

# BGP Ingress-to-Egress Route Configuration in a Capacity-constrained AS

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**Abstract** — The BGP ingress-to-egress route configuration problem is to find a set of paths in an ISP to carry the transit flows, such that the amount of network resources consumed is minimized without violating the bandwidth constraint on all network links. To solve the problem, we first formulate it using Integer Linear Programming (ILP). Due to the high complexity involved in ILP, a heuristic algorithm, called MPPF, is then proposed. MPPF is designed based on the idea that heavily-loaded destination prefixes should be given higher priority to select less expensive edge links and routes. Simulation results show that MPPF requires less network resources and edge link capacity than an alternative heuristic called BTF.

**Keywords** — BGP, Border Router Advertisements, Most Popular Prefix First

## I. INTRODUCTION

A major responsibility of an Internet Service Provider (ISP) is to provide transit service for its neighbors. Traffic goes into and out of an ISP through a set of border routers which are managed by the ISP and are connected to its neighbors via a set of peering edge links. The problem of BGP ingress-to-egress route configuration is to determine a set of ingress-to-egress paths within the ISP's network to carry the transit traffic such that the network resources consumed is minimized.

To fully understand the mechanisms available for configuring ingress-to-egress routes, knowledge of Border Gateway Protocol (BGP) [1] is essential. In short, BGP is a path vector protocol under which routing decisions can be made based on policy. BGP divides the Internet into a collection of Autonomous Systems (ASes). An AS is defined as a set of routers under a single technical administration, e.g. an ISP. ASes exchange routing reachability information through external BGP peering sessions. A border BGP router receives route advertisements from either external peers (in neighboring ASes) or internal peers (in local AS). Each advertisement contains a destination prefix, an IP address of the next-hop, a multi-exit discriminator (MED) and a list of ASes leading to the destination prefix. Some or all of these received routes will be included into its own routing table and advertised to its peers based on a set of decision criteria [1].

When an AS propagates an advertisement to an external peer, the MED field can be used to indicate the preference of accepting incoming traffic at a particular ingress edge (thus ingress router) and the smaller the MED value, the higher the preference. So properly setting the MED field can help to balance the network load. In general, no matter where the transit traffic arrives, as long as it has the same destination prefix, it will be sent to the same selected egress link.

Related work on optimizing the performance of an ISP can be found in some recent literatures. In [2] and [3], the problem

of intra-domain path selection is studied and several OSPF weight assignment algorithms are proposed for setting up peer-to-peer intra-domain paths. In [4], a border router and intra-domain link placement problem is examined. The solution is useful at the development phase of an ISP. In [5], the problem of BGP route configuration is investigated under the assumption that an ISP cannot control the ingress points of the transit traffic and all ingress edge links and intra-domain links have unlimited bandwidth. This problem is proved to be NP-hard. Their proposed heuristic algorithm is based on the Integer Linear Programming (ILP) formulation and is quite complicated. In [6], a time-efficient algorithm based on the idea of most popular prefix first is designed.

In this paper, we extend the model for BGP egress selection [5][6] to take advantages of the MED option in BGP. This allows a local AS to recommend certain ingress edge/router to its neighbors for accepting their incoming transit traffic. The resources consumed by the local AS can be further reduced. Since the assumption of infinite capacity on intra-domain links [5][6] may not be realistic, links with finite bandwidth are considered in this paper. A new heuristic algorithm called MPPF is proposed. It is based on the similar idea of [6] that heavily-loaded destination prefixes should be given higher priority to select less expensive ingress and egress edge links and paths. This allows more traffic flows to go through less expensive paths which can potentially minimize the network resources consumed.

In the next section, the route configuration problem is formally defined. In Section III, we show that the problem can be solved using ILP. In Section IV, the heuristic algorithm MPPF is presented and its performance is evaluated in Section V. Finally, we conclude the paper in Section VI.

## II. PROBLEM FORMULATION

Assume that all intra-domain links and edge links connecting to other ASes have finite capacities and are bidirectional. The capacity allocated to each direction is pre-determined and dedicated. Let  $G = (V, E)$  denote the intra-domain topology where  $V = \{1 \dots N\}$  is the set of routers, and  $E$  is the set of intra-domain links. Among  $N$  routers,  $X$  of them are border routers. The set of edge links is given by  $B = \{b_1, \dots, b_i\}$  and  $R(b_i)$  returns the router associated with edge link  $b_i$ .

Multiple edge links may be connected to the same border router. A neighboring AS may be connected to the local AS through a direct edge link, or indirectly via other ASes. Each neighbor may be connected to the local AS through multiple edge links. For simplicity, we assume that the prefixes received by the AS are non-overlapping. We further assume that route advertisements for any prefix are advertised to all

connecting neighbors so that neighbors are able to choose which ingress points to use (based on the MED value in the advertisements).

Given a set of neighbors  $A = \{A_1, \dots, A_H\}$ . For each neighbor  $A_h$ , let  $In(h)$  denote the set of edge links through which  $A_h$  may send in the transit traffic. External BGP peering sessions at the border routers receive advertisements for network prefixes across the edge links. Let  $P = \{P_1, \dots, P_K\}$  denote the set of prefix advertisements received across all edge links. For each prefix  $P_k$ , let  $Out(k)$  denote the set of edge links at which an advertisement for  $P_k$  has been received.

Each edge link  $b_i$  has an ingress capacity constraint  $C_i^{ingress}$  and an egress capacity constraint  $C_i^{egress}$ . The amount of residual bandwidth on ingress and egress links is denoted by  $w_i^{ingress}$  and  $w_i^{egress}$  respectively. Let  $l$  denote a direct link in  $E$  and let  $d_l$ ,  $C_l$  and  $w_l$  denote the cost per unit traffic, capacity constraint and current residual capacity of that link respectively. Also let  $p = [a, b]$  denote a path connecting routers  $a$  and  $b$  in  $V$  and let  $d_p$  denote the cost per unit traffic along  $p$ , i.e.

$$d_p = \sum_{l \in p} d_l \quad (1)$$

### Problem Statement

Let  $t(h, k)$  be the volume of the traffic flow from neighbor  $A_h$  to destination prefix  $P_k$ . Further denote  $f$  as the ingress-to-egress route configuration function. For the flow from  $A_h$  to  $P_k$ ,  $f(h, k)$  returns an ingress edge  $igr(h, k) \in In(h)$ , an egress edge  $egr(h, k) \in Out(k)$ , and a complete intra-domain path from the router associated with  $igr(h, k)$  to the router associated with  $egr(h, k)$ . For convenience, we write  $f(h, k) = \langle igr(h, k), egr(h, k), p(h, k) \rangle$  where  $p(h, k) = [R(igr(h, k)), R(egr(h, k))]$ .

Our goal is to minimize the total amount of network resources consumed for carrying the transit traffic

$$\sum_{h=1}^H \sum_{k=1}^K t(h, k) \cdot d_{p(h, k)} \quad (2)$$

and  $f(h, k) = \langle igr(h, k), egr(h, k), p(h, k) \rangle$  satisfies the following constraints:

- No violation on ingress edge link capacity, i.e.
$$\sum_{h, k: igr(h, k)=l} t(h, k) \leq C_l^{ingress} \quad \forall l \in B;$$
- No violation on egress edge link capacity, i.e.
$$\sum_{h, k: egr(h, k)=l} t(h, k) \leq C_l^{egress} \quad \forall l \in B;$$
- No violation on intra-domain link capacity, i.e.
$$\sum_{h, k: l \in p(h, k)} t(h, k) \leq C_l \quad \forall l;$$
- The same egress edge link is assigned to all transit traffic flows going to the same destination prefix, i.e., for each prefix  $P_k$ ,  $egr(h, k) = l \quad \forall h$  for some  $l$ .

### III. INTEGER LINEAR PROGRAMMING FORMULATION

To facilitate our problem formulation, we introduce a flat network topology  $G' = (V', E')$ . Details of  $G' = (V', E')$  are defined below:

- $V' = V \cup \{(N+h) \mid A_h \in A\} \cup \{(N+H+k) \mid P_k \in P\}$
- $E' = E \cup \{(N+h, R(e)) \mid A_h \in A, e \in In(h)\} \cup \{(R(e), N+H+k) \mid P_k \in P, e \in Out(k)\}$

- $\forall (i, j) \in E'$ 

$$c_{(i, j)} = \begin{cases} C_l, & \forall l \in E \\ C_e^{ingress}, & N+1 \leq i \leq N+H, e \in In(i-N), j = R(e) \\ C_e^{egress}, & e \in Out(j-N-H), i = R(e), N+H+1 \leq j \leq N+H+K \end{cases}$$
- $\forall (i, j) \in E'$ 

$$d_{(i, j)} = \begin{cases} d_l, & \forall l \in E \\ 0, & \text{otherwise} \end{cases}$$

That is, nodes 1 to  $N$  represent the set of routers in the local AS, nodes  $N+1$  to  $N+H$  represent the set of neighboring ASes ( $A_1$  to  $A_H$ ), nodes  $N+H+1$  to  $N+H+K$  represent the set of destination prefix networks (networks having prefixes  $P_1$  to  $P_K$ ). Note that the cost for the ingress and egress edge links are all set to zero so that they will not affect our intra-AS cost calculations. Let  $X_{ij}^{hk}$  represent the percentage of the traffic from neighbor  $A_h$  to destination prefix  $P_k$  that flows across link  $(i, j)$  in  $E'$ . The ILP formulation for the ingress-to-egress route configuration problem is given below.

### ILP Formulation

$$\min \left( \sum_{h=1}^H \sum_{k=1}^K \sum_{(i, j) \in E'} t(h, k) \cdot d_{(i, j)} \cdot X_{ij}^{hk} \right) \quad (3)$$

s.t.

$$\sum_{j:(i, j) \in E'} X_{ij}^{hk} - \sum_{j:(j, i) \in E'} X_{ji}^{hk} = 0, A_h \in A, P_k \in P, i \neq N+h \text{ and } i \neq N+H+k \quad (4)$$

$$\sum_{j:(i, j) \in E'} X_{ij}^{hk} - \sum_{j:(j, i) \in E'} X_{ji}^{hk} = 1, A_h \in A, P_k \in P, i = N+h \quad (5)$$

$$X_{ij}^{hk} = 0 \text{ or } 1, \forall (i, j) \in E' \quad (6)$$

$$\sum_{h=1}^H \sum_{k=1}^K t(h, k) \cdot X_{ij}^{hk} \leq c_{(i, j)} \quad (7)$$

$$X_{i(N+H+k)}^{hk} = X_{i(N+H+k)}^{h_2k}, A_{h_1}, A_{h_2} \in A, P_k \in P, i \in [1, N] \quad (8)$$

The objective function (3) is to minimize the resources consumed. (4) and (5) are flow conservation constraints. (4) states that the amount of traffic flowing into a node has to be equal to the amount of traffic flowing out of the node for non-source and destination nodes. (5) states that the net flow out of a source node is 1. (6) restricts the  $X_{ij}^{hk}$  variables to be either 0 or 1. (7) is the link capacity utilization constraint. (8) ensures that the same egress edge link is assigned to all transit traffic flows going to the same prefix. Noted that this constrain also differentiates the formulation from those for the well-known multicommodity unsplittable flow problem [7].

Though the ingress-to-egress route configuration problem can be solved by ILP, the process is too complicated for any realistic sized problems.

## IV. HEURISTIC ALGORITHM – MPPF

### A. MPPF Algorithm

Let  $p_k$  be the total amount of traffic destined to prefix  $P_k$ . Our proposed algorithm aims at giving the prefix with the largest amount of traffic destined to it, i.e.  $\max_k \{p_k\}$ , the highest route selection priority. The idea is that if no priority is given to the prefix with the largest  $p_k$  value, it is very likely that the most desirable egress link leading to this prefix together with the corresponding intra-domain route would have been occupied by others. The potential extra cost of carrying this traffic on alternative egress links together with the corresponding intra-domain route would be very high. Since the route configuration priority is based on  $p_k$ , we call our algorithm Most Popular Prefix First (MPPF).



6 requires a worst case time complexity of  $O(K \log K)$ . Step 8 is the most expensive step and it invokes function  $Cost\_Prefix()$  many times.

Function  $Cost\_Prefix()$  in turn goes through at most  $HK$  traffic flows and for each traffic flow, we have to go through  $I$  ingress edges and for each ingress edge, function  $Shortest\_Path()$ , which is based on Dijkstra's Algorithm, is invoked. Let  $N$  be the number of nodes in the topology, the worst case time complexity of Dijkstra's Algorithm is known to be  $O(N \log N + |E|) \sim O(N \log N)$  since  $|E| \sim N$  in a BGP environment. As a result, the time complexity of function  $Cost\_Prefix()$  is  $O(HKIN \log N)$ .

As Step 8.3 iterates function  $Cost\_Prefix()$   $I$  times, its time complexity is  $O(HK I^2 N \log N)$  and it is the most expensive substep in Step 8. Therefore, the running time of MPPF is  $O(HK^2 I^2 N \log N)$ .

### C. Implementation using MPLS

Current OSPF intra-domain routing protocol is shortest-path based. However, due to capacity constraints on internal links, the paths returned by MPPF may not be the shortest. To allow a flow following a non-shortest path, the technique of OSPF weight assignment [2][3] or the technique of Multi-Protocol Label Switching (MPLS) [8] can be used. Since not all paths can be specified by setting OSPF weights [9], MPLS is preferred. With MPLS, each path found by the MPPF algorithm is specified by a logical *label-switched path*. Upon receiving a transit traffic flow, a border router checks its BGP routing table to determine which egress edge (thus egress border router) should be used. Then it forwards the flow to the selected egress border router using a predetermined label-switched path.

As a final remark, MPPF algorithm has assumed that neighboring ASes will always honor the ingress edge recommendations made by the local AS. In reality, this may not be the case, possibly due to the conflict of interests among neighboring ASes. We will study the impact of such factors in the future.

## V. PERFORMANCE EVALUATIONS

### A. Network Model

Consider a local AS with  $N - X$  internal and  $X$  border routers,  $H$  neighboring ASes and  $K$  destination prefixes for transit flows. The network topology for simulation is generated as follows:

- A topology containing  $N$  nodes with cost per unit traffic on the direct link between any two nodes in the range  $\{1 \dots 10\}$  is generated by BRITE [10];  $X$  nodes are picked up randomly to become border routers. Assume  $d_{(i,j)} = d_{(j,i)}$  for any two routers  $r_i$  and  $r_j$ .
- The multihoming degree of each border router is randomly selected from 1 to 3. Each border router is then associated with the corresponding number of edge links. All edge links are uniquely numbered to form the edge set.
- The size of set  $In(h)$  for each neighbor  $A_h$  is randomly selected from 2 to 3. The elements of  $In(h)$  are randomly selected from the edge set.
- For each prefix  $P_k$ , the size of  $Out(k)$  is randomly selected from 2 to 5. The elements of  $Out(k)$  are again randomly selected from the edge set.

### B. Traffic Model

Assume that every neighboring AS has some traffic destined for every destination prefix. So there are altogether  $H \times K$  traffic instances/flows, which forms an  $H \times K$  traffic matrix. Each entry of the matrix represents the traffic volume of a flow. Its value is uniformly distributed between real numbers 0 and 20. Looping is not allowed. So if a neighboring AS has forwarded an advertisement for prefix  $P_k$  to the local AS, this AS cannot inject traffic for prefix  $P_k$  into the local AS.

Two sets of simulations are conducted based on the parameters used in [5]. In particular, simulation results based on ( $N = 100, X = 25, H = 12, K = 35$ ) are plotted in Fig. 4 and Fig. 5. Simulation results based on ( $N = 100, X = 30, H = 17, K = 110$ ) are shown in Fig. 6 and Fig. 7. Each point of simulation results is obtained by taking the average of 20 independent experiments each with a randomly generated BRITE network topology and traffic matrix.

### C. MPPF vs other algorithms

Besides MPPF algorithm, the following algorithms are implemented for comparison:

- BTF (Biggest Traffic First): BTF is an alternative heuristic that might be used by an ISP [5]. In BTF, the set of traffic instances are sorted in non-increasing order. For each traffic instance  $t(h, k)$ , an attempt is made to search for the best shortest path with sufficient capacity connecting the sets  $In(h)$  and  $Out(k)$ . The ingress and egress links are returned automatically. If prefix  $P_k$  has already been assigned to a particular egress link and which still has sufficient egress capacity, the search is limited to paths going to the same egress link only. Otherwise, the search is not limited by any egress link.
- MPPF\_NI (Most Popular Prefix First with No Ingress Recommendation). MPPF\_NI is the same as MPPF except that ingress edges of all transit traffic flows are determined by neighboring ASes and the local AS does not make any recommendations.
- ICS (Infinite Capacity Solution): This is obtained by assuming all ingress capacities, egress capacities and internal link capacities are infinite. It serves as a lower bound.

Note that the algorithms proposed in [5] cannot be extended to cover the ingress-to-egress route configuration problem. In [5], the ingress edges of the traffic flows are assumed to be known in advance and so traffic flows going to the same prefix can be aggregated into a job as in the generalized assignment problem [11]. Also the path used is assumed to be always the shortest path and intra-domain link capacities are assumed to be infinity. However, in our ingress-to-egress route configuration problem, all these assumptions do not hold.

Assume the initial unidirectional capacity of all ingress links and all egress links are fixed to  $ExtBW$ . Also assume that the initial unidirectional capacity of all intra-domain links are fixed to  $IntBW$ . The performance of using two different values of  $IntBW$  is shown in Fig. 5. Fig. 4 and Fig. 6 show the percentage of traffic sent against  $ExtBW$ . Fig. 5 and Fig. 7 show the solution cost, which is normalized by the solution cost obtained using ICS algorithm, against  $ExtBW$ .

From Fig. 4 and Fig. 6, we can see that MPPF requires lower edge capacity than BTF to forward 100% of traffic. In particular, when edge capacity is not enough ( $< 600$  in Fig. 4 and  $< 1200$  in Fig. 6), our MPPF algorithm can forward up to

9.14% and 25% more traffic than BTF algorithm in the two different parameter settings respectively.

From Fig. 5 and Fig. 7, we can see that the normalized solution cost for BTF is worse than that for MPPF. In fact, the normalized solution cost for BTF cannot converge to that of ICS. We can see that the normalized solution cost for BTF is about 10% higher than that of MPPF. For MPPF\_NI, since there is no ingress edge recommendation, its normalized solution cost is 35% - 40% higher than MPPF.

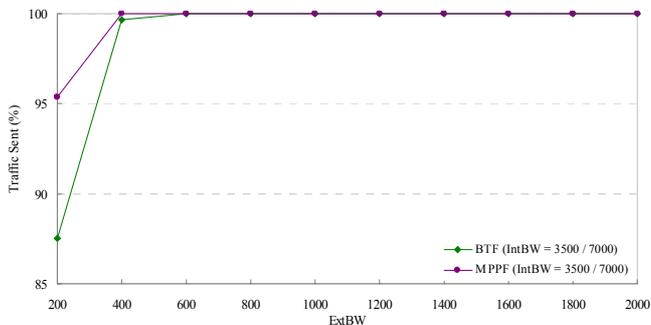


Fig. 4 Percentage of traffic sent ( $N = 100, X = 25, H = 12$  and  $K = 35$ )

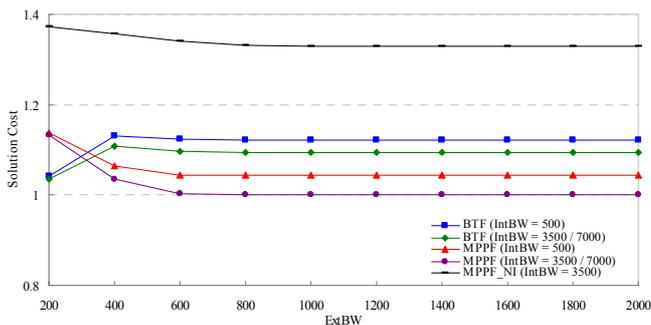


Fig. 5 Normalized solution cost ( $N = 100, X = 25, H = 12$  and  $K = 35$ )

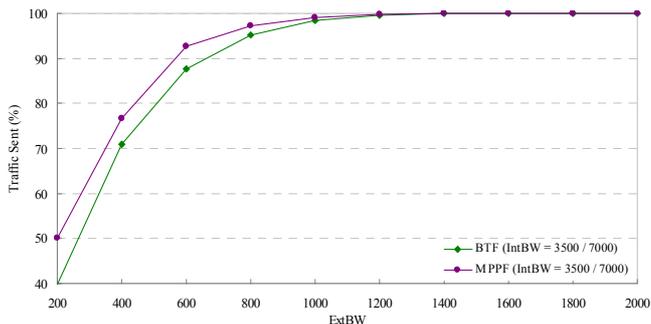


Fig. 6 Percentage of traffic sent ( $N = 100, X = 30, H = 17$  and  $K = 110$ )

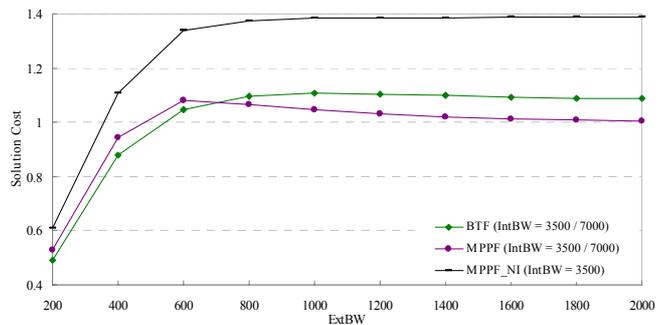


Fig. 7 Normalized solution cost ( $N = 100, X = 30, H = 17$  and  $K = 110$ )

## VI. CONCLUSIONS

The BGP ingress-to-egress route configuration problem is to find a set of paths in an AS/ISP to carry the transit flows, such that the amount of network resources consumed is minimized without violating the bandwidth constraint on all network links. To solve the problem, we first formulated it using Integer Linear Programming (ILP). Due to the high complexity involved in ILP, a heuristic algorithm, called MPPF, was then proposed. MPPF was designed based on the idea that heavily-loaded destination prefixes should be given higher priority to select less expensive edge links and routes.

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