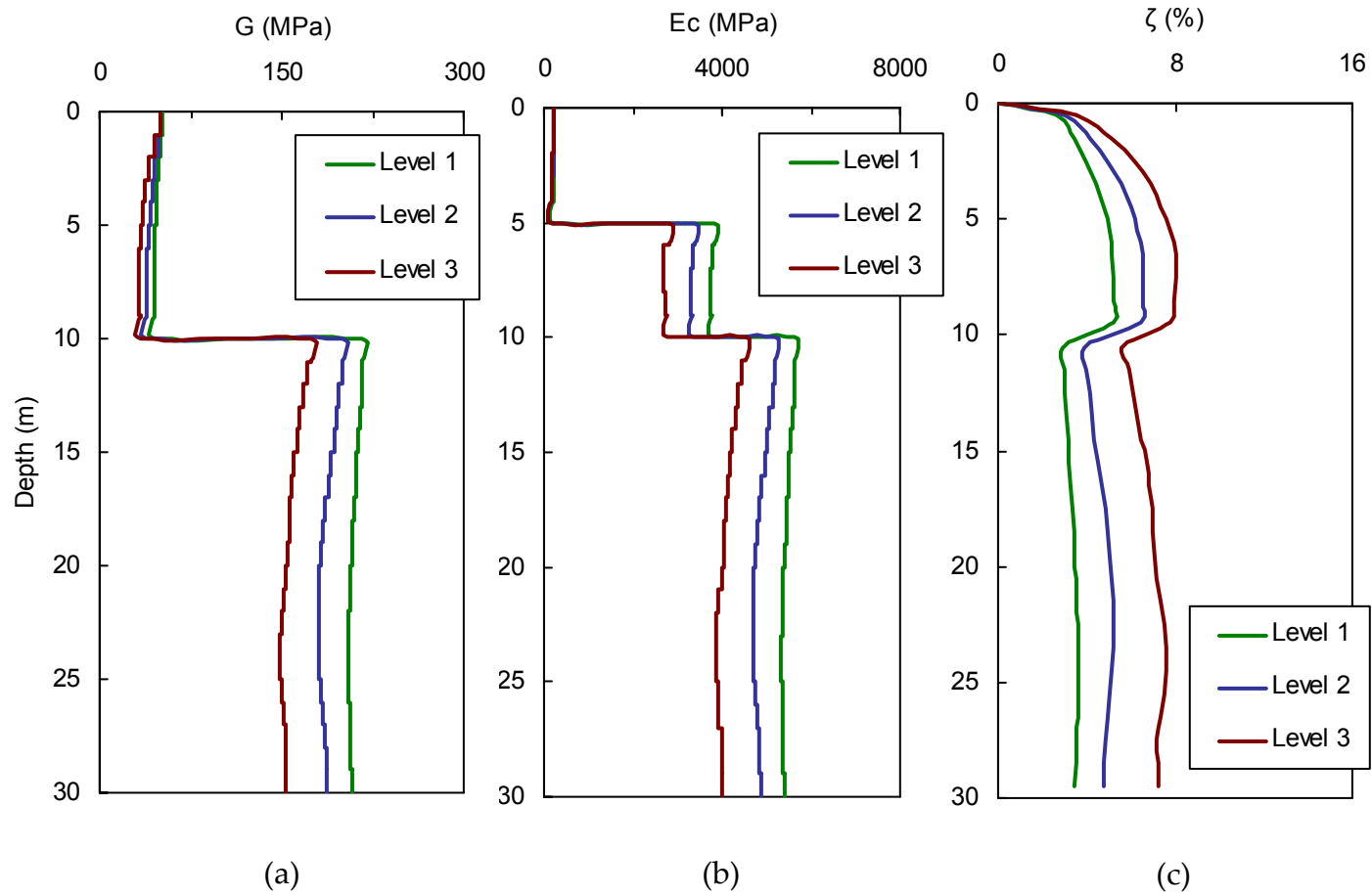
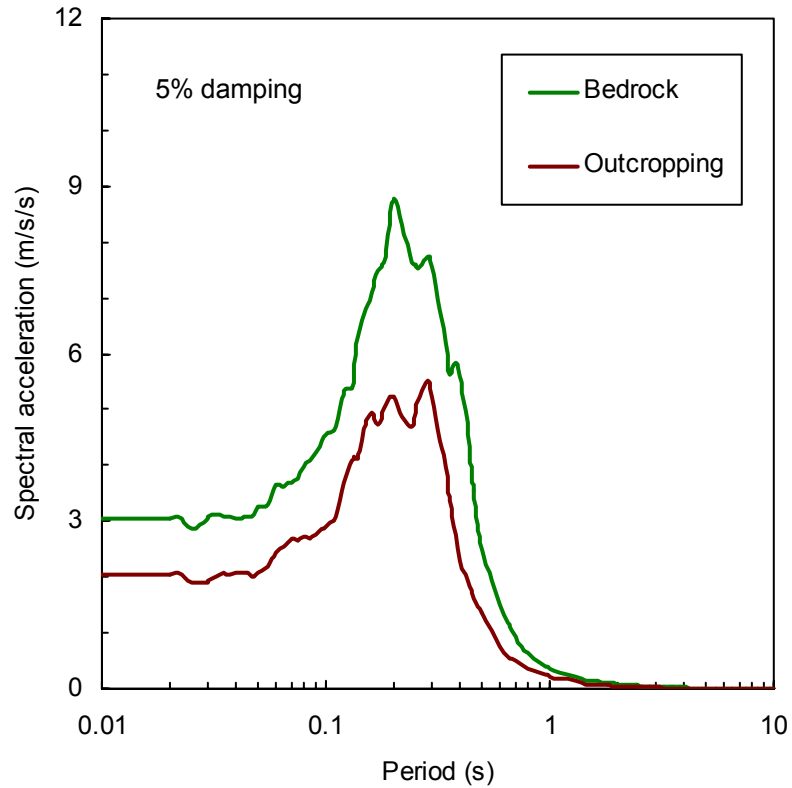
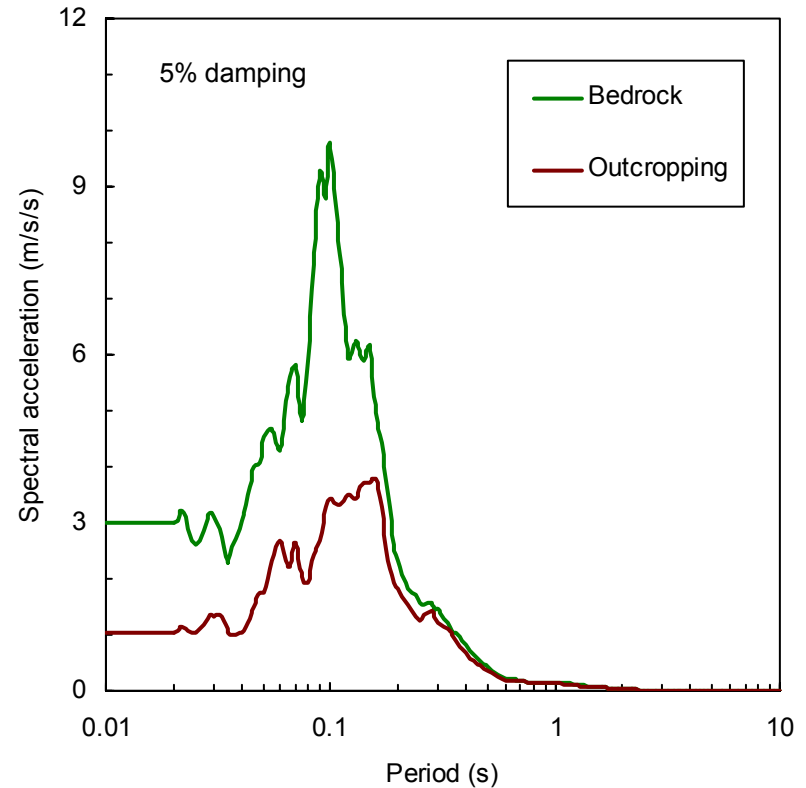


Figure 9. Influence of the intensity of input motion on distributions of degraded moduli and damping with depth: (a) shear modulus; (b) constrained modulus; (c) damping ratio



(a)



(b)

**Figure 10. Influence of input motion position on the response spectra of ground surface motions:
(a) horizontal component; (b) vertical component**

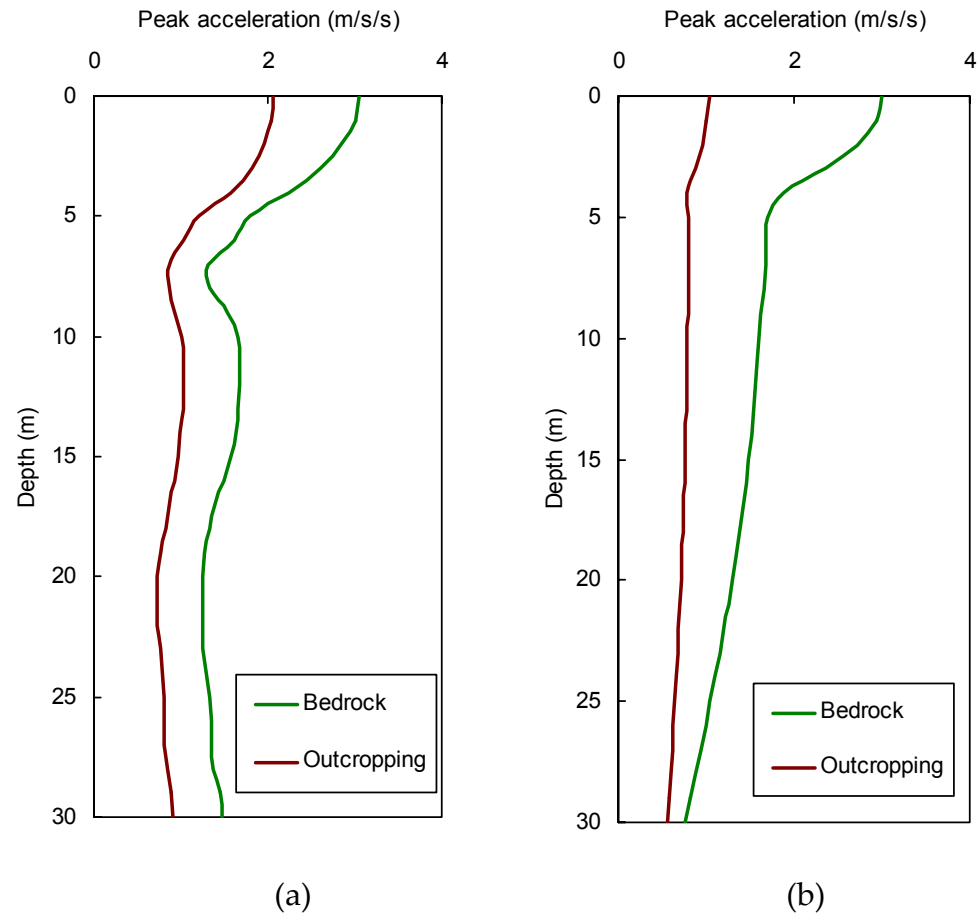


Figure 11. Influence of input motion position on distributions of peak accelerations with depth: (a) horizontal component; (b) vertical component

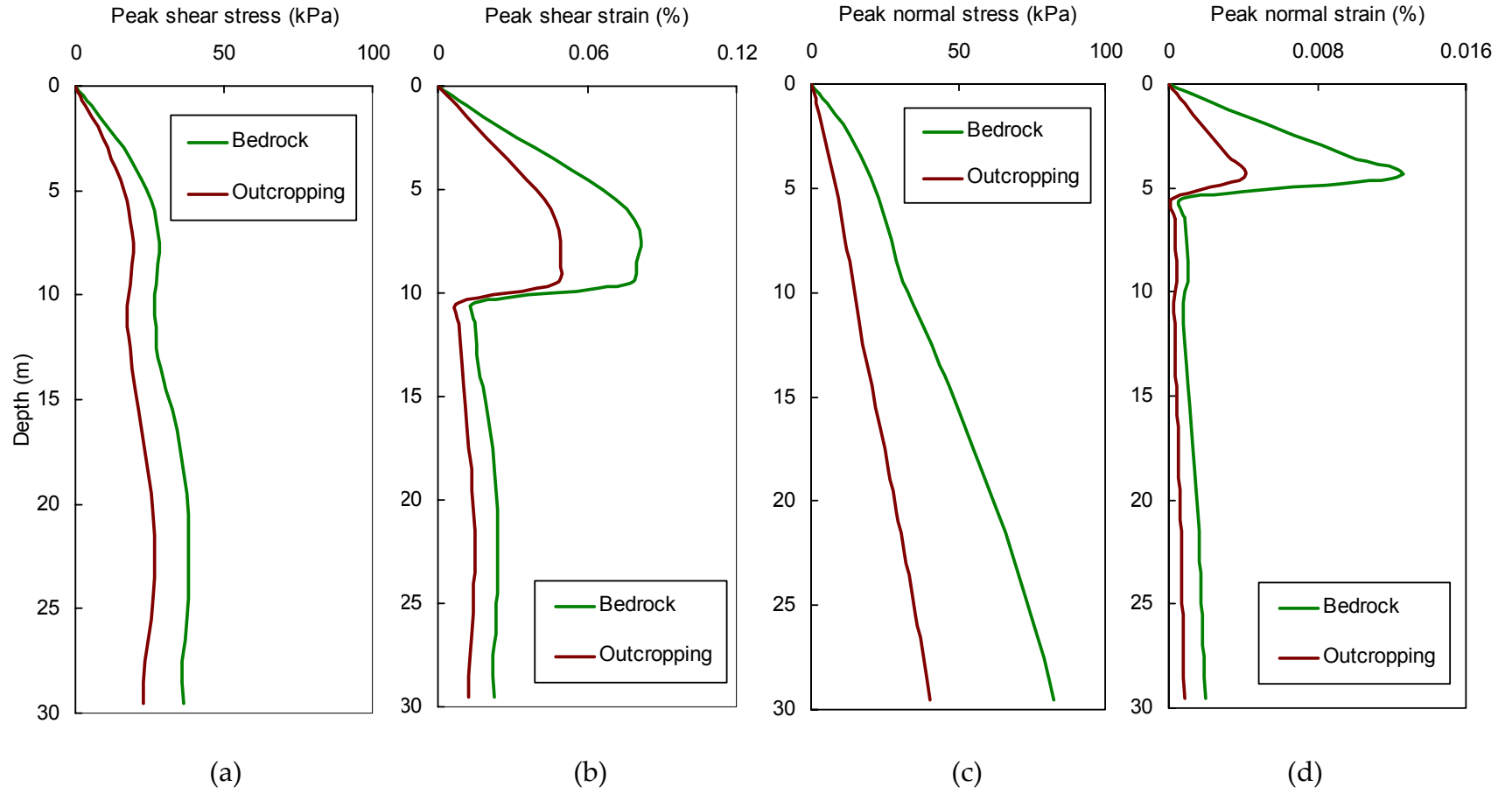


Figure 12. Influence of input motion position on distributions of stresses and strains with depth:
(a) peak shear stress; (b) peak shear strain; (c) peak normal stress; (d) peak normal strain

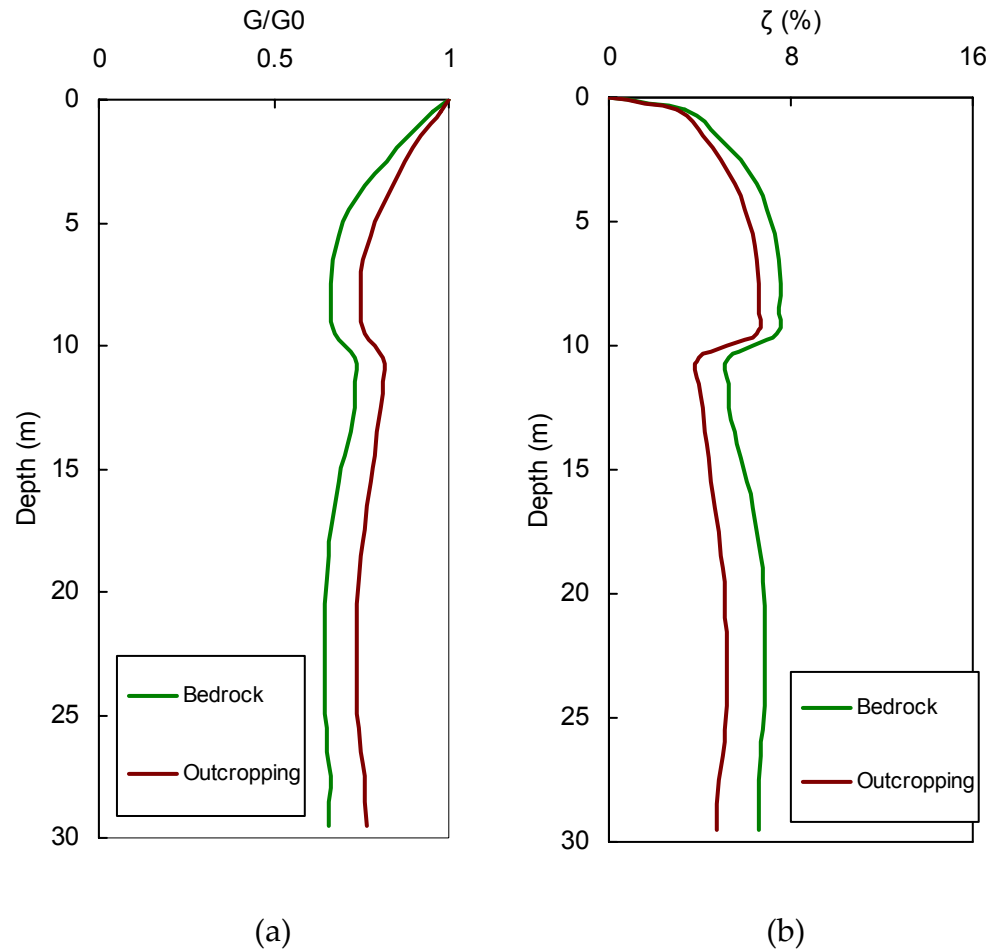


Figure 13. Influence of input motion position on distributions of (a) shear modulus reduction and (b) damping ratio

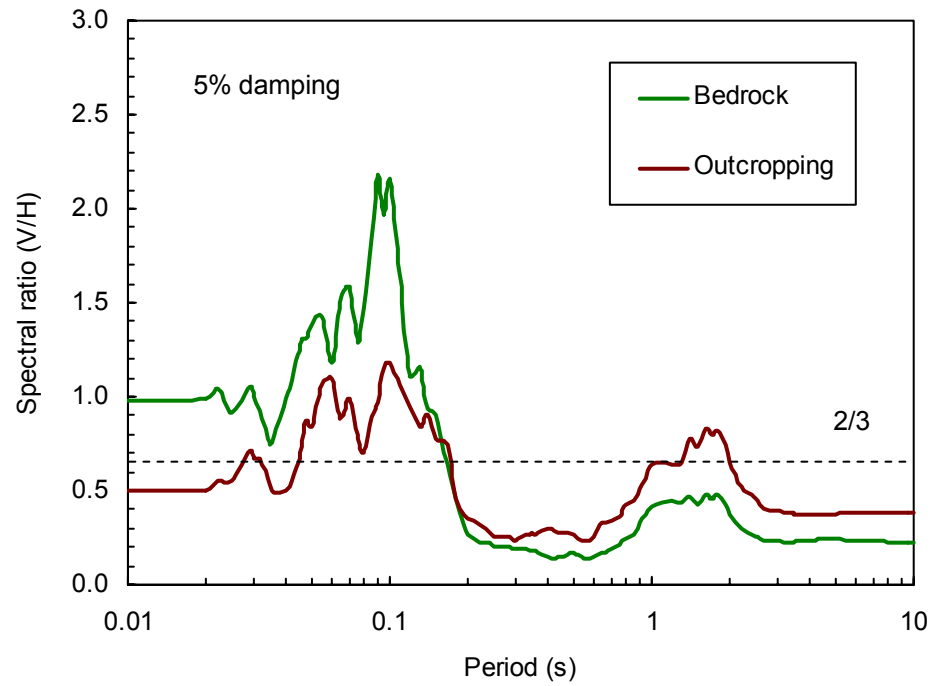


Figure 14. Influence of input motion position on the response spectral ratio between vertical and horizontal surface motions (V/H)

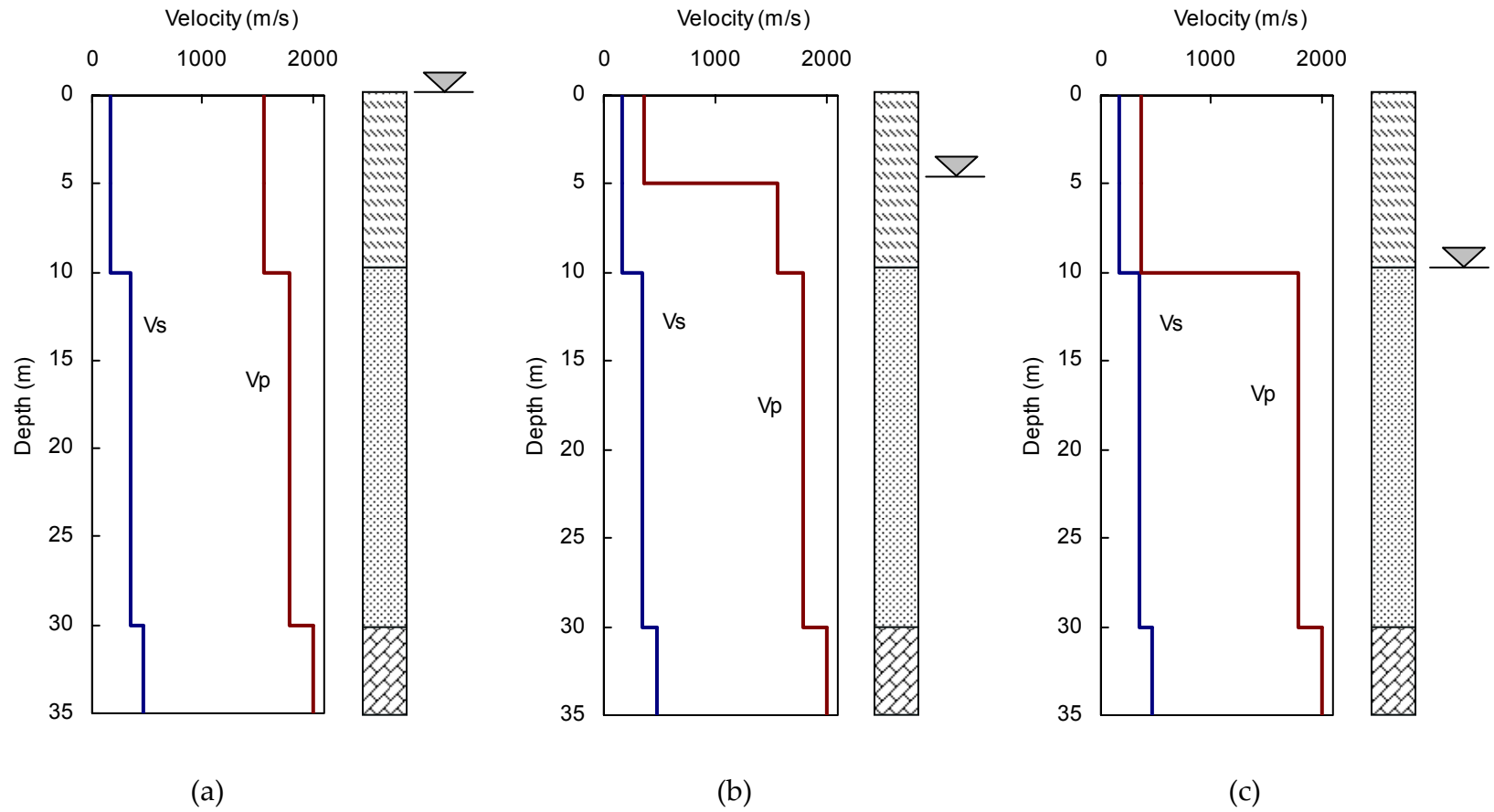


Figure 15. Three cases of water levels under investigation: (a) WL=0 m; (b) WL=5 m; (c) WL=10 m

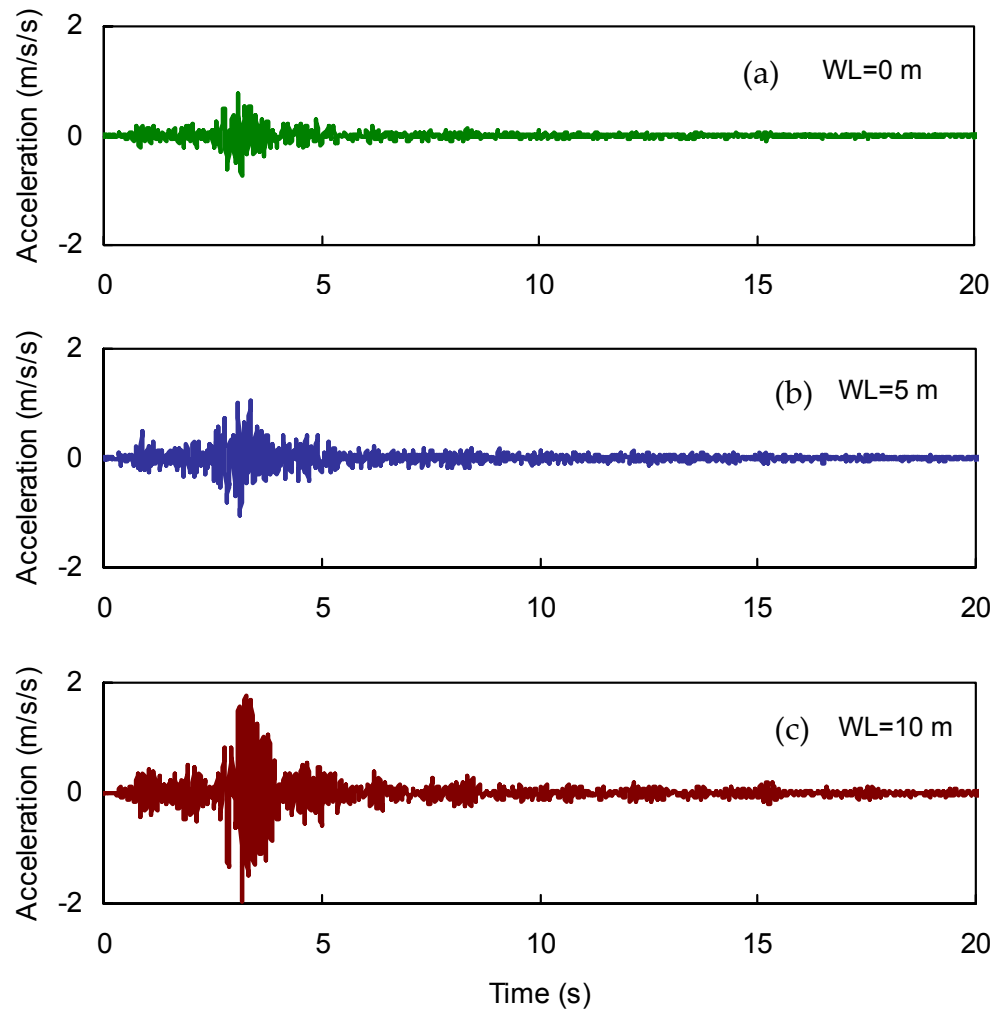
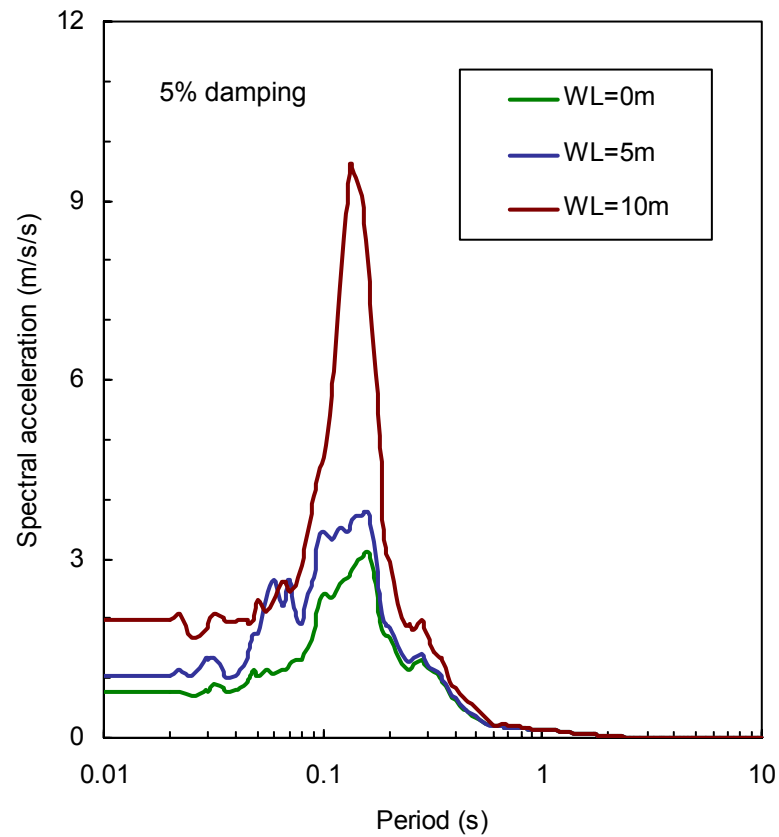
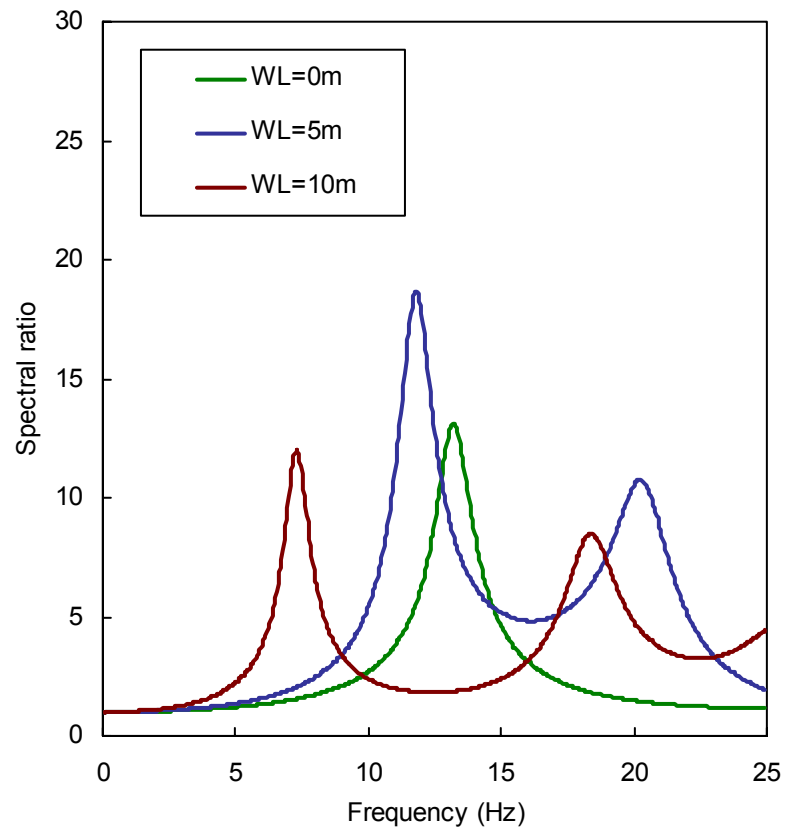


Figure 16. Vertical ground surface accelerations under various water levels: (a) WL=0 m; (b) WL=5 m; (c) WL=10 m



(a)



(b)

Figure 17. Influence of water level on vertical ground motion: (a) surface response spectra; (b) transfer function (surface-to-base)

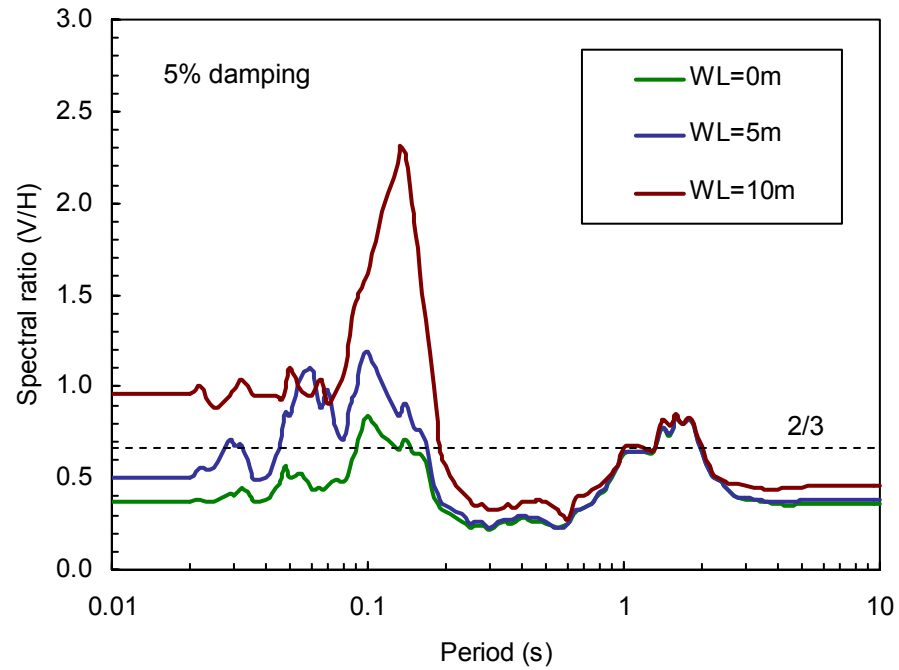


Figure 18. Influence of water level on the response spectral ratio between vertical and horizontal surface motions (V/H)

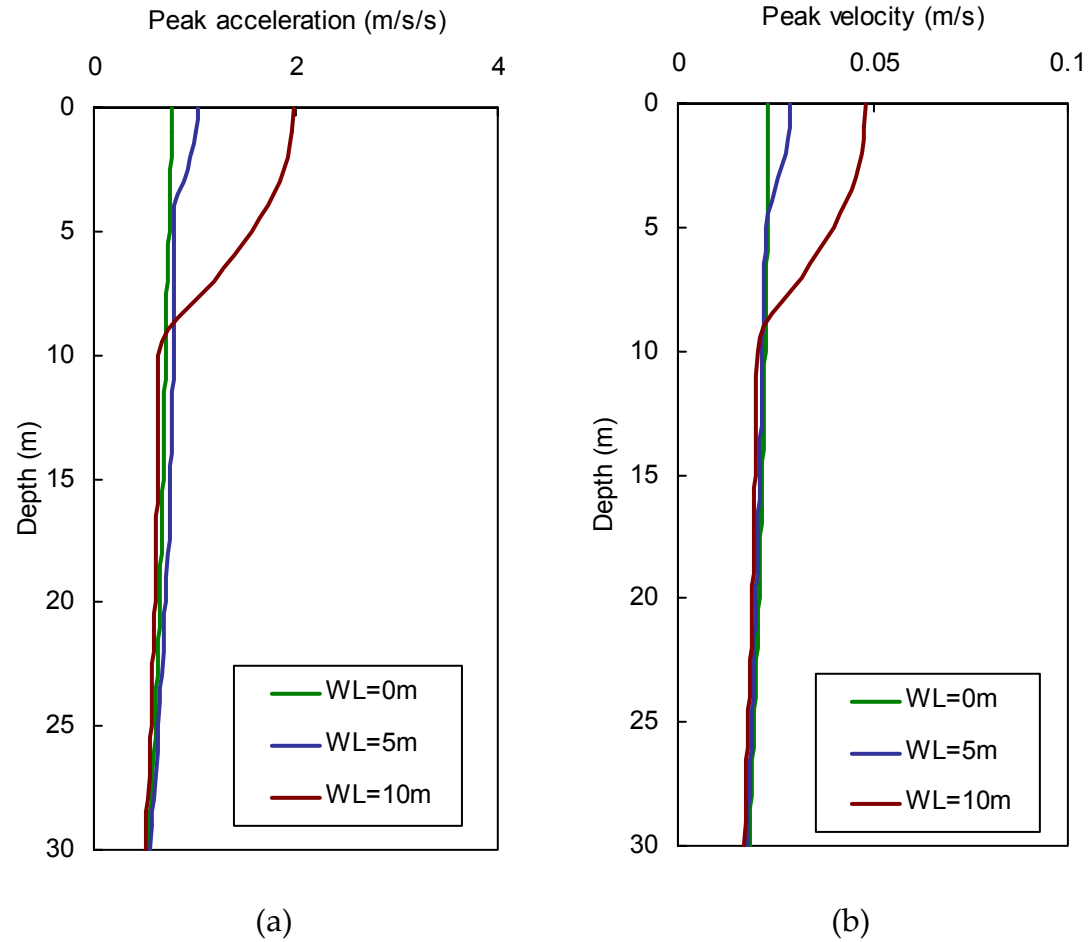
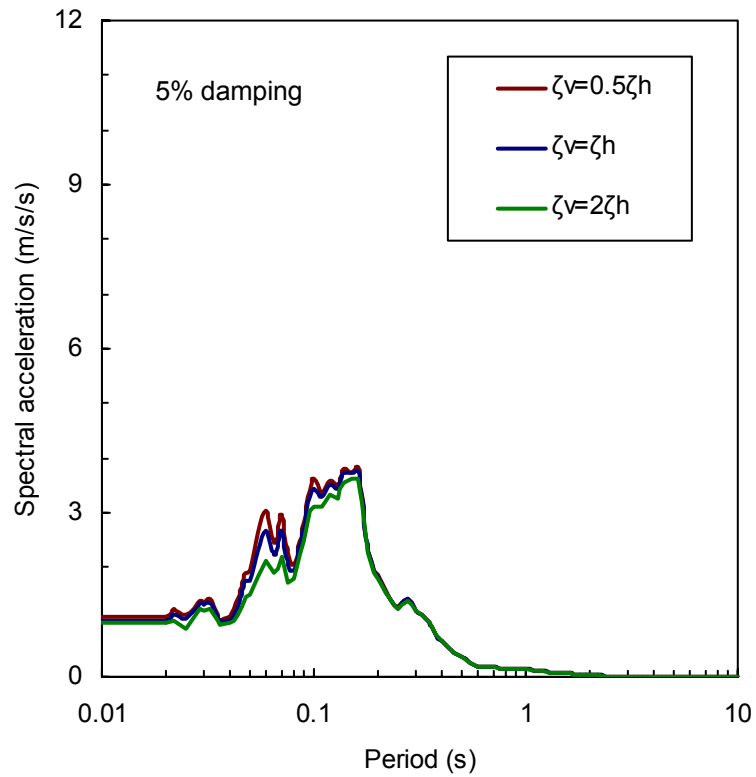
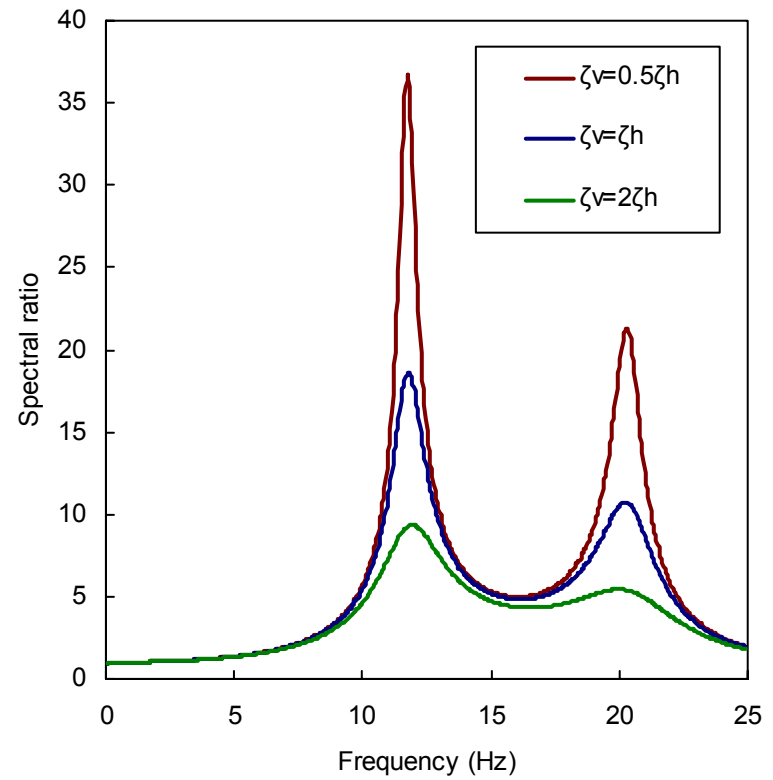


Figure 19. Influence of water level on distributions of (a) peak vertical acceleration and (b) peak vertical velocity



(a)



(b)

Figure 20. Influence of damping ratio on vertical ground motion: (a) surface response spectra; (b) transfer function (surface-to-base)

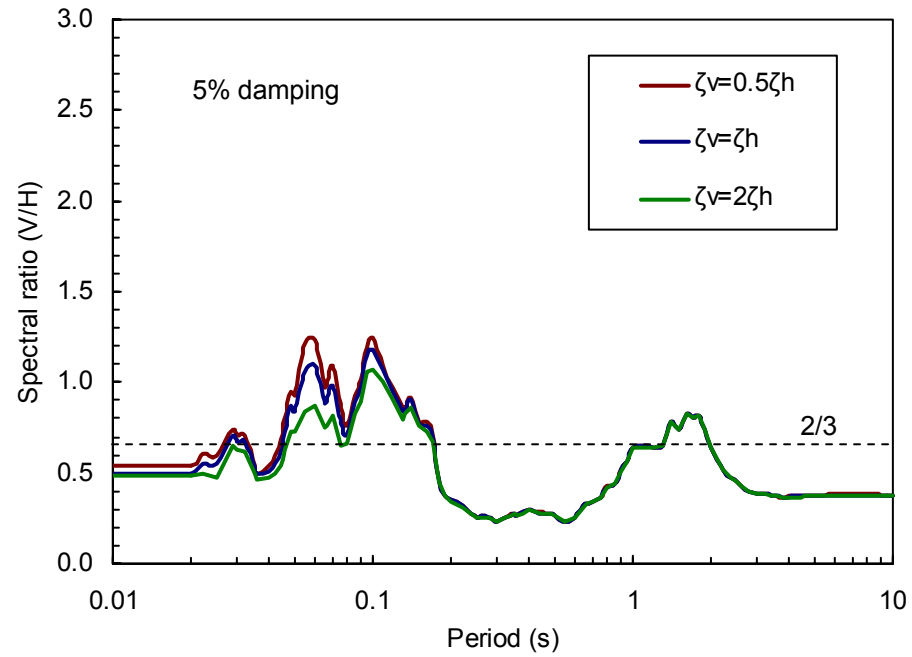


Figure 21. Influence of damping ratio on the response spectral ratio between vertical and horizontal surface motions (V/H)