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Fault-Based Testing of
Database Application Programs with Conceptual Data Model

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Abstract

Database application programs typically contain program units that use SQL statements to manipulate records in database instances. Testing the correctness of data manipulation by these programs is challenging. When a tester provides a database instance to test such a program, the program unit may output faulty SQL statements and, hence, manipulate inappropriate database records. Nonetheless, these failures may only be revealed in very specific database instances.

This paper proposes to integrate SQL statements and the conceptual data models of an application for fault-based testing. It proposes a set of mutation operators based on the standard types of constraint used in the enhanced entity-relationship model. These operators are semantic in nature. This semantic information guides the construction of affected attributes and join conditions of mutants. The usefulness of our proposal is illustrated by an example in which a missing-record fault is revealed.

Keywords: database application testing, fault-based testing, semantic mutants.

1. Introduction

Testing is the most popular means to assure software quality. Among the factors that may affect test results, the environment such as the operating system and the databases is an important issue. In particular, little research on unit testing techniques focuses on the interaction between an application and the databases [15]. We propose a fault-based testing technique in this paper.

Typical database application programs (DB applications) use structured query languages (SQL) [1], such as Oracle 10g, to manipulate data governed by database systems. These data are described structurally in database systems as database schemas, which are sets of rules to define the organization and integral relationships of data. A set of data records satisfying a particular database schema is known as a database instance. Similarly to [15], we define a DB application to be a program unit with a set of database schema. To process a database instance of a database schema, a program unit accepts parametric input values and outputs relevant SQL statements, each of which is a specification of the intended manipulation procedure. Actual records in the database instance are then manipulated according to the SQL statements.

To test a DB application, therefore, testers need to handle this indirect manipulation of data. Testers input a combination of database instances and parametric input values, if any, applicable to run the program unit. Such a combination defines a test case of the DB application.

The program unit may output SQL manipulation statements, such as SELECT, INSERT, UPDATE, and DELETE. These statements will in turn select or modify records in the target database instances. Testers can use either the direct outputs (SQL statements) to observe the test results of the program unit, or the derived outputs (database instances) to observe the test results of the DB application.

The chance of revealing a failure due to a faulty SQL statement, however, differs between these two types of observation. Since the same SQL statement can generally be applied to different database instances, depending on the particular combinations of values of a database instance, a faulty SQL data manipulation statement may be semantically intact with some database instances. Such a faulty SQL statement may select or modify the same set of records in a database instance as if it were the expected one. Detecting a failure in one database instance does not guarantee the revealing of similar failures in other database instances. Intuitively, when the failure is due to a faulty SQL statement, techniques to reveal a failure at the SQL statement level should be more cost effective than those at the database instance level.

In view of the above, among other problems in testing
DB applications [20], there are two major challenges for applying fault-based testing to such programs: (a) formulating strategies to discriminate a SQL statement from its mutants and (b) discriminating SQL statements by means of database instances.

Intuitively, conceptual data models [11] generally contain more semantic information, such as constraints, than database schemas relevant to a DB application. The latter seldom implements all the designed constraints [9]. We propose to use the information captured in conceptual data models to facilitate testers to reason about whether a given SQL statement issued by the program unit of a DB application manipulates the correct sets of data. At the level of parametric inputs and direct outputs of the program unit, there is no need to introduce any particular database instance. Testers may further construct database instances to initialize the selected differentiation scheme. In this way, the evaluation of the DB application can also be conducted at the database instance level.

The main contributions of this paper include: (i) defining semantic mutation operators based on an enhanced entity-relationship model, a type of conceptual data model; (ii) addressing challenge (a) by exploiting the semantic connections between the associated enhanced entity-relationship model and embedded SQL statements to produce SQL-oriented mutants; and (iii) alleviating challenge (b) by cross-comparing the database records manipulated by SQL statements and their mutants.

The rest of the paper is organized as follows: Section 2 summarizes and compares other research work related to the current project. Section 3 will introduce a sample application that we shall use to illustrate our proposed technique. Based on the constraints of the enhanced entity-relationship model defined in Section 4, semantic mutation operators will be defined in Section 5. Section 6 develops on Section 3, to set the scene for applying our fault-based testing technique in Section 7. Finally, concluding discussions will be given in Section 8.

2. Related work

2.1. Testing of database application programs

Test data selection strategies: Chan and Cheung [4] translated embedded SQL statements into ordinary statements to generate test cases conventionally. Kapfhammer and Soffa [15], on the other hand, proposed data-flow testing criteria to test DB applications directly. Haraty et al. [12, 13] regressed DB applications and, hence, reuse test cases by analyzing program dependencies. Robbert and Maryanski [19], tested against individual attributes, relations, and constraints in a given data model.

Database instance generation: (Semi-) automatic construction of database instances lowers the cost of testing. Chayes et al. [6, 9] constructed database instances from sample files that are produced according to category-partitioning schemes on the database schema. Their tool was also used in [10] to test web-based applications by extracting URL control graphs from applications and selecting control sequences to generate test cases. Zhang et al. [23] translated SQL statements with database schemas into constraints and applied constraint solvers to produce fault-based database instances. The generation of constraint-based database test instances was also considered by Neufeld et al. [17].

Other related work: Suárez-Cabal and Tuya [20] measured the extensiveness of coverage of the conditions in target SQL SELECT statements used to identify records in database instances. This inspires us to use located or missing records to distinguish our mutants.

2.2. Fault-based and mutation testing

Fault-based testing aims at demonstrating the absence of prescribed faults in a program [16]. According to Zhu et al. [24], there are at least three kinds of relevant adequacy criterion, namely, mutation testing, perturbation testing, and error seeding.

Mutation testing [8, 14] is an effective, though computationally expensive, fault-based software testing technique. Its core is a set of mutation operators. Each mutation operator involves a legal syntactic change of a program statement. Hence, the applications of mutation operators to a program result in a set of mutants. For strong mutation testing [8], a mutant is said to be killed by a test case if the output of the mutant differs from that of the original program. For weak mutation testing [14, 21], a mutant is killed if the program state after a mutated statement (or component) differs from that of the original program. In either case, such a test case can be used to determine whether it reveals a failure of the original program.

Morell [16] generalized mutation testing to allow the classes of alternative expressions to be infinite. He illustrated how to generate a symbolic expression that described the input of an original program and its alternative forms. The solution of a symbolic expression determines whether a set of alternative forms can be distinguished by a test case.

Perturbation testing [22] considers faults as attributes in an error space. A perturbation of a function captures the
difference between the correct function and an erroneous counterpart. This allows testers to treat faults as functional properties instead of syntactic changes of the original program.

Error seeding [3], injects artificial faults into a program. Chen et al. [7], for example, injected faults dynamically into system functions to test the exception-handling behaviors of programs.

2.3. Comparisons

This paper proposes to generate SQL-oriented mutants as a test data selection strategy. Like [19], we make use of conceptual data models and require test sets to cover the properties so defined. Unlike [19], however, we produce mutants of SQL statements to be executed by test sets. Moreover, our mutants conform to the data model, whereas previous studies [17, 23] produced fault-based database instances that aimed at violating given database constraints.

Our approach is similar to the work of Morell [16] and Zeil [22] for conventional programs. Based on the semantics of SQL statements and a given EER model (see Section 4), we construct alternative constraints to depict alternative mutants. We use the specification nature of the SQL language to treat a SQL statement as a relation. Our approach also allows testers to compare the mutants with the original SQL statements at the symbolic level.

3. Invoice payment analyzer: a sample application

Consider a conference hosting company that develops a DB application to obtain the payment status of their invoices. Invoices are partitioned as normal or canceled. Normal invoices are further partitioned as settled or outstanding, depending on whether payments from customers are required to follow. Each invoice can have invoice detail(s). Like invoices, invoice details are partitioned as canceled, settled, or outstanding. When all the details of an invoice are canceled or settled, the invoice will be treated as settled. When full payment is received in advance, a settled invoice will be directly created without invoice details. Furthermore, every outstanding invoice should have at least one outstanding invoice detail. Any canceled invoice should not have any settled or outstanding invoice detail, but may have canceled invoice detail, if any.

All the inheritance relations described above refer to total and disjoint specialization relations.

Figure 1 shows a conceptual data model (in UML notation) of invoices and their details of the sample application. The application will also be used in Sections 5.1 and 6 to illustrate our testing technique.

4. The enhanced entity-relationship model

We use the enhanced entity-relationship model (EER Model) [11] as the conceptual data model. An entity is something with properties. They are classified into entity types. A relationship is an association between two or more entities. A relationship set is a set of relationships of the same type. It can be expressed in the form of table known as a relation. Each entity type has attributes and each attribute has a value domain. Every value combination of an entity key uniquely identifies an entity of a specific type.

We further describe the standard types of constraint used in the EER model. The value of any derived attribute is worked out from other attributes. We assume that the given EER models capture the necessary derivation formulas. A weak entity type has no entity key of its own. It is identified by an identifying entity type. A participation constraint defines whether an entity must be involved in some relationship. A cardinality constraint defines the number of entities of a specified type involved in a relationship.

The generalization / specialization completeness constraint can be total or partial. Informally, when any member of a superclass must also be a member of at least one of its subclasses, then the constraint is said to be total. Otherwise, it is known as partial. Similarly, the generalization / specialization disjointness constraint can be disjoint or overlapping. The former refers to the restriction that any entity cannot also be a member of a sibling class. Otherwise, it is known as overlapping. The union type completeness constraint can be total or partial. The former means that any member in a subclass should also be entities in all its direct superclasses. Otherwise, it is known as partial.

5. Mutations according to SQL relations on EER model

SQL is a fundamental element of database application programs. In this section, we illustrate via an example
that a database schema may not capture all the constraints defined in an EER model, and then put forward a set of mutation operators based on SQL relations on the EER model.

5.1. Inadequacy of database schema constraints

Let us consider the entity types in Figure 1, in which all the specialization relations are total and disjoint. Consider a particular database schema implementation where each entity type is implemented as a separate table.

Since a canceled detail record can be related to a settled, canceled, or outstanding invoice, and since the latter invoices are in separate tables, there is no foreign key to associate canceled detail records to invoice records. We can see that the association between Invoice and Canceled Detail in Figure 1 is not captured in the above database schema.

5.2. Proposed mutation operators

We propose a set of mutation operators based on the standard types of constraint in the EER model. They cover mutations due to replacements, insertions, and deletions. Table 1 shows a list of replacement mutation operators. They are described and explained briefly via an example in this section. We shall illustrate in more detail in Section 7 how mutants due to two of the operators, namely, PTCR and GSDR, can be killed using the proposed technique. Insertion and deletion mutation operators can be treated similarly.

Consider an embedded SQL statement in Figure 2. It contains a SQL query with four join conditions over two tables, namely Invoice and InvDtl. These two tables implement the type hierarchies in Figure 1, where Invoice and Invoice Detail are the respective base types.

PTCR: The participation constraint replacement operator mutates the participate requirement of an entity type from “must-participate” to “non-participate”, or vice versa. Readers may refer to Section 7 for more details.

CDCR: The cardinality constraint replacement operator alters the cardinalities of entity types in the relation. It also forces the mutated entity type to take specific (or extreme) values within the cardinality constraints. For example, a mutant may force the relation to select entities of Invoice that are associated with more than 10 entities of Invoice Detail. This can be expressed by adding a subquery “10 < (SELECT count(*) FROM InvDtl D2 WHERE H.inv_no = D2.inv_no)”.

IWKR: The identifying/weak entity type replacement operator determines whether an expression on identifying or weak entity type(s) is involved in the relation. For an identifying entity type, IWKR will substitute it with a weak entity type. For a weak entity type, IWKR will substitute it with an identifying entity type. Suppose Invoice Detail is a weak entity type and its identifying entity type is Invoice. A mutant can be formed by replacing “InvDtl” in line s6 by “Invoice”, “sum(D.dtl_pay_amt)” in line s5 by “sum(D.pay_amt)”, “sum(Dtl_status)” in line s9 by “sum(inv_status)”, and “sum(D.dt_unit_pay_amt)” in line s10 according to Formula (1) in Section 6.2.

ATTR: The attribute replacement operator substitutes (an expression on) attribute(s) by (an expression on) other attribute(s) of a compatible type. For example, “sum(D.dtl_pay_amt)” may be replaced by “sum(D.dt_unit_pay_amt)”. This operator also includes the replacement of a composite or structured attribute by its part, and vice versa.

GSCR: The generalization/specification completeness replacement operator substitutes an expression on a partial superclass by an expression on a subclass and the negation form of the superclass. Suppose we have a subclass of normal invoices with a status of “N”, which are not settled or outstanding. The statement “H.inv_status in (‘S’, ‘O’)” on line s8 may be mutated to “H.inv_status = ‘N’ and H.inv_status not in (‘S’, ‘O’)”.

GSDR: The generalization/specification disjointness replacement operator substitutes (an expression on) sibling entity type(s) by (an expression on) other sibling entity type(s) under the same superclass. A sample mutant is to replace the set {Settled Invoice, Outstanding Invoice} by the set {Settled Invoice, Canceled Invoice}. Readers may refer to Section 7 for more details.

UTCR: The union type completeness replacement operator replaces an entity type by (an expression on) a subclass and/or superclass(es) of the subclass, such that these superclasses have the same union type constraint.
Table 1. Replacement mutation operators.

<table>
<thead>
<tr>
<th>Semantic Mutation Operator</th>
<th>Acronym</th>
<th>Description</th>
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<tbody>
<tr>
<td>Participation Constraint Replacement</td>
<td>PTCR</td>
<td>Toggle the participation requirements of entity types in the relation.</td>
</tr>
<tr>
<td>Cardinality Constraint Replacement</td>
<td>CDCR</td>
<td>Replace the cardinalities of entity types in the relation.</td>
</tr>
<tr>
<td>Identifying/Weak Entity Type Replacement</td>
<td>IWKR</td>
<td>Replace (an expression of) identifying type(s) by (an expression of) weak type(s), or vice versa.</td>
</tr>
<tr>
<td>Attribute Replacement</td>
<td>ATTR</td>
<td>Replace (an expression on) attribute(s) by (an expression on) other attribute(s) of a compatible type.</td>
</tr>
<tr>
<td>Generalization/Specialization Completeness Replacement</td>
<td>GSCR</td>
<td>Replace an expression on a partial superclass by an expression on a subclass and the negation form of the superclass.</td>
</tr>
<tr>
<td>Generalization/Specialization Disjointness Replacement</td>
<td>GSDR</td>
<td>Replace (an expression on) sibling entity type(s) by (an expression on) other sibling entity type(s) under the same superclass.</td>
</tr>
<tr>
<td>Union Type Completeness Replacement</td>
<td>UTCR</td>
<td>Replace an entity type by a subclass and/or superclasses of the subclass, such that these superclasses have the same union type constraint.</td>
</tr>
</tbody>
</table>

with the original entity type. Suppose, for example, an entity type A has three superclasses B, C, and D, and the inheritance relation between the former and the latter superclasses is a complete union type relation. The entity type B may be replaced by A, C, D, or other combinations of B, C, and D.

6. An implementation of invoice payment analyzer

The sample DB application contains a database schema (Figure 3), an EER model (Figure 1), and a program unit (Figure 2).

6.1. Database schema

Figure 3 shows the database schema for invoices and invoice details in Microsoft SQLServer 2000 syntax. The table Invoice implements all the entity types concerning invoices, including Invoice, Normal Invoice, Settled Invoice, Outstanding Invoice, and Canceled Invoice. The derived attribute of invoice amount, shown in the column inv_amt, is equivalent to (or derived from) the sum of dtl_inv_amt of the corresponding outstanding and settled invoice details. The interpretations of the columns inv_qty and pay_amt with respect to their invoice details are similar. In particular, dtl_unit_pay_amt is derived through dividing dtl_pay_amt by dtl_qty of the same row. The other columns are self-explanatory.

The table InvDtl implements all the entity types concerning invoice details, including Invoice Detail, Canceled Detail, Settled Detail, and Outstanding Detail. All the columns are self-explanatory.

There are two types of constraint in the database schema in Figure 3. The constraint “inv_no char(10) primary key” specifies that the attribute/column inv_no is an entity key of the table Invoice. Similarly, the entity key of the table InvDtl is a combination of inv_no and dtl_no. The constraint “inv_no char(10) foreign key references Invoice (inv_no)” specifies that any entity in table InvDtl should have a corresponding entity in table Invoice in such a way that the attributes inv_no on both tables must agree with each other.

The symbols “X” for canceled, “S” for settled, and “O” for outstanding are used for the columns inv_status and dtl_status. Thus, an invoice may be described as canceled, settled, or outstanding using the predicates inv_status = ‘X’, inv_status = ‘S’, or inv_status = ‘O’, respectively. The predicates for invoice details are defined similarly: dtl_status = ‘X’ for a canceled detail, dtl_status = ‘S’ for a settled detail, and dtl_status = ‘O’ for an outstanding detail.

6.2. Other EER model constraints and the sample program unit

The expected function of the program unit getPaymentReceived() calculates the total amount of payments received for those invoices that have paid at least
some cutoff amount per quantity amount. The cutoff amount is specified as an input parameter.

Suppose that, according to user requirements, the processing logic should also take into account the effect of directly settled invoice without invoice details. It should use the Invoice table to approximate the average detail amount per quantity amount as if the settled invoice details were present, thus:

\[
dtl\_unit\_pay\_amt = \frac{Invoice.pay\_amt}{Invoice.Inv\_qty}
\]  

(1)

Since this is an important requirement, we also expect this information to be captured as constraints in the EER model.

A sample implementation of the function is shown in Figure 2. Statements \(s_5\) to \(s_{11}\) in the implementation show a SQL query statement. It simply joins the invoice table and the invoice detail table via the invoice number attribute (statement \(s_7\)). It wants to select those records in either outstanding or settled status with the detail payment amount per quantity amount being not less than the cutoff amount. This sample program is faulty, however, as if the data model perceived by the developer were an oversimplified master-detail model, as shown in Figure 4, such that every invoice must have complete records of invoice details.

Figure 5 shows the SQL query statement expected for a correct implementation. Compared to the faulty version in Figure 2, it also selects those invoices without any settled invoice details. In the next section, we shall present the fault-based approach to detect this error.

![Figure 4. An oversimplified data model of invoices and invoice details.](image)

**7. Applying the fault-based approach**

This section illustrates how to derive fault-based mutants from the embedded SQL statements using the mutation operators defined in Section 5. It first analyzes SQL statements using the predicates of corresponding entity types. Consider the faulty SQL query in Figure 2 again. The SQL statements \(s_5\) to \(s_{10}\) access the tables Invoice and InvDtl. Table Invoice is mapped to all kinds of invoice entity type. Similarly, table InvDtl is mapped to all kinds of invoice detail entity type. According to the EER model in Figure 1, by including the specialization relations, there are in total two kinds of associations related to the SQL statement. They are the associations between Normal Invoice and Settled Detail, and those between Outstanding Invoice and Outstanding Detail.

There are known limitations in mutation testing, which also applies to our approach. For example, the question of determining whether a program mutant cannot be killed by any possible test case is generally undecidable. However, since SQL is a formal language and since every SQL statement is self-contained, we believe that, unlike the case of conventional mutants where we must consider all relevant program states before concluding whether a (weak) mutant can be killed, some SQL mutants can be analyzed and compared with the original SQL statement to determine whether it is an equivalent mutant. When it is indeed an equivalent mutant, there is no need to use it to synthesize a program fault for the DB application. This also reduces the number of program mutants and, hence, the cost of testing a subject program.

**7.1. Applying the GSDR mutation operator**

Let us consider the total and disjoint specialization relation of the entity type Invoice Detail. Settled Detail and Outstanding Detail are defined in the relation. Testers can apply the GSDR mutation operator. Since there are three subclasses of Invoice Detail, by exhaustion, there are seven possible non-empty subsets of \{Canceled Detail, Settled Detail, Outstanding Detail\}. One of them is defined in the relation. Hence, there are six possible mutations for this operator based on the specialization relation. Consider a substitution that replaces the original subset by \{Settled Detail, Canceled Detail\}. It will result in the following...

```sql
SELECT sum(D.dtl_pay_amt)
FROM Invoice H, InvDtl D
WHERE H.inv_no = D.inv_no
AND H.inv_status in ('S', 'O')
AND D.dtl_status in ('S', 'O')
AND D.dtl_unit_pay_amt >= (cutoff value)
UNION ALL
SELECT sum(H.pay_amt)
FROM Invoice H
WHERE H.inv_status = 'S'
AND (H.pay_amt >= H.inv_qty * (cutoff value))
AND NOT EXISTS (SELECT 1 FROM InvDtl D
WHERE D.inv_no = H.inv_no
AND D.dtl_status = 'S')
```

**Figure 5. An expected SQL query for getPaymentReceived().**
condition fragment:

\[
\begin{align*}
\text{InvDtl.inv_no} &= \text{Invoice.inv_no} \\
\text{AND Invoice.inv_status IN ('S', 'O')} \\
\text{AND InvDtl.dtl_status IN ('S', 'X')} \\
\text{AND InvDtl.dtl_unit_pay_amt} &= \langle \text{cutoff value} \rangle
\end{align*}
\] (2)

We note the following: When testers apply conventional, syntactic mutation operators, such as “replace a constant by another constant”, they can also obtain a mutant similar to that in equation (2). For example, by replacing the constant symbol “0” by the symbol “X” in statement \(s_9\) of the faulty program, testers can generate the same mutant. There is, however, a difference between such syntactic mutants and our semantic mutants. Our approach replaces the sets of logical subclasses of the superclass in a specialization hierarchy. For example, we will generate a mutant that replaces “(‘S’, ‘O’)” by “(‘X’)”. An application of the conventional mutation operator cannot produce such a change.

To unify the identifiers of equation 2 with those of Figure 2, testers substitute the table identifiers Invoice and InvDtl in equation 2 by the instance identifiers “H” and “D”, respectively. They then substitute the unified equation 2 into the SQL statements \(s_7\)–\(s_9\) of Figure 2 to produce a mutant \(M_1\). The embedded SQL part of \(M_1\) will be:

```
SELECT sum(D.dtl_pay_amt) \\
FROM Invoice H, InvDtl D \\
WHERE H.inv_no = D.inv_no \\
AND H.inv_status in ('S', 'O') \\
AND D.dtl_status in ('S', 'X') \\
AND D.dtl_unit_pay_amt >= \langle \text{cutoff value} \rangle
```

7.2. Applying the PTCR mutation operator

Let us illustrate the application of another mutation operator. Consider the relation between entity types Normal Invoice and Settled Detail. We apply the PTCR mutation operator. According to Figure 1, any entity of Settled Detail must be associated with one entity of Normal Invoice. According to the EER model, it is not possible to have a settled invoice detail without a corresponding invoice. Hence, the result of applying the mutation operator that toggles the participation requirement of Normal Invoice from “must-participate” to “non-participate” cannot result in a legitimate mutant.

On the other hand, each Normal Invoice may or may not be associated with any Settled Detail. Applying the mutation operator, it will generate a candidate fragment of a mutant that requires non-participation of Settled Detail.

```
Invoice.inv_status IN ('S', 'O') \\
AND NOT EXISTS (SELECT 1 FROM InvDtl D1 \\
WHERE D1.inv_no = Invoice.inv_no \\
AND D1.dtl_status = 'S') \\
AND InvDtl.dtl_unit_pay_amt >= \langle \text{cutoff value} \rangle
```

Here, “EXISTS (SELECT 1 ... WHERE ...)” is the standard SQL technique for checking the existence of an entity that fulfills a specified condition.

Thus, a second mutant \(M_2\) can be formed using equation (3) instead of equation (2). However, the condition “InvDtl.dtl_unit_pay_amt >= \langle \text{cutoff value} \rangle” on the last line of equation (3) uses a column of table InvDtl, which does not exist in this case. Testers must apply equation (1) in Section 6.2 to derive the value of dtl_unit_pay_amt instead. Moreover, since the data types of the relevant columns Invoice.pay_amt, Invoice.inv_qty, and dtl_unit_pay_amt are integers, the formulation of the mutant uses “Invoice.pay_amt >= Invoice.inv_qty * \langle \text{cutoff value} \rangle” instead of “Invoice.pay_amt / Invoice.inv_qty >= \langle \text{cutoff value} \rangle.”

Furthermore, according to the EER model, the derived attribute Invoice.pay_amt is semantically equivalent to the sum of InvDtl.dtl_unit_pay_amt attributes of relevant invoices. The sum of the former attribute readily substitutes the sum of the latter attributes (as far as each entity type in the relation is concerned). The other parts of the mutant \(M_2\) follow a similar synthesis approach as above. Thus, the embedded SQL part of \(M_2\) will be:

```
SELECT sum(H.pay_amt) \\
FROM Invoice H \\
WHERE H.inv_status IN ('S', 'O') \\
AND NOT EXISTS (SELECT 1 FROM InvDtl D1 \\
WHERE D1.inv_no = H.inv_no \\
AND D1.dtl_status = 'S') \\
AND (H.pay_amt >= H.inv_qty * \langle \text{cutoff value} \rangle)
```

7.3. Weak mutation testing

Suppose that testers are interested in weak mutation testing [14, 21]. Informally, a weak mutant is said to be killed if the state of the mutant immediately following the execution of the mutated statement (or component) is not identical to that of the original program. Since we are interested in using SQL statements to distinguish different sets of data model constraints, we interpret that, for the same entity type applicable to both the original program and a mutant, if they affect different sets of records, the mutant is said to be killed. We elaborate the concept in more detail as follows:

In general, a program unit may involve a number of databases and hence a number of database schemas. Let \(C\) be a program unit with input domain \(D\) for its input parameters and \(\Sigma = \langle \sigma_1, \sigma_2, \ldots, \sigma_n \rangle\) be a tuple of database schemas. Following the description in Section 1, a DB application \(P\) is a tuple \(\langle C, \Sigma \rangle\) in which each database schema \(\sigma_i\) in \(\Sigma\) is associated with an EER model \(E_i\). A database instance is a concrete state of a database schema. The current program state of the DB application is the current program state of its program unit \(C\) with the current
Figure 6. Sample instances of the invoice and invoice detail tables.

(a) Invoice Table

<table>
<thead>
<tr>
<th>inv_no</th>
<th>inv_dt</th>
<th>inv_stl_dt</th>
<th>inv_status</th>
<th>inv_amt</th>
<th>inv_qty</th>
<th>pay_amt</th>
<th>cust_no</th>
<th>order_no</th>
</tr>
</thead>
<tbody>
<tr>
<td>419</td>
<td>10/22/2004</td>
<td>12/31/2004</td>
<td>S</td>
<td>360</td>
<td>1</td>
<td>360</td>
<td>schoeung</td>
<td>qsic04-01</td>
</tr>
<tr>
<td>3554</td>
<td>10/18/2005</td>
<td>12/02/2005</td>
<td>S</td>
<td>360</td>
<td>1</td>
<td>360</td>
<td>wkchan</td>
<td>qsic05-02</td>
</tr>
<tr>
<td>304</td>
<td>09/22/2003</td>
<td>09/22/2003</td>
<td>S</td>
<td>360</td>
<td>1</td>
<td>360</td>
<td>thise</td>
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(b) InvDtl Table

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database instances whose schemas are defined in \( P \). For example, the program unit \texttt{getPaymentReceived()} with the database schema in Figure 3 constitutes the sample DB application for illustrating our unit testing technique. The parametric input domain for \texttt{getPaymentReceived()} is the set of valid integers.

By a similar token, a test case for \( P \) is a tuple \( \langle T, \Psi \rangle \) in which \( x \) is an element in domain \( D \) and \( \Psi = (\psi_1, \psi_2, \ldots, \psi_n) \) is a sequence of database instances such that each \( \psi_i \) corresponds to a state of the database schema \( \Sigma_i \) of the DB application. For example, the database instance in Figure 6 with the input parameter \texttt{cutoff} = 200 forms a test case for our sample DB application. The direct output of the test case from the program unit consists of SQL statements, which will be executed by a database system with the database instances to produce derived output, such as updated records in the database instances.

Let \( S \) be a SQL statement issued by the program unit \( C \) associated with the database schemas \( \Sigma \). Let \( \Sigma_i \) (such as \( \Sigma_2 \) in our example) be a mutated SQL statement of \( S \) after a mutation operator has been applied to \( S \) and the EER model \( E_i \). Replacing \( S \) in \( C \) by \( \Sigma_i \) produces a mutant \( \Sigma_i \) of the program unit \( C \). The tuple \( \langle C, \Sigma_i \rangle \) forms a mutant of the DB application \( P = \langle C, \Sigma \rangle \).²

We note that a sequence of database instances, say \( \Psi' \), is part of a state of the DB application under test and, hence, we distinguish mutants from the original program using the intermediate state at the point where the SQL statement is issued from the program unit. We may consider our approach as a type of weak mutation test data selection strategy.

Let \( f(\cdot) \) be a function that accepts a SQL statement \( S \), a sequence of database schemas, and a sequence of their corresponding database instances to return a set of records manipulated by \( S \), such that each record is annotated with the relevant SQL statements affecting it. Let \( S(P, T) \) denote an instance of \( S \) when the DB application \( P \) accepts a test case \( T \). A mutant \( \Sigma_i \) of \( S \) is said to be killed if \( f(S(P, T), \Sigma, \Psi') \) and \( f(S_i(P, T), \Sigma, \Psi') \) differ. The mutant \( \Sigma_i \) of the program unit \( C \) is said to be killed if the SQL-oriented mutant \( \Sigma_i \) is killed. A mutant \( \langle \Sigma_i, \Sigma \rangle \) of DB application \( P = \langle C, \Sigma \rangle \) is said to be killed if the mutant \( \Sigma_i \) is killed.

Let us continue our example to distinguish mutants from an original SQL statement at the database instance level. Consider the database instances shown in Figure 6 with the input parameter \texttt{cutoff} = 200. The faulty sample program \texttt{getPaymentReceived()} will select settled invoices with invoice numbers 419 and 3554. On the other hand, the mutant \( M_2 \) will select the settled invoice with invoice number 304. Since the records selected from the entity type Settled Invoice are not identical, the mutant is killed. This missing settled invoice reveals that the faulty program is corrected, by substituting the
expected SQL query in Figure 5 into the relevant part on lines $s_5 - s_{10}$ of Figure 2. Since the correct statement is a union query, given an input $\textit{cutoff} = 200$ for the database instance shown in Figure 6, it will return two rows, one from each sub-query. The two returned rows are 1140 (based on the 1st, 2nd, and 6th rows of the $\text{InvDtl}$ table) and 360 (based on the 2nd row of the $\text{Invoice}$ table). As the order of the record set is not specified in the SQL statement, it can be the row of 1140 followed by that of 360, or vice versa. We discover another fault on line $s_{13}$ of Figure 2. It should be a $\text{while}$ statement instead of an $\text{if}$ statement; otherwise, it cannot process the results from both sub-queries in the same run. Suppose the first row in the record set is 1140. Similarly to the description in the above paragraph, it will miss the row due to the second sub-query. In this case, the failure is detected by mutant $M_2$. On the other hand, suppose the first row in the record set is 360. The faulty program will miss to report those invoices with invoice details. In this situation, the failure is detected by mutant $M_1$ instead.

8. Concluding discussions

Testing database application programs with SQL as the tools to access and modify database instances is gaining an increasing amount of research attention. This paper proposes a novel fault-based testing approach to address the special characteristics and challenges for testing DB applications at the unit level.

The notion of mutating statements for mutation testing of a program has a long history. It should not be difficult to apply conventional mutation operators such as replacing a logical connector by another syntactically legal logical operator (say, “Invoice.inv_no = $\text{InvDtl}.inv_no$” by “Invoice.inv_no $\neq$ $\text{InvDtl}.inv_no$”) to produce SQL-related mutants. Hence, we assume that such mutation operators can be defined without problem.

Furthermore, non-database-related statements can be regarded as conventional statements of the programming language in question. They can be tested using techniques applicable to that programming language. For instance, by ignoring embedded SQL statements, testers can apply predicate testing to test Boolean expressions in a database application program as if it were a conventional program. Similarly, they can also apply conventional mutation testing to test non-SQL statements.

We are currently doing experimental studies to evaluate the effectiveness of our approach. Our initial investigation is conducted on the sample application presented in this paper. We mechanically generate 35 non-equivalent mutants for this subject program, where a mutant is said to be non-equivalent if its outcome is different from that of the original program. For the purpose of control, we also apply conventional mutation operators to mechanically generate 34 conventional non-equivalent mutants. On average, it needs 4 test cases to kill all the semantic mutants, and 6 test cases to kill all the conventional mutants. The case study shows that our approach detects 89.5% of faulty (but not mutated) versions of the subject program, whose faults are not limited to embedded SQL statements. On the other hand, the conventional approach detects 78.9%. We also find that, for the two mutation operators explained in this paper, PTCR is more effective than GSOR, which, in turn, is more effective than conventional operators. We must emphasize, however, that the preliminary results are based on a limited amount of data. We shall report our major findings when we have accumulated more experience.

We focus, therefore, on semantic mutants of embedded SQL statements based on the semantics of the conceptual data model. We employ the standard types of constraint of the EER model to formulate mutation operators. Generally speaking, semantic information, which is invaluable to software testers, is not as extensively available in database schemas as in conceptual data models. For various reasons such as performance [9], some desirable constraints are not implemented in the database schemas associated with the programs under test. To the best of our knowledge, this work is the first of its kind to consider semantic relationships defined in conceptual data models to generate mutants for fault-based testing of DB applications.

We exploit the semantic information captured from the conceptual data model, such as the relationships between the stored and derived attributes, and combine them with embedded SQL statements to produce SQL-oriented mutants. Specifically, we analyze the SQL statements to be mutated, and then find out the affected entity types, relations, and constraints. Based on the analysis results, mutation operators are applied to the SQL statements to produce mutants. Without such semantic transformation, some useful mutants, such as $M_2$ of the sample application, are difficult to formulate.

In view of the preference by testers to check database instances of a DB application instead of checking SQL data manipulation statements in its program unit, we use database instances plus parametric inputs and derived outputs to conduct fault-based testing to kill SQL-oriented mutants at the database instance level.

We have illustrated our proposal through a SQL query example. However, subquery and join conditions of SQL data manipulation statements, including $\text{INSERT}$, $\text{UPDATE}$, and $\text{DELETE}$ statements, share a lot of similarities with query statements. The discussions in this paper can be applied to these language constructs. Nevertheless, more thorough investigations are recommended.

We shall further construct and evaluate formal models to represent legal constraints and business logics for
testing purpose. Since we have not yet come up with a satisfactory technique to derive non-equivalent SQL-related mutants automatically, we shall seriously address this issue. We believe that, since SQL is a language with formal semantics, it should allow us to analyze and create non-equivalent mutants, rather than generating a large class of equivalent mutants. We shall conduct experiments to determine the fault-detection capability of our proposal. Testing DB applications with data definition statements will also be an area to be examined. The issue of automatic test oracles will also be addressed. Finally, we shall construct a prototype tool to implement our approach.

Acknowledgement

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References