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Anchor Point Indexing in Web Document Retrieval

Ben Kao, Joseph Lee, Chi-Yuen Ng, and David Cheung

Abstract—Traditional World Wide Web search engines, such as AltaVista.com, index and recommend individual Web pages to assist users in locating relevant documents. As the Web grows, however, the number of matching pages increases at a tremendous rate. Users are often overwhelmed by the large answer set recommended by the search engines. Also, if a matching document is a hypertext, the document structure is destroyed and the individual pages that compose the document are returned instead. The logical starting point of the hypodocument is thus hidden among the large basket of matching pages. Users need to spend a lot of effort browsing through the pages to locate the starting point, a very time consuming process. This paper studies the anchor point indexing problem. The set of anchor points of a given user query is a small set of key pages from which the larger set of documents that are relevant to the query can be easily reached. The use of anchor points help solve the problems of huge answer set and low precision suffered by most search engines by considering the hyperlink structures of the relevant documents, and by providing a summary view of the result set.

Index Terms—Anchor points, hypertext, information retrieval, indexing, World Wide Web.

I. INTRODUCTION

The Internet enables a computer user to be connected to virtually endless numbers of sites on the network. The World Wide Web (WWW) uses the Internet to transmit hypermedia documents between computer users located around the world. Large amounts of interesting and valuable information have been made available on the Web for retrieval. In order to fully utilize the power of the WWW as an information source, it is essential to develop intelligent software systems on top of the Web to assist users in retrieving relevant documents.

Search engines are the most popular tools that people use to locate information on the Web. A search engine works by traversing the Web via the hyperlinks that connect the Web pages, performing text analysis on the pages it has encountered, and indexing the pages based on the keywords they contain [19]. A user seeking information from the Web would formulate his information goal in terms of a few keywords composing a query. A search engine, on receiving a query, would match the query against its document index. All of the pages that match the user query will be selected into an answer set and be ranked according to how relevant the pages are with respect to the query. Relevancy here is usually based on the number of matching keywords that a page contains, with the “positions” of the matches taken into account. (For example, a matching keyword that appears in the title of a page is considered more relevant than an occurrence in the text body.)

Although search engines have been proven in practical use as indispensable tools for Web information retrieval, they suffer from a number of drawbacks [7], [12]. The simple keyword matching criteria very often do not provide queries with the expressive power to distinguish the target documents from the millions of pages available on the Web. This results in large answer sets and thus low precision. Users are often overloaded by the myriad of pages returned, seriously weakening the usability and the effectiveness of the search engines. Also, if the target document is a hypertext that consists of a number of Web pages being connected by hyperlinks, the document structure is destroyed. Individual pages that compose the document are scrambled and are returned out of order. The logical starting page of the hypodocument is thus hidden among the large basket of matching pages. The purpose of this paper is to study the low precision problem of traditional search engines and suggest solutions to relieve users from being overloaded by the large number of recommended pages. In particular, we introduce the concept of anchor points which consider the hyperlink structures of the Web pages when processing queries to achieve the following goals:

• improve the ranking of matching documents;
• identify good starting points (anchors) that allow efficient and orderly accesses to pages that belong to the same logical hypertext documents;
• reduce the size of the answer set by recommending only those pages that are representative of the ones which match the query and which belong to the same logical clusters.

The balance of this paper is organized as follows. In Section II we discuss some common deficiencies of traditional search engines. In particular, we study the large-size, low-precision answer set problem, and the aftermath of disregarding the hyperlink structures of documents when making a recommendation. In Section III we mention some related works. In Section IV we propose the idea of recommending anchor points instead of individual matching pages. Loosely speaking, given a query, the anchor points constitute a small set of key pages from which the set of matching pages can be accessed easily and in a logical order. The idea is that by presenting to the users a restricted set of “representative” pages, users are able to perform a fast first-level screening of the pages to single out a selected set of good candidates before examining each one of them. Also, if some of the matching pages belong to the same logical hypertext document, the anchor point that connects to them provide a good logical starting point for browsing. We propose a model for matching a query to a set of anchor points. To demonstrate the effectiveness of our approach, we implemented a prototype system for indexing anchor points and evaluated its performance through experiments. In Section V we describe our experiments and show the results. In Section VI we discuss the various design
II. SHORTCOMINGS OF SEARCH ENGINES

In this section we identify and discuss four sources of ineffectiveness of traditional search engines. These include

- large answer set;
- low precision;
- unable to preserve the hypertext structures of matching hyperdocuments;
- ineffective for general-concept queries.

A. Large Answer Set

Most search engines boast of their services mentioning their extensive coverage of the Web. AltaVista.com, for example, maintains 200+ gigabytes of index data covering more than 50 million sites. Empowered by high performance workstations, large storage servers, and sophisticated indexing techniques, these search engines handle user queries with reasonable response times. The quality of the responses, however, are sometimes questionable. The large number of pages indexed plus relatively loose matching criteria often result in large answer sets (sets of matching pages). Users are overloaded with the vast amounts of information returned from the search engines. Even though search engines rank the pages in the answer set by guessing how relevant they are with respect to the queries, the ranking systems are far from perfect given the limited expressive power of the keyword-based query interfaces. Browsing through the numerous pages returned is a tiring and time consuming process. Users do not usually have the patience to toil through more than the first 30 hits returned by a search engine. Table I illustrates this problem by showing the results obtained from querying four popular search engines with some sample queries.

From the table we see that the answer sets are huge. If it takes a person 5 s to decide whether a page is relevant or not, screening through 100,000 recommendations takes about six man-days. Of course, one would argue that the screening would stop as soon as one good recommendation is found. Still, as suggested by Table I, the first relevant page may not be found until a couple dozens pages have been examined, many more if one is unlucky. Also, the first relevant page may not be the best page that can be found in the answer set. More screening is required if one would like to compare relevant hits looking for a better match.

Besides illustrating the large answer set problem, Table I also gives us a hint on how to avoid overwhelming the users with the numerous recommendations. The last column of the table suggests that the large number of pages can be grouped into a small number of logical clusters. Now, if a search engine could be smart enough to identify the clusters and recommend to the users only one representative page per cluster, the users would be able to screen through the suggested list much more efficiently. As an example, any one of the pages that is returned due to the query “nba scoreboard november 19 1997” would lead the user to the sports site’s Web structure containing all the game summaries. If these are not the pages the user is looking for, all of them could be skipped by one inspection of a single page.

<table>
<thead>
<tr>
<th>Goal</th>
<th>Query</th>
<th>Search Engine</th>
<th>no. of hits</th>
<th>no. of relevant pages in the first 30 hits</th>
<th>Rank of 1st relevant hit</th>
<th>no. of logical clusters in the first 30 hits</th>
</tr>
</thead>
<tbody>
<tr>
<td>Find the site of Microsoft Windows</td>
<td>microsoft windows</td>
<td>Alta Vista</td>
<td>1,675,241</td>
<td>3</td>
<td>10th</td>
<td>4</td>
</tr>
<tr>
<td>Find RIFF specification</td>
<td>riff specification</td>
<td>Lycos</td>
<td>unknown</td>
<td>1</td>
<td>12th</td>
<td>26</td>
</tr>
<tr>
<td>Find NBA scoreboard</td>
<td>nba scoreboard</td>
<td>Excite</td>
<td>71,118</td>
<td>27</td>
<td>3rd</td>
<td>2</td>
</tr>
<tr>
<td>Find general information about cricket</td>
<td>cricket</td>
<td>Infoseek</td>
<td>40,990</td>
<td>1</td>
<td>22nd</td>
<td>20</td>
</tr>
</tbody>
</table>

1 A page which simply contains the keywords as specified in the query but does not satisfy the goal is not considered a relevant hit.
Interestingly, a “representative page” needs not be one that is highly ranked by a traditional search engine. For example, one could imagine that the game summary pages can all be reached by an index page. If the target of the user’s goal is some of the game summary pages (e.g., all those games played in November), the index page might as well be the best starting point (an anchor) that the user can have. However, the index page may not contain the keywords with high enough occurrence frequencies for it to score high under the ranking systems of traditional search engines (e.g., the keyword “November” may occur only once in the index page, among others). Ranking anchor points is thus an interesting and challenging problem.

We will discuss how anchor points could be found given a user query in Section IV.

B. Low Precision

In addition to “information overload,” low precision of the answer sets is sometimes another concern of the effectiveness of search engines. Previous studies have conducted experiments showing that relevant pages are often interspersed with irrelevant ones in the ranked query outputs [13]. The implication is that users cannot afford to examine only the first few, or any small subset, of the answer set. Table I illustrates this problem by showing the number of pages among the first 30 hits that are relevant to a search goal. We see that, for some queries, the numbers are less than honorable.

The problem of low precision has been documented in a number of previous studies [7], [12]. We will mention some of the references in Section III. While there are many factors that lead to low precision results, we remark that under the simple model of matching Web pages against user queries based solely on word statistics, the current approach taken by most search engines might already be representing the best effort. We believe that working on a better user interface that assists the users to better express their search goals should be a more fruitful option in precision improvement. One example system developed by The University of Arizona using the idea of concept space [4], [5] has demonstrated that user queries can be semi-automatically enhanced to improve the precision of the answer sets. (Excite.com also takes a similar approach.)

In this paper, we do not attempt to solve the low precision problem. However, we identify and study one important source of the problem and discuss how the concept of anchor points could help tackle it.

The biggest attraction of the Web is that it provides an on-line source of information being structured as a huge network of Web pages, each contains a certain piece of interesting knowledge. Users are free to access and navigate the Web via hyperlinks connecting related information units. Hypertext is especially useful for “on-line presentation of large amounts of loosely structured information such as on-line documentation or computer-aided learning” [20]. It is therefore a useful concept that Web document authors like to adopt. As an example, the Usenet Hypertext Frequently Asked Questions Archive stores FAQs of different subjects in hierarchical hypertext structures. A FAQ is usually broken up into a number of parts, each part containing a number of questions and their answers. Fig. 1 shows a logical hypertext structure of a FAQ document.

To the author of the FAQ, the whole structure constitutes a single document, and the part index represents the logical starting point of the document. Unfortunately, traditional search engines ignore the structural information embedded in the hyperlinks and index the pages separately. If a user queries an engine with the keywords and, none of the pages matches all the keywords. These pages would be ranked very lowly by the engines even though the hyperdocument as a whole might provide all one needs to know about the subjects. On the other hand, if the author puts everything in one single Web page, the document would match the user query very well. This reveals
a drawback of the ranking mechanism of traditional search engines, namely, it works against documents that are presented in hypertext structures.

To deal with this ranking misjudgment, a search engine should recognize the fact that logically the pages belong to a hyperdocument (or a cluster) and that the document is relevant to the subjects that occur in the pages \((A, B, C)\) in our example. That is to say, the search engine should be able to 1) match queries against hypertext structures and 2) return an entry point through which the constituent pages can be easily accessed. As we have alluded to earlier, an anchor point is a representative page of a cluster of pages that provides a good starting point and that allows efficient and orderly accesses to pages that belong to the same logical cluster, the idea of anchor points meets our second requirement. To satisfy the first requirement, we need to associate a page with not only the keywords it contains, but also the keywords that occur in the cluster the page belongs to. (With our FAQ example, the search engine should associate the keywords \(A, B, C\) with the part index page because those keywords occur in the cluster and the pages containing them can be easily accessed through the part index.) In Section IV, we will describe how this type of keyword associations are derived and how the associations are used to efficiently locate anchor points given a user query.

C. Destroying the Hypertext Structures of Matching Hyperdocuments

Another inadequacy of traditional search engines again results from not preserving the hypertext structures of matching hyperdocuments when making recommendations. Even if an engine could match a query with the pages of a hyperdocument, the hypertext structure is flattened and the individual pages are returned out of order. As an example, we submitted the query “C80 faq” to AltaVista.com looking for information about a DSP chip named C80. AltaVista.com successfully located a forum with hundreds of postings about the chip. The postings were organized as a hypertext with an index page pointing to the numerous postings, ordered by date. Each posting was contained in a separate Web page. Although the pages returned by the search engine matched the query goal, the postings listed in the answer set were totally out of order, and the index page was not listed in the first 100 hits returned. A user thus needs to reconstruct the logical reading path from the disorganized answer set. A better approach would be to recognize that the pages belong to the same cluster and to return a logical starting point (such as the index page). The concept of anchor point again applies here. We will demonstrate how anchor points help ameliorate the problem in Section V.

D. General Concept Queries

Finally, while traditional search engines perform quite well for “specific” and “precise” queries (e.g., “find me the solution for solving the Rubik’s cube”), they are not particularly effective in serving general concept queries. As an example, someone may want to know about the sport cricket. Ideally, a site such as CricInfo that is dedicated to the sport would be a perfect match. Unfortunately, the query “cricket” is too general for traditional search engines with their simple keyword-matching systems. The result is that any Web page that contains the keyword “cricket” matches the query, be it the start page of CricInfo, a page written by a fifth grader on his favorite sports, or a page reporting the scores of an international cricket tournament.

As the Web develops, we see more and more information sources that are dedicated to specific topics of interests. There are sites for tennis, sites for salmon, and even sites for Big Foot. If a user is looking for some general information about a topic, chances are that a site exists on the Web that is specialized on that topic. Recommending Web sites instead of individual Web pages becomes more meaningful to this type of general concept queries.

Currently, the best way to look for specialized information sources is to use a directory service, such as Yahoo.com. The down sides of this approach are that subject categorization is done by hand and that the sites need to be suggested.

As an alternative, one could imagine that the Web pages of a specialized site circle around a major subject, and thus could be considered as parts of a very big cluster or a hypertext document rooted at the site’s home page. Also, as we have discussed, an anchor point is a representative page of a cluster and that it is associated with the keywords found in the cluster. It is reasonable to argue that a specialized site’s home page is a good anchor point that matches the general concept query (on the site’s specialized subject). The concept of anchor points is thus useful in recommending Web sites and answering general concept queries.

III. RELATED WORKS

The goal of our study is to improve the effectiveness of information retrieval on the WWW. In particular, we focus on improving the ranking system of search engines dealing with hypertext documents, cutting down on the size of answer sets, supporting general concept queries, and identifying good starting points for efficient and orderly accesses to hypertext documents. The inadequacies of traditional search engines with respect to some of the above issues are mentioned in [7], [12].

Some research studies take another approach to matching users to information on the Web. Instead of indexing the whole Web like traditional search engines do (a server-based approach), these studies work on the design of intelligent client-based Web tools that “learn” about a user’s interests and guide the user in traversing the Web, zeroing on the target documents. Here, we briefly mention two such systems. Interested readers are referred to [1]–[3], [6], [16], [17], for more details. De Bra and Post [3], developed a client-based search engine. The system allows a user to specify a search goal in three different ways:

1) by keywords—documents are ranked according to the occurrences of the user-supplied keywords;
2) by regular expression—documents are ranked according to the number of matches of the user-supplied patterns;
3) by external filters—a user can provide a program that assigns scores to documents.
The search engine explores the Web using a fish search algorithm with relevant documents ranked according to the scoring system the user specified.

Letizia [17] is an intelligent agent that works with a conventional Web browser. It tracks the user’s browsing behavior and tries to infer the user’s goals. While the user is reading a page, Letizia conducts a resource-limited search based on the goals it deduced. Relevant pages found during the search will be recommended to the user upon request. The goal of Letizia is to automatically perform some of the Web exploration on behalf of the user to anticipate future page accesses.

In [16], an intelligent system is designed which tracks users’ browsing behavior to deduce sets of keywords (called term vectors). These term vectors are used to describe the information that the users are interested. The paper proposes an architecture of an intelligent system that integrates various tools to analyze the users’ accessing behavior and automatically brings in relevant documents for the users. The system consists of two learning agents, one for discovering users’ topics of interest, and another for discovering the topics covered by information sources. The system then matches users to Web sites based on the topics accordingly.

The expressive power of conventional search engine query interfaces is relatively weak when restricted to keyword-based search. The deficiencies are documented in [7]. One of the many problems is that a concept under interest may be described by many terms. For example, someone looking for information about “AIDS” would miss documents that mention only “HIV.” One approach to this problem is to construct a concept space graph representing the important terms and their weighted relationships. This concept space graph is then used to augment keyword queries by complementing user supplied keywords with their strongly associated terms [4]. Concept space construction involves frequency analysis and cluster analysis [5]. However, these analyzes are very computationally expensive and thus are not suitable for a highly dynamic Web environment.

### IV. Anchor Points

In Section II, we explained how recommending anchor points can improve the effectiveness of search engines, particularly in dealing with hypertext documents. To reiterate, given a user query and subsequently a set of matching Web pages which form a number of clusters, we propose that the system should recommend, instead of all the matching pages, a set of anchors (possibly one for each cluster) such that

1) an anchor is a representative page of a cluster (i.e., by inspecting the anchor, a user can easily deduce what the pages in the corresponding cluster are about);
2) an anchor provides efficient and orderly accesses to the pages in the corresponding cluster.

In our discussion so far, we have only presented the idea of anchor points fairly informally. For example, we have not defined what we mean by a cluster, what we mean by a page being a representative one of a cluster, or what we mean by efficient accesses to a cluster of pages. The reason is that there are, in fact, many different ways one could interpret the terms. (For example, efficient accesses of pages may be defined in terms of the number of network requests, the number of mouse clicks, or the amount of memory cache needed.) In order to avoid restricting ourselves to one interpretation, we focused our previous discussion on the general concept and the motivation of the problem. In this section, we present one formal definition of anchor points. We show how to process queries in anchor point recommendation. We will demonstrate the effectiveness of our approach in solving the commonly occurring problems in traditional search engines (Section II) via experiments in Section V.

#### A. Definitions

We define the distance from a Web page $A$ to a Web page $B$, denoted by $D(A, B)$, to be the minimum number of hyperlinks that need to be traversed to reach page $B$ starting from page $A$. If page $B$ is unreachable from $A$, we have $D(A, B) = \infty$. We define the $k$-neighborhood of a Web page $A$, denoted by $N_k(A)$, to be the set of all the pages that are within distance $k$ or less from $A$. Fig. 2 illustrates these terms. For example, the distance from page $A$ to page $J$ is 3 ($A \rightarrow E \rightarrow D \rightarrow J$) while the distance from page $J$ to $A$ is 4 ($J \rightarrow E \rightarrow D \rightarrow C \rightarrow A$). The 2-neighborhood of page $A$ is the set of all the pages encircled by the dotted lines. With our notations, we have $D(A, J) = 3$, $D(J, A) = 4$, and $N_2(A) = \{A, B, C, D, E, F, G, H\}$.

We assume a scoring function $f$ exists such that given a keyword $a$ and a Web page $X$, $f(X, a)$ measures the extent that page $X$ matches the keyword $a$. We call the value of this function the score of page $X$ with respect to $a$. There are many choices for such a function. One simple example would be

$$f(X, a) = \begin{cases} 0, & \text{if } X \text{ does not contain } a \\ 1, & \text{if } X \text{ contains } a. \end{cases}$$

Alternatively, $f(X, a)$ could be the normalized occurrence frequency of $a$ in $X$, as is done in term frequency inverse document frequency (TFIDF) [15]. A third example would be the probabilistic model as suggested in [18] in which the authors proposed a function that estimates the probability that a document $X$ is relevant to a keyword $a$. 

![Fig. 2. Distance and neighborhood.](image-url)
Recall that our goal is to recommend a page to a user starting from which he is likely to find relevant pages via simple navigation. Here, let us assume that by simple navigation, we mean that the user does not need to traverse more than \( k \) links away from the suggested starting point. In order to measure how well potentially a page \( X \) can lead a user to pages that match a keyword \( a \), we define a potential function \( P_k(X, a) \) as follows:
\[
P_k(X, a) = \sum_{Y \in N_k(X)} f(Y, a) \times \alpha^{D(Y,X)}
\]
where \( \alpha \) is a constant parameter between 0 and 1.\(^2\) In other words, the potential function of a page \( X \) with respect to a keyword \( a \) gives the sum of all the scores of the pages in \( X \)'s \( k \)-neighborhood, with each page’s contribution to the score scaled down exponentially with respect to its distance from page \( X \). The constant \( \alpha \) controls the pace of the scale-down (the smaller the value, the faster the pace).

Depending on the semantics of the function \( f \), different quantitive interpretations can be associated with the potential function. For example, if \( f(Y, a) \) represents the amount of information that a page \( Y \) contains about the keyword \( a \), and \( \alpha \) is the probability that a user follows a hyperlink, then \( \alpha^{D(Y,X)} \) gives the probability that page \( Y \) is visited if a user starts at page \( X \), and \( P_k(X, a) \) gives the expected amount of information that a user would learn about keyword \( a \) if he starts from page \( X \) (assuming that the user does not take more than \( k \) hops away from \( X \)). As another example, if \( f(Y, a) \) measures the probability that page \( Y \) is relevant to keyword \( a \), then \( f(Y, a)\alpha^{D(Y,X)} \) is the probability that a user starting from page \( X \) would get a relevant page in \( Y \) about the keyword \( a \). Hence, \( P_k(X, a) \) is equal to the expected number of pages that are relevant to \( a \) that a user would visit given that he starts at page \( X \). In any case, intuitively, \( P_k(X, a) \) is an indicator of how much information about \( a \) one can get starting from page \( X \). For the purpose of discussion, we will use the second interpretation of \( f \) (i.e., \( f(Y, a) \) measures the probability that page \( Y \) is relevant to \( a \)) for the rest of this section.

### B. Queries

Given a query \( Q \) and a page \( X \), our approach to evaluate whether \( X \) is a good anchor point for \( Q \) is by estimating the number of relevant documents (w.r.t. \( Q \)) that are within distance \( k \) from \( X \) and that a user will visit if he starts from \( X \). We call this estimate the potential of \( X \) with respect to \( Q \) (\( \text{Potential}(X, Q) \)). Anchor points are ranked based on their potentials. In this subsection we show how anchor point potentials are computed.

As we have discussed in Section IV-A, if \( f(Y, a) \) is a measure of the probability that page \( Y \) is relevant to a keyword \( a \), then \( P_k(X, a) \) is the expected number of relevant pages (w.r.t. \( a \)) in \( X \)'s \( k \)-neighborhood that a user would visit if he starts from \( X \). So, for a single-keyword query \( Q = a \), \( \text{Potential}(X, Q) \) is simply \( P_k(X, a) \), as is given in (1).

As an example, Fig. 1 shows the hypertext structure of a hypothetical FAQ document. If \( \alpha = 0.8, k = 3 \), and the scoring function \( f(X, a) \) simply returns 1 if \( X \) contains \( a \); 0 otherwise, then the tuple beside each page with respect to the page in the Figure shows the values of Potential with respect to the keywords \( A, B, C \), respectively. For example, we have
\[
\begin{align*}
\text{Potential}(\text{"part I"}, A) &= P_k(\text{"part I"}, A) = 2.4 \\
\text{Potential}(\text{"part I"}, B) &= P_k(\text{"part I"}, B) = 2.752 \\
\text{Potential}(\text{"part I"}, C) &= P_k(\text{"part I"}, C) = 0.512.
\end{align*}
\]

In this example, the anchor points for keywords \( A, B, \) and \( C \) are “part index”, “part index”, and “part III.” respectively.

For a multiple-keyword query \( Q \), \( \text{Potential}(X, Q) \) can also be estimated based on \( P_k(X, a_i) \) where \( a_i \)’s are the keywords in \( Q \). Here, we distinguish two cases: conjunctive queries and disjunctive queries.

To simplify our discussion, let us define \( \Pr(Q) \) to be that, given a page in \( X \)'s \( k \)-neighborhood that a user visits if he starts from \( X \), the probability that the page is relevant to \( Q \). Since the expected number of pages \( (n_k(X)) \) in \( X \)'s \( k \)-neighborhood that a user would visit if he starts from page \( X \) is simply
\[
\frac{\Pr(Q)}{n_k(X)} = \frac{P_k(X, a_1) \cdot P_k(X, a_2) \cdot \ldots \cdot P_k(X, a_m)}{n_k(X)} = \left( \frac{m}{n_k(X)} \right)^m.
\]

Thus
\[
\text{Potential}(X, Q) = \Pr(Q) \cdot n_k(X) = \left( \prod_{i=1}^{m} P_k(X, a_i) \right) / (n_k(X))^{m-1}.
\]

We remark that, in practice, the independent assumption may not hold. However, we would like to point out that the Potential function as defined above is used only to rank anchor points. It is not used to compute an accurate estimate of the number of relevant pages. In fact, this independent assumption is used in other information retrieval techniques, such as GLOSS [9]–[11]. A GLOSS server is one that maintains certain statistics about a number of information sources such as document libraries. Given a user query (conjunctive or disjunctive), the GLOSS server estimates, based on the statistics, which information source is most likely to contain the largest number of matching documents. Basically, the server remembers, for each information source and each keyword \( a \), the number of documents in the information source that contain \( a \). GLOSS uses this keyword statistics and the independent assumption to estimate the expected number of documents that each information source contains that match a query. It is shown that, in practice, such
estimation is extremely effective in ranking information sources on how likely they contain relevant documents to queries.

The potential of a page with respect to a disjunctive query can be similarly estimated. Given a disjunctive query \( Q = a_1 \lor a_2 \lor \cdots \lor a_m \), by the principal of inclusion and exclusion, we have

\[
Pr[Q] = Pr[a_1 \lor a_2 \lor \cdots \lor a_m] \\
= \sum_i Pr[a_i] - \sum_{i \neq j} Pr[a_i \land a_j] \\
+ \cdots + (-1)^{m-1} \sum_{i \neq j \neq \cdots \neq e_m} Pr[a_i \land \cdots \land a_e] \\
= \sum_i \frac{P_k(X, a_i)}{n_k(X)} - \sum_i \frac{P_k(X, a_i)}{n_k(X)} \cdot \frac{P_k(X, a_j)}{n_k(X)} \\
+ \cdots + (-1)^{m-1} \sum_{i \neq j \neq \cdots \neq e_m} \left( \prod_{i=1}^{m} \frac{P_k(X, a_i)}{n_k(X)} \right).
\]

Thus

\[
\text{Potential}(X, Q) = Pr[Q] \cdot n_k(X)
\]

(3)
can be estimated by the \( P_k(X, a_i) \)'s.

As an example, if we apply the above formula to the FAQ hypertext (Fig. 1), the anchor points for the queries “A \& B” and “A \lor C” are the page marked with an asterisk and “part index,” respectively.

V. EXPERIMENTS

In order to demonstrate the effectiveness of our model, we have built a prototype system and have conducted a series of experiments. We took snapshots of Web pages from four information sources. These include a Sports site, a Newspaper site, a site that contains FAQs’ and a site that maintains a collection of NetNews articles. These sites were chosen because they had very different hypertext structures and contents. Most importantly, these structures are commonly found in major information sources on the Web. For example, Newspaper organizes its pages into different sections (e.g., World News, Sports, Weather, etc.) with cross-references among them. On the other hand, NetNews articles form many long lists of follow-up postings with few references between the lists. By studying the effectiveness of our model over a diversified set of information sources, we will be able to learn about the robustness of the model and how it can be improved.

Our prototype system for indexing and recommending anchor points is implemented based on the model discussed in the previous sections. The Web pages collected from the snapshots were parsed to obtain the word statistics and the hypertext structures of the information sources. Based on this information, the various data structures needed to compute anchor point potentials were constructed. These data structures include the scoring function \( f(X, a) \), the \( k \)-neighborhood of each page, and the single-keyword Potential function \( P_k(X, a) \). We will discuss how these data structures are maintained and constructed in Section VI.

Volunteers were invited to test the performance of the prototype system by submitting queries that covered a broad range of topics. These queries include single-keyword queries, multiple-keyword (conjunctive and disjunctive) queries and general-concept queries. For each query, the inquirer would traverse the Web pages in the snapshots manually and would locate and rank the pages that he/she would consider the best “starting pages.” We then submitted the same set of queries to our prototype and compared its recommendations against the inquirer choices. The goals of these experiments are to find out

• precision of the recommendations. That is how good the recommended anchor points are in leading a user to the requested information;
• conciseness of the recommendations. That is how well the recommended anchor points summarize the relevant pages;
• appropriate values for \( k \) and \( \alpha \);
• stability of anchor points; that is, how they shift over time as the web pages in the information sources get updated.

In the rest of this section, we briefly summarize some general observations from our experiments. We first show a few examples of the queries submitted to and the recommendations returned from the prototype. We then discuss briefly how the values of \( k \) and \( \alpha \) are chosen. Finally, we submitted the same set of queries to different snapshots (taken at different times) of the information sources. We show that anchor points are usually fairly “stable” despite frequent updates of individual Web pages. Interested readers are refer to [14] for more details.

Sports and Newspaper

The Web sites Sports and Newspaper exhibit very similar hypertext structures. Both of them organize their documents into several major sections (e.g., local news, international news, weather, finance, etc.) Each section consists of a section index page which contains headlines (with pointers to the corresponding article pages) and pointers to subsection index pages. Another common feature of both Sports and Newspaper is that most of the pages contain a menu bar with references to the section index pages. Hence, starting from any page in the hypertext structure, a user can reach a section index in just one hop.

We describe the hypertext structure of Sports and Newspaper as shallow and broad. We found that starting from the home page, one can reach a major portion of the pages in the information source within four hops. As an example, the 4-neighborhood of the Sports’s home page represents 54.3% of all the pages in Sports (66.3% for Newspaper). The hypertext structure is thus very short or shallow. Also, most of the pages contain many hyperlinks to other pages. For example, in our experiment, the NBA index page in Sports contains 49 links to other pages. A page thus has a very extensive or broad reach to others.

With a shallow and broad hypertext structure, pages are fairly close to each other. Also, the \( k \)-neighborhoods of any two pages overlap to a large extent even if \( k \) is moderately large (e.g., when \( k = 4 \)). Recall that a page \( X \) is considered an anchor point of a query \( Q \) if one can find much information about \( Q \) in the \( k \)-neighborhood of \( X \) and that the information is close to \( X \). With a shallow and broad hypertext structure, we need a fine measure of \( k \)-neighborhood (i.e., a small \( k \)) and a fine measure
of closeness (i.e., a small \( \alpha \)) in order to better distinguish the pages’ anchor point rankings. Therefore, in the experiment on Sports and Newspaper, we picked \( k = 2 \) and \( \alpha = 0.2 \).

Fig.3 shows an example query \( <<\text{nba & scoreboard>>} \) and the potential values of the top five recommendations in Sports evaluated with respect to the query. The goal of the query is to locate information about the scores of NBA matches. We note that the highest-ranked recommendations represent very good anchor points to the query. For example, the first-ranked recommendation is the NBA section index page, from which a user can find a link directing the user to the NBA scoreboard section, a link to the highlights of today’s NBA match boxscores, a link to score statistics, besides others. The second-ranked recommendation is a page containing today’s scoreboard. This page also contains a calendar on which each date is associated with a link to a boxscore page of matches played on that date. The third-ranked recommendation is an index page to the NBA editorial section. This page also contains much information about NBA matches and scores, as well as a link to the scoreboard page.

We submitted many different types of queries in the experiment to test the effectiveness of our prototype. In most cases, we found that the suggested pages are precise and relevant to our queries. Most importantly, the recommended pages represent logical starting points from which relevant information can be orderly retrieved in their pages represent logical starting points from which relevant to our queries. Most importantly, the recommended recommendations represent very good anchor points to the query. For example, the first-ranked recommendation is the NBA section index page, from which a user can find a link directing the user to the NBA scoreboard section, a link to the highlights of today’s NBA match boxscores, a link to score statistics, besides others. The second-ranked recommendation is a page containing today’s scoreboard. This page also contains a calendar on which each date is associated with a link to a boxscore page of matches played on that date. The third-ranked recommendation is an index page to the NBA editorial section. This page also contains much information about NBA matches and scores, as well as a link to the scoreboard page.

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As we have discussed, anchor points (especially those for general concepts) tend to be indexes. For example, in Sports, the best anchor point of \( <<\text{Sports>>} \) is the NBA index page. We note that anchor points are relatively stable for two reasons: First, indexes usually have long life-spans. Second, although the content of anchor points change (we have different headlines every day for an interesting world), their ranks against queries (which take into account the aggregate contents of their \( k \)-neighborhoods) stay relatively stable.

To verify the stability of anchor points, we collected different snapshots of each information source over a period of time, applied the same set of queries on the snapshots, and compared the results. (An example demonstrating anchor point stability can be found in [14].) From our experiments, we observe that even though there are minor re-orderings of the recommendations, the set of anchor points the system returns stays relatively unchanged. Anchor points are therefore fairly stable in the sense that they remain the best starting points for retrieving relevant information even though the content of an information source is constantly updated. The stability property allows the system to use a smaller refresh rate. That is, the potential function needs not be recomputed too often. As we will see in the next section, maintaining the potential function requires a higher computational cost than maintaining an inverted index used by traditional search engines. However, the lower recomputation rate can offset the higher CPU demand in anchor point computation. We will explore other techniques in reducing the computational cost in the next section.

### VI. Data Structures and Algorithms

As we have discussed in Section IV, computing the potential of a page with respect to a query requires the system to maintain certain information about the network of Web pages. This includes the scoring function \( f(X, a) \), the distance function \( D(X, Y) \), and the \( k \)-neighborhood of a page \( N_k(X) \). From this data, one can derive the potential function \( P_k(X, a) \) according to (1), and hence the anchor point rankings using (2) and (3). In this section, we discuss the data structures for storing the various information and the algorithms for their derivations.

**Scoring Function:** Given a page \( X \) and a keyword \( a \), the scoring function \( f(X, a) \), returns a score which indicates how relevant page \( X \) is with respect to \( a \). In our prototype, we calculate this score as the normalized word count of \( a \) in \( X \) according
to the TFIDF formula [18]

\[ f(X, a) = \text{freq}_{a \in X} \times \log_2 \frac{n}{\text{docfreq}_a} + 1 \]

where
- \( \text{freq}_{a \in X} \) is the occurrence frequency of keyword \( a \) in page \( X \),
- \( n \) is the total number of pages indexed,
- \( \text{docfreq}_a \) is the document frequency of keyword \( a \).

We represent the scoring function using an inverted index [8], just like most traditional search engines do.

**Adjacency and \( k \)-Reachability:** The simplest way to store the adjacency relationship is to use a square bit-matrix. An entry \((i, j)\) in the matrix is set to 1 if page \( j \) contains a hyperlink pointing to page \( i \). This representation, however, is not very space efficient. We found that the adjacency matrices are very sparse for most information sources. Table II shows some typical adjacency matrix occupancies.

We notice that the occupancies are very small. Even for **Sports** and **Newspaper** whose hypertext structures are broad, an average page is only adjacent to about 0.5% of all the pages located in the same source. The occupancy is much lower for narrow hypertext structures (such as FAQ and NetNews). To save space, our prototype represents the adjacency relationship using inverted adjacency lists. That is, for each page \( i \), we maintain a linked list of pages which contain hyperlinks pointing to page \( i \).

From the inverted adjacency lists, we derive the \( k \)-reachability relationship between pages. The goal is to find out, for a page \( A \) that is inside the \( k \)-neighborhood of another page \( B \), how many hops it takes to go from \( B \) to \( A \). Again, the \( k \)-reachability relationship can be represented by a matrix. The entry \((i, j)\) gives the distance from page \( j \) to page \( i \) if the distance is smaller than or equal to \( k \). Table III shows the occupancies of some \( k \)-reachability matrices for \( k = 2 \) and \( k = 3 \). As we have discussed in Section V, **Sports** and **Newspaper** have a broad hypertext structure. For them, we use a small value of \( k \) (\( = 2 \)). On the other hand, FAQ and NetNews have a very narrow hypertext structure, which allows a larger \( k \) (\( = 3 \)) to be used. In any case, Table III shows that with the appropriate value of \( k \), the \( k \)-reachability matrices are sparse. We thus represent the matrix using linked lists. In particular, for each page \( A \), we keep \( k \) linked lists, \( L_i(A) \) (\( 1 \leq i \leq k \)), where \( L_i(A) \) represents the set of pages whose distance to \( A \) is \( i \), i.e., \( L_i(A) = \{ B \mid D(B, A) = i \} \). An algorithm for deriving the inverted \( k \)-reachability lists and the size of each page’s \( k \)-neighborhood from the inverted adjacency lists can be found in [14].

**Potential Function:** The potential function \( P_k(X, a) \) returns the potential value of a page \( X \) with respect to a keyword \( a \). Similar to the scoring function, we represent the potential function using inverted lists. That is, for each keyword \( a \), we maintain a list of pages which have nonzero potentials with respect to \( a \), and their potential values. An algorithm for deriving the potential function can be found in [14].

**Query Processing:**

Given a query \( Q \) that is composed of the keywords \( \{a_1, \ldots, a_m\} \), to calculate the potentials of the pages with respect to \( Q \), we first retrieve the inverted lists of the potential function corresponding to the keywords. This gives us \( S_i \) (\( 1 \leq i \leq m \)) where \( S_i = \{ \text{page } p \mid P_k(p, a_i) > 0 \} \). If \( Q \) is a conjunctive query, we find the intersection of the \( S_i \)’s, and compute \( \text{Potential}(X, Q) \) for only those pages \( X \in \bigcap_{i=1}^{m} S_i \) using (2). On the other hand, if \( Q \) is disjunctive, we find the set union and evaluate the pages’ potentials according to (3). The pages are then sorted in decreasing values of their potentials.

### A. Storage Requirement

Comparing with traditional search engines, recommending anchor points requires the system to maintain more data. This includes the \( k \)-reachability lists and more importantly the potential function. In this section we discuss the additional storage requirement and how we could reduce it.

As we have discussed previously, our system uses a small \( k \) value (2) for information sources (**Sports** and **Newspaper** whose hypertext structures are broad (containing many links). From Table III, we see that for an average page in **Sports** or **Newspaper**, the size of its 2-neighborhood is less than 500 pages\(^3\). The storage overhead for maintaining the \( k \)-reachability lists is acceptable even for these broad hypertext structures. For example, our prototype uses 11 MB to store the 2-reachability lists of **Newspaper** whose documents require 110 MB of storage. The overhead is therefore only 10% of the document database. This storage overhead for sources with narrow hypertext structures is much smaller. For example, in **NetNews**, the storage overhead for maintaining the 3-reachability lists is only 1.9% of the document database size.

The storage requirement for the potential function, however, can be much higher than that of the scoring function maintained by traditional search engines. This is because while we keep an entry of \( f(X, a) \) only if page \( X \) contains the keyword \( a \), in the anchor point system, we need to keep an entry of \( P_k(X, a) \) if keyword \( a \) occurs in any pages that are within the \( k \)-neighborhood of page \( X \). As an example, in the **Newspaper** snapshot, there are 5788 pages containing 36 021 keywords. A full potential function (or scoring function) would have as many as \( 3 \) Estimated by multiplying the number of documents in the source by the occupancy of the 2-reachability matrix. For **Sports**, it is \( 9116 \times 5.4\% = 492 \); for **Newspaper**, it is \( 5788 \times 8.2\% = 474 \).
5788 × 36 021 = 208 million entries. Among these, about 137 million entries (65.8%) of the potential matrix are nonzero and have to be kept. Comparing with only 1.14 million nonzero entries for the scoring function, maintaining the potential function requires 120 times the storage of that is needed to maintain the scoring function alone.

One way to reduce the storage requirement is to throw away those less significant entries of the potential function. We observe that most of the entries contain, in fact, very small values. Again, taking Newspaper as an example, 68.1% of all non-zero potentials are below 1.0, and about 93.5% of them are below 10.0. The remaining 6.5% of the potential function entries have values range from ten to a maximum potential of about 8 000.0. In summary, the values of the potential function are extremely skewed. We note that, given a query, a page which has a small potential value with respect to a keyword in the query is not likely to rank high in the recommendation. Approximating the small potential values by 0 (i.e., not keeping them) may not severely affect the quality of the recommendation. Throwing away small-value entries in the potential function can thus significantly reduce the storage demand.

Removing small entries from the potential function, however, reduces the amount of knowledge of the system. It is thus interesting to see how that would affect the system’s performance in answering queries. We repeated some of the user queries after removing small potential values that account for 90% of the total number of nonzero potentials. We found that in most cases, the cut did not affect the high-ranked recommendations at all. The quality of the answer set remains very good. (See [14] for a more detailed description of the experiment.)

We remark that removing small potential entries has a very mild effect on single-keyword queries. This is because only low-ranked recommendations are removed from the answer sets. For a multiple-keyword conjunctive query, however, a page may be kicked out of the answer set if it has a low potential with respect to a keyword in the query even though it may has extremely high potentials with respect to the others. This kind of omission may not be too bad if the user gives equal weight to all the query keywords. For a disjunctive query, the page will not lose much in its ranking because it is supported mainly by those keywords for which it has high potentials [see (3)].

VII. CONCLUSION

We identified four sources of ineffectiveness of traditional search engines and introduced the concept and use of anchor points. Given a user query, the set of anchor points is a set of key pages from which the larger set of documents that are relevant to the query can be easily reached. The use of anchor points help solve the problems of huge answer set and low precision suffered by most search engines. The major improvement is achieved by considering the hyperlink structures of the relevant documents, and by providing a summary view of the result set. We have implemented a prototype based on the concept of anchor point. Comparisons were made to traditional search engines. We found that our approach gave higher ranks to pages (such as indices) that provided better starting points for accessing relevant pages. On the other hand, traditional search engines tend to ignore the logical structure of hyperdocuments, and relevant pages are distributed unpredictably in the answer set.

We have addressed some implementation issues of an anchor point indexing system. In particular, we discussed how the various information and data for computing anchor points are efficiently maintained. We also showed that anchor points are fairly stable. Frequent update of the anchor point index is thus unnecessary. This offsets the CPU requirement of handling a larger data structure (the potential function) than traditional search engines require (the scoring function).

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