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Benchmarking the Task Graph Scheduling Algorithms

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Abstract

The problem of scheduling a weighted directed acyclic graph (DAG) to a set of homogeneous processors to minimize the completion time has been extensively studied. The NP-completeness of the problem has instigated researchers to propose a myriad of heuristic algorithms. While these algorithms are individually reported to be efficient, it is not clear how effective they are and how well they compare against each other. A comprehensive performance evaluation and comparison of these algorithms entails addressing a number of difficult issues. One of the issues is that a large number of scheduling algorithms are based on radically different assumptions, making their comparison on a unified basis a rather intricate task. Another issue is that there is no standard set of benchmarks that can be used to evaluate and compare these algorithms. Furthermore, most algorithms are evaluated using small problem sizes, and it is not clear how their performance scales with the problem size. In this paper, we first provide a taxonomy for classifying various algorithms into different categories according to their assumptions and functionalities. We then propose a set of benchmarks which are of diverse structures without being biased towards a particular scheduling technique and still allow variations in important parameters. We have evaluated 15 scheduling algorithms, and compared them using the proposed benchmarks. Based upon the design philosophies and principles behind these algorithms, we interpret the results and discuss why some algorithms perform better than the others.

Keywords: Performance Evaluation, Benchmarks, Multiprocessors, Parallel Processing, Scheduling, Task Graphs, Scalability.

1 Introduction

The problem of scheduling a weighted directed acyclic graph (DAG), also called a task graph or macro-dataflow graph, to a set of homogeneous processors to minimize the completion time, has intrigued researchers even before the advent of parallel computers. The problem is NP-complete in its general forms [15], and polynomial-time solutions are known only for a few restricted cases [11]. Since tackling the scheduling problem in an efficient manner is imperative for achieving a meaningful speedup from a parallel or distributed system, it continues to be a focus of great attention from the research community. Considerable research efforts expended in solving the problem have resulted in a myriad of heuristic algorithms. While each heuristic is individually reported to be efficient, it is not clear how effective these algorithms are and how they compare against each other on a unified basis.

The objectives of this study include proposing a set of benchmarks and using them to evaluate the performance of a set of DAG scheduling algorithms (DSAs) with various parameters and performance measures. Since a large number of DSAs have been reported in the literature with radically different assumptions, it is important to demarcate these algorithms into various classes according to their assumptions about the program and machine model. A performance evaluation and comparison study should provide answers to the following questions:

- What are the important performance measures? The performance of a DSA is usually measured in terms of the quality of the schedule (the total duration of the schedule) and the running time of the scheduling algorithm. Sometimes, the number of target processors allocated is also taken as a performance parameter. One problem is that usually there is a trade-off between the first two performance measures; that is, efforts to obtain better solution often incur a higher time-complexity. Furthermore, using more processors can possibly result in a better solution. Another problem is that most algorithms are evaluated using small problem sizes, and it is not known how the algorithms scale with the problem size.
- What problem parameters affect the performance? The performance of DSAs, in general, tends to bias towards the problem graph structure. In addition, other parameters such as the communication-to-computation ratio, the number of nodes and edges in the graph, and the number of target processors also affect the performance of a DSA. Thus, it is important to measure the performance of DSAs by robustly testing them with various ranges of such parameters.
- What benchmarks should be used? There does not exist any set of benchmarks that can be considered as a standard to evaluate and compare various DSAs on a unified basis. The most common practice is to use random graphs. The use of task graphs derived from various parallel applications is also common. However, in both cases, there is again no standard that can provide a robust set of test cases. Therefore, there is a need for a set of benchmarks that are representative of various types of synthetic and real test cases. These test cases should be diverse without being biased towards a particular scheduling technique and should allow variations in important parameters.
- How does the performance of DSAs vary? Since most DSAs are based on heuristics techniques, bounds on their performance levels and variations from the optimal solution are not known. In addition, the average, worst, and best case performance of these algorithms is not known. Furthermore, since not all DSAs make identical assumptions, they must be segregated and evaluated within various categories.
- Why some algorithms perform better? Although some qualitative and quantitative comparisons of some DSAs have been carried out in the past (see [16], [19], [30]), they mainly presented experimental results without giving a rationale of why some algorithms perform well and some do not. The previous studies were also limited to a few algorithms and did not make a comprehensive evaluation. The design philosophies and characteristics of various algorithms must be understood in order to assess their merits and deficiencies. The qualitative analyses can ensue some future guidelines for designing even better heuristics.

In this paper, we describe a performance study of various DSAs with the aim of providing answers to the questions posed above. First, we define the DAG scheduling problem in the next section, and provide an overview of various fundamentals scheduling techniques and attributes that are shared by a vast number of DSAs in Section 3. This is followed by a chronological summary and a taxonomy of various DSAs reported in the literature presented in Section 4. Since it is not the objective of this research to provide a survey on this topic, the purpose of this taxonomy is to set a context in which we select a set of algorithms and explain their major characteristics. All of these algorithms have been implemented on a common platform and tested using the same suite of benchmark task graphs with a wide
assumptions simply based on the levels or other attributes of the nodes. The static
list vs. dynamic list: The set of ready nodes are often maintained as a ready list. Initially, the ready list includes only the
entry nodes. After a node is scheduled, the nodes freed by the scheduled node are inserted into the ready list such that the list is
sorted in descending order of node priorities. The list can be maintained in two ways: A ready list is static if it is constructed before scheduling starts and remains the same throughout the
whole scheduling process. A ready list is dynamic if it is rearranged according to the changing node priorities.
Greedy vs. non-greedy: In assigning a node to a processor, most scheduling algorithms attempt to minimize the start-time of a
node. This is a greedy strategy. However, some algorithms do not necessarily minimize the start-time of a node but consider other
factors as well.
Time-complexity: The time-complexity of a DSA is usually expressed in terms of the number of node, v, the number of edges, e, and the number of processors, p. The major steps in an algorithm include a traversal of the DAG and a search of slots in the processors to place a node. Simple static priority assignment in general results in a lower time-complexity while dynamic priority assignment inevitably leads to a higher time-complexity of the scheduling algorithm. Backtracking can incur a very high time complexity and is therefore not usually employed.

A Classification of DAG Scheduling Algorithms

The static DAG scheduling problem has been tackled with large variations in the task graph and machines models. Figure 1 provides a classification and chronological summary of various static DSAs. Since it is not the purpose of this paper to provide a survey of such algorithms, this summary is by no means complete (a more extensive taxonomy on the general scheduling problem has been proposed in [8]). Furthermore, a complete overview of the literature is beyond the scope of this paper. Nevertheless, we believe our classification scheme can be extended to most of the reported DSAs.

Earlier algorithms have made radically simplifying assumptions about the task graph representing the program and the
model of the parallel processor system [11]. These algorithms assume the graph to be of a special structure such as a tree, fork-join, etc. In general, however, parallel programs come in a variety of structures, and as such many recent algorithms are designed to tackle arbitrary graphs. These algorithms can be further divided into two categories. Some algorithms assume the computational costs of all the tasks to be uniform [11] whereas other algorithms assume the computational costs of tasks to be arbitrary. Some of the earlier work has also assumed the inter-task communication to be zero, that is, the task graph contains precedence but without cost. The problem becomes less complex in the absence of communication delays. Furthermore, scheduling with
communication delays is NP-complete.

Scheduling with communication may be done using duplication or without duplication. The rationale behind the task duplication based (TDB) scheduling algorithms is to reduce the communication overhead by redundantly allocating some nodes to multiple processors. In duplication-based scheduling, different strategies can be employed to select ancestor nodes for duplication.

Non-TDB algorithms assuming arbitrary task graphs with arbitrary costs on nodes and edges can be divided into two categories: some scheduling algorithms assume the availability of unlimited number of processors, while some other algorithms assume a limited number of processors. The former class of algorithms are called the UNC (unbounded number of clusters) scheduling algorithms [3] and the latter the BNP (bounded number of processors) scheduling algorithms [3]. In both classes of algorithms, the processors are assumed to be fully-connected and no attention is paid to link contention or routing strategies used for communication. The technique employed by the UNC algorithms is also called clustering (see [14], [16], [20], [26], [34] for details). At the beginning of the scheduling process, each node is considered a cluster. In the subsequent steps, two clusters are merged if the merging reduces the completion time. This merging procedure continues until no cluster can be merged. The rationale behind the UNC algorithms is that they can take advantage of using more processors to further reduce the schedule length. However, the clusters generated by the UNC may need a post-processing step for mapping the clusters onto the processors because the number of processors available may be less than the number of clusters.

A few algorithms have been designed to take into account the most general model in which the system is assumed to consist of an arbitrary network topology, of which the links are not contention-free. These algorithms are called the APN (arbitrary processor network) scheduling algorithms [3]. In addition to scheduling tasks, the APN algorithms also schedule messages on the network communication links.

In the following we list the algorithms chosen in our study. For detailed descriptions and characteristics we refer the reader to the cited publications. To narrow the scope of this paper, we do not consider TDB algorithms (for a more detailed overview of such algorithms, see [13]).

- BNP Scheduling Algorithms: HLFET [11], ISH [21], MCP [32], ETF [17], DLS [31], and LAST [7].
- UNC Scheduling Algorithms: EZ [28], LC [20], DSC [34], MD [32], and DCP [22].

5 Benchmark Graphs

In our study, we propose and use a suite of benchmark graphs consisting of 5 different sets. The generation techniques and characteristics of these benchmarks are described as follows:

5.1 Peer Set Graphs

The Peer Set Graphs (PSGs) are example task graphs used by various researchers and documented in publications. These graphs are usually small in size but are useful in that they can be used to trace the operation of an algorithm by examining the schedule produced. A detailed description of the graphs is provided in Section 6.1.

5.2 Random Graphs with Optimal Solutions

These are random graphs for which we have obtained optimal solutions using a branch-and-bound algorithm. We call these graph random graphs with optimal solutions using branch-and-bound (RGBOS). This suite of random task graphs consists of three subsets of graphs with different CCRs (0.1, 1.0, and 10.0). Each subset consists of graphs in which the number of nodes vary from

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* We use the term cluster and processor interchangeably since in the UNC scheduling algorithms, merging a single node cluster to another cluster is analogous to scheduling a node to a processor.
10 to 32 with increments of 2, thus, totalling 12 graphs per set. The graphs were randomly generated as follows: First the construction cost of each node in the graph was randomly selected from a uniform distribution with the mean equal to 40 (minimum = 2 and maximum = 78). Beginning with the first node, a random number indicating the number of children was chosen from a uniform distribution with the mean equal to \( \nu/10 \). The communication cost of each edge was also randomly selected from a uniform distribution with the mean equal to 40 times the specified value of CCR. To obtain optimal solutions for the task graphs, we applied a parallel A* algorithm [23] to the graphs. Since generating optimal solutions for arbitrarily structured task graphs takes exponential time, it is not feasible to obtain optimal solutions for large graphs.

5.3 Random Graphs with Pre-Determined Optimal Schedules

These are random graphs with pre-determined optimal solutions (RGPOS). The method of generating graphs with known optimal schedules is as follows: Suppose that the optimal schedule length of a graph and the number of processors used are specified as \( L_{opt} \) and \( p \) respectively. For each PE \( i \), we randomly generate a number \( n_i \) from a uniform distribution with mean \( \nu / p \). The time interval between 0 and \( L_{opt} \) of PE \( i \) is then randomly partitioned into \( n_i \) sections. Each section represents the execution span of one task; thus, \( x_i \) tasks are “scheduled” to PE \( i \) with no idle time slot. In this manner, \( v \) tasks are generated so that every processor has the same schedule length. To generate an edge, two tasks \( n_i \) and \( n_j \) are randomly chosen such that \( FT(n_i) < ST(n_j) \). The edge is made to emerge from \( n_i \) to \( n_j \). As to the edge weight, there are two cases to consider: (i) the two tasks are scheduled to different processors, and (ii) the two tasks are scheduled to the same processor. In the first case the edge weight is randomly chosen from a uniform distribution with maximum equal to \( (ST(n_j) - FT(n_i)) \) (the mean is adjusted according to the given CCR value). In the second case the edge weight can be an arbitrary positive integer because the edge does not affect the start and finish times of the tasks which are scheduled to the same processor. We randomly chose the edge weight for this case according to the given CCR value. Using this method, we generated three sets of task graphs with these CCRs: 0.1, 0.5, and 1.0. Each set consists of graphs for which the number of nodes vary from 50 to 500 in increments of 50; thus, each set contains 10 graphs.

5.4 Random Graphs without Optimal Schedules

The fourth set of benchmark graphs, referred to as random graphs with no known optimal solutions (RGNOS), consists of 250 randomly task graphs. The method of generating these random task graphs is the same as that in RGBOS. However, the sizes of these graphs are much larger, varying from 50 nodes to 500 nodes with increments of 50. For generating the complete set of 250 graphs, we varied three parameters: size, communication-to-computation ratio (CCR), and parallelism. Five different values of CCR were selected: 0.1, 0.5, 1.0, 2.0 and 10.0. The parallelism parameter determines the width (defined as the largest number of non-precedence-related nodes in the DAG) of the graph. Five different values of parallelism were chosen: 1, 2, 3, 4 and 5. A parallelism of 1 means the average width of the graph is \( \nu / \sqrt{v} \), a value of 2 means the graph has an average width of \( \nu / 2 \) and so on. Our main rationale for using these large random graphs as a test suite is that they contain as their subset a variety of graph structures. This avoids any bias that an algorithm may have towards a particular graph structure.

5.5 Traced Graphs

The last set of benchmark graphs, called traced graphs (TG), represent some of the numerical parallel application programs obtained via a parallelizing compiler [3]. We use Cholesky factorization graphs for this category.

6 Performance Results and Comparison

In this section, we present the performance results and comparisons of the 15 scheduling algorithms which were implemented on a SUN SPARC IPX workstation with all of the benchmarks described above. The algorithms are compared within their own classes, although some comparison of UNC and BNP algorithms are also carried out. The comparisons are made using the following six measures.

- **Normalized Schedule Length (NSL):** The main performance measure of an algorithm is the schedule length of its output schedule. The NSL of an algorithm is defined as:

  \[ NSL = \frac{L}{\sum_{i \in CP} w(i)} \]

  where \( L \) is the schedule length. It should be noted that the sum of computation costs on the CP represents a lower bound on the schedule length. Such lower bound may not always be possible to achieve, and the optimal schedule length may be larger than this bound.

- **Number of Processors Used:** The number of processors used is another important measure of an algorithm and it varies widely for different algorithms. The number of processors used are measured for the BNP and UNC algorithms.

- **Running Time of the Algorithm:** The running time of a scheduling algorithm is another important performance measure because a long running time can severely limit the scalability of an algorithm.

6.1 Results for the Peer Set Graphs

The results of applying the UNC and BNP algorithms to the PSC are shown in Table 1. The APN algorithms were not applied to this set of example graphs because many network topologies are possible as test cases making a fair comparison quite difficult. As can be seen from the table, the schedule lengths produced vary considerably, despite the small sizes of the graphs. This phenomenon is contrary to our expectation that the algorithms would generate the same schedule lengths for most of the cases. It also indicates that the performance of various DSA’s is more sensitive to the diverse structures of the graphs rather than their sizes. A plausible explanation for this pathological observation is that the ineffective scheduling technique employed in some algorithms leads to mistakes made in the earlier stages of the scheduling process so that long schedule lengths are produced.

6.2 Results for RGBOS benchmarks

The results of the UNC and BNP algorithms for the RGBOS benchmarks are shown in Table 2 and Table 3, respectively. Since
optimal solutions for specific network topologies are not known, the APN algorithms were again not applied to these benchmarks. Table 2 includes the percentage degradations from the optimal schedule lengths produced by the UNC algorithms. The overall average degradations for each algorithm are given in the last row. As can be seen, when CCR is 0.1, both MD and DCP generate optimal solutions for half of the test cases, and the overall average degradation is less than 2%. Other algorithms generate optimal solutions for few number of cases and the overall average degradation is larger. Among all the UNC algorithms, the DCP algorithm performs the best.

Table 2: The percentage degradations from the optimal solutions of for the RGBOS benchmarks (UNC algorithms).

<table>
<thead>
<tr>
<th>CCR</th>
<th>0.1</th>
<th>0.3</th>
<th>0.5</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Algorithm</td>
<td>LC</td>
<td>EZ</td>
<td>MD</td>
<td>DCP</td>
</tr>
<tr>
<td>&lt;0.01</td>
<td>85</td>
<td>84</td>
<td>86</td>
<td>89</td>
</tr>
<tr>
<td>0.01</td>
<td>86</td>
<td>85</td>
<td>87</td>
<td>90</td>
</tr>
<tr>
<td>0.05</td>
<td>87</td>
<td>86</td>
<td>88</td>
<td>91</td>
</tr>
<tr>
<td>0.1</td>
<td>88</td>
<td>87</td>
<td>89</td>
<td>92</td>
</tr>
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</table>

Table 3: The percentage degradations from the optimal solutions of for the RGBOS benchmarks (BNP algorithms).

<table>
<thead>
<tr>
<th>CCR</th>
<th>0.1</th>
<th>0.3</th>
<th>0.5</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Algorithm</td>
<td>BNP</td>
<td>TET</td>
<td>LAST</td>
<td>WLP</td>
</tr>
<tr>
<td>&lt;0.01</td>
<td>30</td>
<td>12</td>
<td>15</td>
<td>21</td>
</tr>
<tr>
<td>0.01</td>
<td>31</td>
<td>12</td>
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<td>22</td>
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<tr>
<td>0.05</td>
<td>32</td>
<td>12</td>
<td>15</td>
<td>23</td>
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<tr>
<td>0.1</td>
<td>33</td>
<td>12</td>
<td>15</td>
<td>24</td>
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Table 3 indicates that the BNP algorithms generate fewer optimal solutions compared to the DCP algorithm. The overall average degradations are also higher than that of the DCP algorithm. However, compared with other UNC algorithms, the MCP, TET, ISH, and DLS algorithms perform better both in terms of the number of optimal solutions generated and the overall degradations. Among all the BNP algorithms, the MCP algorithm performs the best while the LAST algorithm performs the worst.

We summarize our observations from Table 2 and Table 3 as follows.

- Greedy BNP algorithms have shown higher capability in generating optimal solutions than the non-greedy and non-CP-based UNC algorithms with DCP as the only exception.
- CP-based algorithms are clearly better than the non-CP-based ones as can be seen from the results of DCP and MCD.

6.3 Results for the RGBOS Benchmarks

The results of applying the UNC and BNP algorithms to the RGBOS benchmarks are shown in Table 4 and Table 5, respectively. Since optimal solutions for specific network topologies are not known, the APN algorithms were again not applied to the RGBOS task graphs. In Table 4, the percentage degradations from the optimal schedule lengths of the UNC algorithms are shown. The overall average degradations for each algorithm are again shown in the last row of the table. As can be seen, when CCR is 0.1, the DCP generates optimal solutions for more than half of the test cases and the overall average degradation is less than 2%. Other algorithms generate optimal solutions for a few number of cases and the overall average degradation is larger. The percentage degradations in general increase with CCRs. When CCR is 0.0, none of the UNC algorithms except DCP can generate any optimal solution. The results given in Table 5 indicate that the BNP algorithms generate a similar number of optimal solutions and values of percentage degradations. When CCR is 10.0, none of the BNP algorithms generates any optimal solutions. In summary, the results of Table 4 and Table 5 lead to similar conclusions as those made in Section 6.2.

Table 4: The percentage degradations from the optimal solutions of for the RGBOS benchmarks (UNC algorithms).

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<tr>
<th>CCR</th>
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<td>0.1</td>
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Table 5: The percentage degradations from the optimal solutions of for the RGBOS benchmarks (BNP algorithms).

<table>
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<tr>
<th>CCR</th>
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<td>23</td>
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<td>0.1</td>
<td>33</td>
<td>12</td>
<td>15</td>
<td>24</td>
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</table>

6.4 Results for the RGBNS Benchmarks

Since the optimal solutions for the RGBNS benchmarks are not known, we evaluate and compare the algorithms with a more extensive range of parameters including graph sizes, CCRs, and parallelisms.

6.4.1 Comparing Schedule Lengths

The average NSLs for the BNP, UNC, and APN scheduling algorithms are given in Figure 2. Each curve in the plots is the average of 25 test cases with various CCRs and parallelisms. Figure 2 reveals that the behavior of these algorithms is consistent in terms of their relative performance for various number of nodes in the graph. Among the BNP scheduling algorithms, the performance of the MCP algorithm is the best while the LAST algorithm is outperformed by all other algorithms. We also observe that the NSLs for all the algorithms show a slightly increasing trend if the task graph size is increased. This is because the proportion of nodes other than those on the CP increases making it more difficult to achieve the lower bound. For the UNC scheduling algorithms, we observe that the DCP and MD algorithms perform significantly better as compared to the rest of the algorithms. The NSLs for the DSC and LC algorithms are similar.

Although the BNP algorithms are designed for a limited number of processors (as an input parameter), we ran each algorithm with a very large number of processor such that the number of processors became virtually unlimited. From this experiment, we noted the average number of processors used by these algorithms for each graph size (the number of processors used is shown later in Figure 3). In another experiment, we reduced the number processors to 50% of that average. Since no significant difference in the NSLs as well as the relative performance of these algorithms can be observed, we do not include those results in this paper. One possible reason for this phenomenon is that the schedule length is dominated by the scheduling of CP nodes. In the case of a very large number of processors, the non-CP nodes are spread across many processors, while in the case of a fewer number of processors, these nodes are packed together without making much impact on the overall schedule length.

For the APN scheduling algorithms, the target architectures included an 8-processor ring, an 8-processor hypercube, a 4 x 2 mesh, and an 8-processor clique. The average NSLs for these experiments are shown in Figure 2b). Each point on the curve now represents the average of 100 NSLs. One reason for the much larger NSLs in these cases is that the number of processors used were
algorithms for various number of nodes in the task graph. Each

These numbers for the HLFET and

uses a large number of processors. This is because it uses

value in the table again is the average of 25 cases. The MCP

networks with more communication links. However, these results

impact on the overall schedule length. In terms of the impact of the

main reason for the better performance of BSA is an efficient

scheduling of communication messages that can have a drastic

performance. For example, significant differences are

observed between the NSLs of BSA and BU. The performance of DLS is relatively stable with respect to the graph size while MH yields fairly long schedule lengths for large graphs. As can be seen, the BSA algorithm performs admirably well for large graphs. The main reason for the better performance of BSA is an efficient scheduling of communication messages that can have a drastic

impact on the overall schedule length. In terms of the impact of the topology, we find that all algorithms perform better on the networks with more communication links. However, these results are excluded due to space limitations.

Figure 3(a) shows the average number of processors used by

the BNP scheduling algorithms. The DLS algorithm uses the

smallest number of processors, even compared to ETF although both algorithms share similar concepts. The numbers of processors used by the MCP and ETF algorithms are close. On the other hand, these numbers for the HLFET and ISH are also similar.

Figure 3(b) shows the average number of processors used by

the UNC scheduling algorithms. As can be seen, the DSC algorithm uses a large number of processors. This is because it uses a new processor for every node whose start time cannot be reduced on a processor already in use. The LC and EZ algorithms also use more processors than others because they pay no attention on the use of processors. In contrast, the DCP algorithm has a special processor finding strategy: as long as the schedule length is not affected, it tries to schedule a child to a processor holding its parent even though its start time may not reduce. The MD algorithm also uses relatively smaller number of processors because, to schedules a node to a processor, it first scans the already used processors.

6.4.3 Algorithm Running Times

In this section, we compare the running times of all the

algorithms. Table 6 shows the running times of the BNP scheduling algorithms for various number of nodes in the task graph. Each value in the table again is the average of 25 cases. The MCP

algorithm is found to be the fastest algorithm while DLS and ETF are slower than the rest. The large running times of the DLS and ETF algorithms are primarily due to exhaustive calculations of the start times of all of the ready tasks on all of the processors. The running time of LAST and HLFET are also large while ISH takes reasonable amounts of time. Based on these running times results, the BNP algorithms can be ranked in the order: MCP, ISH, HLFET, LAST, and (DLS, ETF).

From the running times of UNC scheduling algorithms shown

in Table 6, we observe that the LC and DSC algorithms yield the

minimum running time. The running times of MD, EZ and DCP are close. Based on these running time results, these algorithms can be ranked in the order: LC, DSC, EZ, DCP, and MD. For the APN scheduling algorithms, the BU algorithm is found to be the fastest. The running times of the MH and BSA algorithms are close while those of the DLS algorithm are relatively large. Based on these results, in terms of running times, these algorithms can be ranked in the order: BU, BSA, MH, and DLS.

6.4.2 Number of Processors Used

The number of processors used by an algorithm is an important performance measure especially for the algorithms that are designed for using an unlimited number of processors. The BNP algorithms are designed for a bounded number of processors, but as explained earlier, were tested them with a very large number (virtually unlimited number) of processors; we then noted the number of processors actually used.

Figure 3(a) shows the average number of processors used by

the BNP scheduling algorithms. The DLS algorithm uses the

smallest number of processors, even compared to ETF although both algorithms share similar concepts. The numbers of processors used by the MCP and ETF algorithms are close. On the other hand, these numbers for the HLFET and ISH are also similar.

Figure 3(b) shows the average number of processors used by

the UNC scheduling algorithms. As can be seen, the DSC algorithm uses a large number of processors. This is because it uses a new processor for every node whose start time cannot be reduced on a processor already in use. The LC and EZ algorithms also use more processors than others because they pay no attention on the use of processors. In contrast, the DCP algorithm has a special processor finding strategy: as long as the schedule length is not affected, it tries to schedule a child to a processor holding its parent even though its start time may not reduce. The MD algorithm also uses relatively smaller number of processors because, to schedules a node to a processor, it first scans the already used processors.

6.4.3 Algorithm Running Times

In this section, we compare the running times of all the

algorithms. Table 6 shows the running times of the BNP scheduling algorithms for various number of nodes in the task graph. Each value in the table again is the average of 25 cases. The MCP

† The number of processors used by a typical UNC algorithm is very large—the LC algorithm, for instance, uses more than 100 processors for a 500-node task graph.
These can be good test cases for evaluating and comparing future algorithms.

The current research concentrates on further elaboration of various techniques, such as reducing the scheduling complexities, improving computation estimations, and incorporating network topology and communication traffic. A promising avenue for solving the first two problems is by parallelizing static scheduling on the target parallel machine where the user program executes [2].

In UNC algorithms, clusters obtained through scheduling are assigned to a bounded number of processors. All nodes in a cluster must be scheduled to the same processor. This property makes the cluster scheduling algorithms more complex than the standard BNP scheduling algorithms. Two such algorithms called Sarkar’s assignment algorithm and Yang’s RCP algorithm are described in [28] and [33], respectively. Sarkar’s algorithm combines the cluster merging and ordering nodes into one step, considering the execution order. RCP merges clusters without considering the execution order, which may lead to a poor decision on merging. However, RCP has a lower complexity. Both algorithms are simple and do not utilize the information provided by the UNC scheduling. Generally, cluster scheduling is a relatively unexplored area. More effective algorithms are to be designed. It would be an interesting study to compare the BNP approach with the UNC+CS approach.

The APN algorithms can be fairly complicated because they take into account more parameters. Further research is required in this area, and the effects of topology and routing strategy need to be determined.

References