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DETECTION OF VEHICLE OCCLUSION USING A GENERALIZED DEFORMABLE MODEL

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ABSTRACT
This paper presents a vehicle occlusion detection algorithm based on a generalized deformable model. A 3D solid cuboid model with up to six vertices is employed to fit any vehicle images, by varying the vertices for a best fit. The advantage of using such a model is that the number of parameterized vertices is small which can be easily deformed. Occlusion is detected by recording the changes in the Area Ratio and the dimensions of the generalized deformable model. Our tests show that the new modeling algorithm is effective in detecting vehicle occlusion.

1. INTRODUCTION
Visual traffic surveillance (VTS) is an active research area as it is believed by many that it is going to have significant impacts to most of the traffic problems in big cities today. A common goal for many of these VTS systems is to be able to identify and track the movement of vehicles. In this, deformable models are often used to model the vehicles, where vehicle types and orientation information may be extracted. However, the complexity of deformable models is high and the success of matching the vehicle image with the model can be hard to come by if the vehicle image is incomplete or occluded by other vehicles or stationary objects. One possible solution to this particular problem is to use a simple generalized model which may be more effective and robust. Evolved from the same line of argument, a simple generalized deformable model is proposed in this paper. It employs a 3D solid cuboid model with up to six vertices to fit any vehicle images, by varying the vertices for a best fit. The advantage of using such a model is that the number of parameterized vertices is small which can be easily calculated. This model was tried on a series of occlusion cases and was found to be able to discern the occluded vehicles and those that are not.

2. METHODOLOGY
The whole idea lies on the fitting of the model on the binary representation of the vehicle in 2D. Once a best fit is determined, the resulting model is transformed into 3D, where parameters such as height, width and length of the vehicle are calculated. By considering the area ratio between the model and the binary representation of the vehicle, as well as its width and height, vehicles that are occluded can be detected based on these parameters. Fig. 1 depicts the conceptual flow of the methodology employed. In this method, the binary representation of the vehicle is extracted using a background estimation algorithm. The fitting of the generalized model is performed in 2D, as the vehicle image is also in 2D. This is done by transforming the 3D model into 2D, and calculate the lines between the vertices that best fit the vehicle image. Once the best fit model is determined, this 2D model is transformed back to 3D where 3D parameters are calculated. In general, if a vehicle is not occluded, the area of the model should be slightly larger than the area of the vehicle image. When occlusion occurs, this ratio changes. In addition, the width and height of the model also indicate the presence of occlusion.

3. BINARY REPRESENTATION OF A VEHICLE
In principle, the deformable model can be applied directly to a segmented version of the image. The problem with this is that if the segmentation algorithm is not ideal, the segmented result may not be faithfully representing the vehicle concerned. Besides, segmentation usually ends up with far more details than required, and can introduce unwanted effects when fitting the model. Based on this, the concept of background estimation is adopted here. By estimating the stationary background, the moving vehicle (object) can be deduced by simply subtracting the background from the original image, as depicted in Figs. 2(b) and 2(c). Once the vehicle is extracted, its binary representation can be easily determined as given in Fig. 2(d). In this case, only the 2D outline of the vehicle is important for the model fitting, not any internal details.
camera height is \( h \) and the distance between the focusing point and the camera is \( d \). A 3D point \( P = (P_x, P_y, P_z) \) is thus projected onto the 2D camera image plane as \( p = (p_x, p_y) \).

**Figure 2 - Binary representation of a vehicle**

### 4. GENERALIZED DEFORMABLE MODEL

The generalized deformable model, \( M \), proposed is basically a solid 3D cuboid with 6 vertices, \( M = \{v_k | k = 0, \ldots, 5\} \). The vertices are parameterized such that their values can be calculated to fit a particular vehicle. A model of this type has several properties: 1) it can be used to model any type of vehicles; 2) easily deformed to fit any size of vehicles; 3) does not suffer from incomplete or occluded vehicle images. However, it should also be pointed out that because of the simplicity of the model, the type of vehicles it can differentiate would be limited. This is a compromise from the more complex deformable model with many more vertices.

In general, the model can be realized as a modified 3D wire frame projected on the a 2D plane as shown in Fig. 3. This is a modified version as the front facing three edges (dotted lines) are not considered as part of the wire frame. In other words, the 2D model consists of only the outlines defined by \( v_0 \) to \( v_5 \). For this reason, this model has three pairs of parallel edges along three 2D orientations (\( \hat{x} \), \( \hat{y} \) and \( \hat{z} \)) as depicted. The fitting is only confined to these six lines.

Once the model fitting in 2D is completed, the \( \hat{x} \), \( \hat{y} \) and \( \hat{z} \) orientation components must be transformed to 3D orientations \( \hat{X} \), \( \hat{Y} \) and \( \hat{Z} \). If the 3D vehicle features are to be determined, this transformation between the 2D and 3D spaces is mainly determined by the camera model depicted in Fig. 4, where the camera is focusing at point \( O \) with focal length \( f \). The

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**Figure 3 - Generalized deformable model.**

4D-to-2D mapping function:

\[
\begin{align*}
px &= P_x \sqrt{f^2 + p_y^2} / \sqrt{(d + P_x)^2 + (h - P_y)^2} \\
py &= f \left[ hP_y + dP_x \right] / d \left[ (d + P_x)^2 + h(h - P_y) \right] \\
pz &= P_z \sqrt{f^2 + p_y^2} / \sqrt{(d + P_x)^2 + (h - P_y)^2} \\
p &= (p_x, p_y, p_z)
\end{align*}
\]

When the three 2D orientations \( \hat{x} \), \( \hat{y} \) and \( \hat{z} \) are determined, model \( M \) is created along these orientations and its vertices are adjusted to fit the vehicle image, where these vertices must satisfy the following criteria:

\[
|v_0 - v_1| = |v_3 - v_4| = |v_2 - v_3| = |v_5 - v_6| \\
|v_1 - v_2| = |v_4 - v_5| \quad \text{and} \quad |v_2 - v_3| = |v_5 - v_6|
\]

where \( |a-b| \) denotes the distance between \( a \) and \( b \). This ensures the model obtained is regular as the model does not make any assumption on the camera perspective. If we allow \( M \) to be irregular without knowing or considering the camera perspective, such irregularity may be due to the camera perspective or the shape of the vehicle. Using the above fitting approach and criteria, Fig. 5 illustrates an example of a vehicle fitted by the model. It can be seen that the model fitted is not perfect, but is close enough to represent the vehicle.
5. 3D MODEL PARAMETERS

To determine the 3D parameters of model $M$, it is necessary and appropriate to assume that $V_1$, $V_2$, and $V_3$ are on the plane of the road surface, i.e., $P_n = 0$. Therefore, the width and depth of the model can be computed by Eqs. (4) and (5) respectively. Furthermore, as $V_3$ is directly above $V_1$, by solving Eqt. (6), the height of the model can be determined.

\[
\text{width} = |\Phi^{-1}(v_2, 0) - \Phi^{-1}(v_3, 0)| \quad \ldots (4)
\]
\[
\text{depth} = |\Phi^{-1}(v_3, 0) - \Phi^{-1}(v_2, 0)| \quad \ldots (5)
\]
\[
\text{height} = V_1 - V_2
\]
\[
\Phi^{-1}(v_3, \text{height}) = \Phi^{-1}(v_1, 0) + \begin{pmatrix} 0 \\ \text{height} \end{pmatrix} \quad \ldots (6)
\]

6. OCCLUSION DETECTION

Essentially, occlusion is detected by monitoring the changes of the 3D model parameters and an extra parameter called Area Ratio, $R_{\text{area}}$, as given in Eqt. (7).

\[
R_{\text{area}} = \frac{A_{\text{mask}}}{A_{\text{model}}} \quad \ldots (7)
\]

where $A_{\text{mask}}$ is the area of the binary vehicle image and $A_{\text{model}}$ is the area of model $M$. The Area Ratio basically describes how well the model fits the binary vehicle image. As $A_{\text{model}}$ is always larger than $A_{\text{mask}}$, $R_{\text{area}}$ is always less than one. An ideal fit is that $R_{\text{area}}$ equals to one, whereas a good fit means $R_{\text{area}}$ is close to one, and a poor fit means otherwise. The difference in $R_{\text{area}}$ can also be used to discern different types of vehicles in a limited sense.

The argument is that when occlusion occurs, $R_{\text{area}}$ and the dimension of the model change abruptly. Figs. 6 and 7 illustrate two possible occlusion cases. In Fig. 6, the vehicle on the right is occluded by the bus in the adjacent lane. The 3D model fitted as a result is much wider than expected and does not match with the usual dimensions of typical vehicles. It also reduces the $R_{\text{area}}$ value substantially. Fig. 7 is similar except that the model lengthens. The reduction in $R_{\text{area}}$ is not as severe as Fig. 6.

Therefore, the monitoring of occlusion is carried out by comparing the 3D dimensions and $R_{\text{area}}$ of the model in the current image, $n$, with the last image without occlusion, $m$, according to Eqt. (8).

\[
|R_{\text{area}}(n) - R_{\text{area}}(m)| > \epsilon_1 \quad \text{or} \quad |R_{\text{width}}(n) - R_{\text{width}}(m)| > \epsilon_2 \quad \text{or} \quad |R_{\text{height}}(n) - R_{\text{height}}(m)| > \epsilon_3 \quad \ldots (8)
\]

where $R_{\text{width}}$ and $R_{\text{height}}$ are the normalized width and height of the vehicle model. The values $\epsilon_1$, $\epsilon_2$, and $\epsilon_3$ are thresholds to permit small changes in the values. The values of $\epsilon_1$, $\epsilon_2$, and $\epsilon_3$ used in our evaluations are both 0.05. When there is no occlusion, $R_{\text{area}}$ should be relatively constant, close to one. This is also true for the other model parameters too. However, when occlusion occurs, $R_{\text{area}}$ decreases and some of the other parameters increase.

To prove the proposed occlusion detection method, two model cars moving in a laboratory environment are set up, with a camera mounted on a tripod at about 0.3m above a model road. An image sequence was acquired and subject to the method proposed in Fig. 1, where for each image, the vehicles' binary representations are generated, 2D model fitted, and 3D model and parameters determined, as well as $R_{\text{area}}$ calculated. Fig. 8 depicts a sample set of the image sequence with the 3D model overlaid on the images, and Table 1 shows the parameters obtained for the 'bus' and the detection results.

<table>
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<tr>
<th>Image</th>
<th>$R_{\text{area}}$</th>
<th>$R_{\text{width}}$</th>
<th>$R_{\text{height}}$</th>
<th>Occlusion</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.88</td>
<td>0.42</td>
<td>0.57</td>
<td>×</td>
</tr>
<tr>
<td>2</td>
<td>0.87</td>
<td>0.44</td>
<td>0.56</td>
<td>×</td>
</tr>
<tr>
<td>3</td>
<td>0.60</td>
<td>0.62</td>
<td>0.32</td>
<td>✓</td>
</tr>
<tr>
<td>4</td>
<td>0.79</td>
<td>0.82</td>
<td>0.60</td>
<td>✓</td>
</tr>
<tr>
<td>5</td>
<td>0.80</td>
<td>0.37</td>
<td>0.84</td>
<td>✓</td>
</tr>
<tr>
<td>6</td>
<td>0.61</td>
<td>0.22</td>
<td>0.64</td>
<td>✓</td>
</tr>
<tr>
<td>7</td>
<td>0.85</td>
<td>0.40</td>
<td>0.55</td>
<td>×</td>
</tr>
<tr>
<td>8</td>
<td>0.86</td>
<td>0.38</td>
<td>0.54</td>
<td>×</td>
</tr>
</tbody>
</table>

Table 1 - Simulation results for 'bus'
As can be seen from the table, the non-occluded cases have $R_{area}$ in the range of 0.85 or above, and the model width and height vary within a small range. On the other hand, the occluded cases have small $R_{area}$ and both $R_{width}$ and $R_{height}$ different from the typical figures by a large margin.

7. CONCLUSION

In conclusion, the occlusion detection method based on a generalized deformable model as presented in this paper is an effective way for detecting vehicle occlusion. Central to the method is a generalized deformable model, which is characterized by its small number of vertices and the transformation between the 2D and 3D spaces for model fitting. According to our preliminary tests, the model is able to fit different types and sizes of vehicles. By monitoring the changes in the area ratio, model width and height with respect to previous images, vehicle occlusion can be detected successfully. This result will have positive impact to the subsequent segmentation and tracking of vehicles. Further development of this method will be focused on the evaluation on road traffic scenes and on the study of how the generalized model can be used for a wider class of vehicles.

8. REFERENCES


