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An Advanced Permanent Magnet Motor Drive System for Battery-Powered Electric Vehicles

C. C. Chan and K. T. Chau

Abstract—Recent availability of high-energy neodymium-iron-boron (Nd-Fe-B) permanent magnet (PM) material has focused attention on the use of the PM synchronous motor (PMSM) drive for electric vehicles (EV's). A new Nd-Fe-B PMSM is proposed for the drive system, which possesses high power density and high efficiency, resulting in greater energy and space savings. The design and optimization of the motor employ finite element analysis and computer graphics. Increasingly, a new PWM inverter algorithm is developed for the drive system, which can handle the nonconstant battery voltage source. An efficiency optimizing control is adopted to further improve the energy utilization of the drive system. Both the control strategy and the PWM generation are implemented in a single-chip microcontroller. As a result, the motor drive achieves high power density, high efficiency, and compactness. A prototype of the 3.2-kW battery-powered drive system has been designed and built for an experimental mini-EV.

I. INTRODUCTION

In the past decades, dc variable-speed drive systems were commonly used for industrial drive and electric vehicle (EV) applications. Studies [1]–[4] have shown that an ac drive system offers several definite advantages over dc drive systems for EV's, among which are these:

1) light weight and high efficiency,
2) efficient regenerative braking,
3) robustness and reliability, and
4) almost maintenance free.

In recent years, the International Electric Vehicle Research Center has launched a series of research projects on the development of advanced EV's with an ac propulsion system [5]. The projects of the electric sedan [6] and electric van [7] have been concentrated on the development of advanced control strategies with the application of standard construction induction motors. On the other hand, the high-efficiency, high power density special motor drives are undergoing development for EV applications.

Recent research has indicated that the permanent magnet (PM) ac motors, which include the PM synchronous motor (PMSM) and the brushless dc motor (BDCM) and inherently possess high efficiency and high power density, are becoming attractive in high-performance drive systems and have the prospect to compete in the induction motor market [8]–[10]. Although the PMSM and the BDCM are similar in construction, their mathematical models, hence steady-state and dynamic behaviors, are different [11]. The PMSM has a sinusoidal back EMF and requires sinusoidal stator currents to produce constant torque, while the BDCM has a trapezoidal back EMF and requires rectangular stator currents to produce constant torque. In general, the PMSM is very similar to the standard wound rotor synchronous motor except that the excitation is provided by a magnet instead of a field winding. Since there is no difference between the back EMF produced by a magnet and that produced by an excited coil, the mathematical model of a PMSM is also similar to that of a wound rotor synchronous motor. As the transformation of the synchronous machine equations from the A-B-C phase variables to the D-Q variables forces all sinusoidally varying inductances in the A-B-C frame to become constant in the D-Q frame, the D-Q model of the PMSM can be derived. On the contrary, since the back EMF in the BDCM is nonsinusoidal, the inductances do not vary sinusoidally in the A-B-C frame, and it does not seem advantageous to transform the equations to the D-Q frame since the inductances will not be constant after transformation. Hence the A-B-C phase variables model is used for the BDCM.

The BDCM must be operated in the closed-loop mode where a relatively expensive and delicate rotor position sensor is used, even though many attempts have been made to eliminate this sensor to facilitate the commutation of the power converter. Its speed control is generally accomplished by regulating the applied voltage. This motor has a significant torque pulsation due to the commutating current during the phase commutation of the switching devices. On the contrary, the PMSM can be operated in either the open-loop mod or the closed-loop mode where the rotor position sensor may be used only when some sophisticated control strategies are implemented. Similar to a wound rotor synchronous motor, the rotor of the PMSM is always in synchronism with the rotating field, which depends on the applied frequency. Similar to the classical polyphase ac motors, namely the synchronous motor and the induction motor, the PMSM produces an essentially constant instantaneous torque or so-called smooth torque [12]. Being fueled by rapid developments in high-energy magnet material technology [13], [14], modern computation methods for electromagnetic analysis [15], [16], and powerful computing environment [17], [18], numerous motor geometries of the PMSM have been designed. In general, the design philosophy is to further improve the power density and efficiency by adopting either flux enhancement [10], armature-reaction...
TABLE I

SPECIFICATIONS OF MINI-EV

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
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<tr>
<td>Vehicle Gross Weight</td>
<td>403 kg</td>
</tr>
<tr>
<td>Normal Payload</td>
<td>200 kg</td>
</tr>
<tr>
<td>Top Speed</td>
<td>30 km/h</td>
</tr>
<tr>
<td>Gradability</td>
<td>15°</td>
</tr>
<tr>
<td>Acceleration (0 - 20 km/h)</td>
<td>8 s</td>
</tr>
<tr>
<td>Range (20 km/h constant)</td>
<td>70 km</td>
</tr>
<tr>
<td>Battery</td>
<td>4×12 V 75 Ah lead acid</td>
</tr>
</tbody>
</table>

reduction, or high-speed operation. In this paper, a newly designed PMSM with special rotor geometry is developed, which is suitable for EV applications. Since the magnet material is relatively expensive, in practice, it may not be economical to design the PMSM at a very high power range. However, the required output power of a mini-EV is of several kilowatts, which is a suitable power range for economical application of the PMSM.

For battery-powered EV's, the energy stored in the battery becomes so precious that a high-efficiency drive system is of the utmost importance. Besides using the PMSM to improve the energy utilization of the drive system, an efficiency optimizing control scheme is adopted [19], [20]. The control strategy operates by measuring the current on the dc link and adjusting the voltage output of the inverter to minimize this quantity. In this way, the system optimizes the combined motor-inverter efficiency, not just the motor efficiency. Since the control strategy requires the output voltage and efficiency to be individually controllable, a voltage-controlled voltage-source PWM inverter is used. However, the voltage level of the battery fluctuates significantly, which depends on the battery state-of-charge, discharging current, temperature, and aging. Conventionally, in order to compensate for such fluctuation, an additional pulsewidth compensator unit is installed. Instead of using an additional unit, a new PWM algorithm, namely the equal-area pulsewidth modulation (EAPWM), is proposed and implemented, which can handle a changing battery voltage [21].

Owing to the increasing demands imposed on knowledge of critical areas and tools for design and optimization, the electromagnetic field approach to the design of electrical machines has been widely accepted. As the finite element method (FEM) is regarded as one of the most powerful tools in electromagnetic field analysis [22], it is adopted to design and optimize the proposed PMSM. Since the mathematical model of a PMSM is similar to that of a wound rotor synchronous motor, the PMSM is modeled by using the standard synchronous machine equivalent circuit.

III. PM SYNCHRONOUS MOTOR

A. Motor Geometry

Starting from the last decade, numerous geometries of the PMSM have been introduced. They are usually based on the further improvements of power density and efficiency by adopting either flux enhancement, armature-reaction reduction, or high-speed operation. Electrical motors should be operated
at an air-gap flux density of about 0.8 T to achieve high efficiency, and an iron-core flux density of about 1.2 T to ensure good utilization of laminated iron cores. The flux-enhancement arrangement of the PMSM allows higher flux densities in the air-gap and enables the operating point of the magnets to be shifted toward the optimum, which leads to the saving in relatively expensive magnet materials. However, with the employment of flux enhancement, the effective air-gap (including the actual air-gap and the magnets) to be bridged by the armature field is usually very small, leading to a strong armature reaction. This leads to limit the attainable average force density of the PMSM. Moreover, due to the high armature reactance of the PMSM, the operating performance of the inverter is degraded. In [23], a technique of using appropriately laminated iron poles to reduce the armature reaction was furnished. It is well known that the power density of electrical motors can be significantly increased by using a higher operating speed. By burying the magnets inside the rotor, they are then physically protected. Thus, under high-speed operation, the mechanical integrity of the rotor can be maintained.

The proposed PMSM, adopting a high-energy neodymium-iron-boron (Nd-Fe-B) magnet material and a new rotor geometry, is shown in Fig. 3. In conjunction with the flux-enhancement arrangement, the armature reaction can be considerably reduced by making air slots symmetrically along the D-axes within the rotor. It is due to the fact that the air slot at each pole center has to be bridged by the armature field while the flux path for the excitation field has only an insignificant change. To avoid any serious harmonic distortion in the air-gap flux, a closed air slot is used. Due to the fact that the magnets are buried inside the rotor and are physically protected, a high-speed operation is permissible. Therefore, the proposed motor geometry allows the simultaneous attainments of flux enhancement, armature-reaction reduction, and high-speed operation, resulting in higher power density and higher efficiency.

B. Analysis and Optimization

As the proposed PMSM has an unconventional rotor geometry and uses materials with anisotropic and/or nonlinear properties, electromagnetic design approach is necessary. The electromagnetic analysis can also give much greater knowledge of critical areas of the PMSM and provide a tool for optimization. Nowadays, the FEM, which was originally proposed by Silvester and Chari [22], is regarded as one of the most powerful tools in electromagnetic analysis of electrical machines. By solving the following nonlinear partial differential equation with proper boundary conditions

\[ \nabla^2 A = -\mu J \]

where \( A \) is the vector magnetic potential, \( \mu \) is the magnetic permeability, and \( J \) is the current density, while other field quantities can then be easily derived from the vector magnetic potentials. With the employment of FEM for electromagnetic calculation and computer graphics for solid modeling, animation, pre- and post-processing of the massive database [17], [18], a computer-aided design software for the PMSM is developed in a powerful workstation [24]. The magnetic field distributions due to the magnet, D-axis armature reaction and Q-axis armature reaction are colorfully and interactively evaluated. The field pattern is not only represented by using colors and intensities, its actual value of flux density corresponding to the location pointed by the on-line cursor is also displayed. Black-and-white photos of the magnetic field distributions of the PMSM are shown in Fig. 4.

The optimization of the proposed PMSM includes the minimization of magnet material outlay, as well as the maximization of iron-core utilization, and the reduction of armature reaction in conjunction with the arrangement of flux enhancement. Moreover, the magnet operating point on its demagnetizing curve should be considered so that it must refrain from demagnetization during starting or heavy loading conditions. The optimization flowchart is illustrated in Fig. 5. Focusing on the purposely introduced air slots, the shapes and dimensions are iteratively optimized. From Table 1, it can be found that the Q-axis armature reaction can be effectively reduced by a factor of 3.0 without a sacrifice of induced EMF. In conjunction with the flux enhancement, an air-gap flux density is of 0.8 T.

C. Specifications

The specifications of the three-phase, four-pole PMSM specially designed for a battery-powered EV drive system are listed as follows:

- Rated voltage: 32 V
- Rated output power: 3.2 kW
- Rated speed: 4800 rpm
- Rated efficiency: 88.4%
- Rated power factor: 0.935
- Rated power density: 2009 kW/m³
- Overall weight: 24 kg
- Magnet remanence: 1.1 T
- Magnet coercivity: 680 kA/m.
Fig. 4: Magnetic field distributions. (a) Permanent magnet field distribution. (b) D-axis armature field distribution. (c) Q-axis armature field distribution.

D. Mathematical Model

It is common practice to model the PMSM using the standard synchronous machine model [19]. For steady-state operation from balanced sinusoidal voltages, the model reduces to the per-phase equivalent circuit shown in Fig. 6.

In Fig. 6, $V$ is the applied voltage, $R_s$ is the stator resistance, $X_s$ is the synchronous reactance, $R_o$ is the iron-loss (core-loss) resistor, $E_o$ is the induced EMF, $I_1$ is the stator current, $I_2$ is the rotor current, and $I_c$ is the iron-loss current. As iron loss is dictated by hysteresis and eddy currents, the use of a single-valued iron-loss resistor can accurately represent the flux and frequency dependence of the eddy-current losses but is only an approximation for the hysteresis loss. Instead of adopting a sophisticated model of iron loss, a control strategy that does not require an accurate modeling of iron loss is preferred. Increasingly, by using a self-adaptive control strategy, there is no need to purposely evaluate the model parameters.

IV. PWM Inverter

A high-power bipolar-junction transistorized inverter has the advantages over its thyristorized counterpart in the aspects of commutation problems, switching frequency, and efficiency. Moreover, it also has the advantages over its power MOSFET-based counterpart in the aspects of power handling capabilities, conduction resistance, and cost. Although a new power device, namely the insulated gate bipolar transistors (IGBT's), has been reported to have the advantages of both power bipolar-junction transistors (BJT's) and power MOSFET's, the BJT's are still the most mature technologically and are the power device most commonly used in motor drive applications [25]. In order to simplify the base-drive circuitry, Darlington-configured BJTs are used to build the three-phase full-bridge PWM inverter. In each base-drive circuit, a hybrid IC is used as an isolation amplifier for the interface between the gating signal and the power transistor module [26], [27]. The inverter
TABLE II
EFFECTS OF AIR SLOTS

<table>
<thead>
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<th>(i) Without air slots</th>
<th>(ii) With air slots</th>
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<tbody>
<tr>
<td>$E_o$ (pu)</td>
<td>1.129</td>
<td>1.128</td>
</tr>
<tr>
<td>$X_{ad}$ (pu)</td>
<td>0.322</td>
<td>0.322</td>
</tr>
<tr>
<td>$X_{aq}$ (pu)</td>
<td>0.735</td>
<td>0.248</td>
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Fig. 5. Optimization flowchart.

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The concept of EAPWM is to divide one period of sinusoidal wave into $S$ segments and to evaluate the pulselwidths so that the pulse area is equal to the area of the related segment of the sinusoidal wave with respect to the same reference as illustrated in Fig. 7. Unlike the natural-sampled PWM techniques, the pulselwidths can be expressed as a simple algebraic equation, and therefore this technique is more straightforward for producing PWM pattern.

Using the reference shown in Fig. 7, the required output voltage $V_o$ is expressed as

$$V_o = V_d + V_m \sin \omega t$$

(2)

where $V_d$ is the dc supply voltage, $V_m$ is the amplitude of required output voltage and $\omega$ is the required output frequency, then the related area $A_j$ for the $j$th segment between time interval $t_j$ and $t_{j+1}$ can be calculated as follows:

$$A_j = \int_{t_j}^{t_{j+1}} (V_d + V_m \sin \omega t) dt.$$  

(3)

The corresponding pulse area $B_j$ can be expressed as

$$B_j = 2V_d P_j$$

(4)

where $P_j$ is the unknown pulselwidth for the $j$th segment. Applying the EAPWM concept to (3) and (4), $P_j$ can be
determined as follows:

\[ P_j = \frac{1}{\omega} \left[ \frac{\theta_{j+1} - \theta_j}{2} + \frac{V_m \cos \theta_j - \cos \theta_{j+1}}{V_d} \right] \]  

(5)

where \( \theta_j \) and \( \theta_{j+1} \) are angle intervals of the \( j \)th segment. The corresponding notch width \( N_j \) can be expressed as follows:

\[ N_j = \frac{1}{\omega} \left[ \frac{\theta_{j+1} - \theta_j}{2} - \frac{V_m \cos \theta_j - \cos \theta_{j+1}}{V_d} \right] \]  

(6)

The calculated pulsewidths are located at the center of each segment, which gives output symmetry at \( \pi/2 \) and \( 3\pi/2 \). Thus the required calculation and harmonic distortion can be reduced. Since the expressions of pulsewidths and notch widths are nearly the same except the sign of the second term, the required calculation can be further reduced to a quarter period only. Hence the EAPWM is highly suitable for real-time computation and can be easily implemented using a single-chip microcontroller.

For the mini-EV, the 48-V battery pack voltage may vary significantly from 37 V at the nearly empty case to 60 V at the fully charged case. Conventionally, the modulation depth of the inverter voltage is modified by an additional pulsewidth compensator unit in the controller so as to maintain the inverter output voltage. However, since the pulsewidths of the EAPWM algorithm are directly related to the dc supply voltage, they are automatically adjusted for a changing battery voltage. The harmonic content of EAPWM is low, which has been proved to be very similar to that of the regular-sampled PWM [21].

The advantages of EAPWM are summarized as follows:

1. The modulation depth can be automatically adjusted for a changing battery voltage.
2. The PWM pattern can be calculated in real time.
3. The algorithm can be implemented with minimum hardware and compact software.
4. The harmonic content is low.

In this PMSM drive system, the number of pulses per output cycle (frequency ratio) is kept at 12 in most of the frequency range, while in very low frequency or start-up conditions, it is increased to 120 so as to avoid a pulsing rate the motor cannot tolerate.

V. CONTROLLER

In order to further improve the energy utilization of the drive system, the control strategy is based on efficiency optimization [20]. There are basically two approaches to efficiency optimization. One method employs a loss model of the machine and regulates the controlled quantities to minimize the total loss. A second approach is to measure the power delivered to the drive and use a search algorithm to adjust a control variable until it detects a minimum in the power. The latter one is selected, which has the advantage that it does not depend on a loss model of the machine and therefore is insensitive to variations in the motor parameters, such as the temperature change in resistance, and does not require accurate modeling of complicated phenomena such as iron loss. Hence, there is no need to accurately evaluate the model parameters of the PMSM.

By using the equivalent model of the PMSM shown in Fig. 6, the per-phase total loss can be expressed as

\[ P_{\text{Cu}} = \left( \frac{P}{E_0} \right)^2 \left( \frac{R_c}{R_c} \right) \]  

(7)

\[ P_{\text{Fe}} = \left[ \frac{P^2 X_a^2}{E_0^2} \right] \]  

(8)

\[ P_{\text{loss}} = P_{\text{Cu}} + P_{\text{Fe}} \]  

(9)

where \( P \) is the per-phase output power, \( P_{\text{Cu}} \) is the per-phase copper loss, \( P_{\text{Fe}} \) is the per-phase iron loss, \( P_{\text{loss}} \) is the per-phase total loss, and variables with subscripts \( d \) and \( q \), respectively, represent their \( D \)- and \( Q \)-axis components. By using (7)-(9), typical loss characteristics are simulated in Fig. 8. It is found that there is a unique optimum operating point of the input voltage. In particular, it can be observed that the minimum total loss occurs at a lower voltage than does the minimum copper loss, verifying that the maximum torque/ampere scheme may not actually maximize the efficiency of the PMSM drive.

Based on the simulation, the efficiency-optimizing algorithm is to automatically adjust the applied voltage of the PMSM such that the total power loss is minimum, which can be reflected by the minimum input power to the PMSM. Instead of measuring the PWM voltage and current of the motor input to calculate the input power, it is more convenient to measure the dc voltage and current of the inverter input. Hence, by using only the information of battery voltage and current, the combined inverter-motor efficiency optimization can be attained. This technique is particularly suitable for applications where efficiency and simplicity are desirable.

The major function of the controller is to control the three-phase PWM inverter, hence the operation of the PMSM, in accordance with the control strategy. The special requirements of this mini-EV controller are listed as follows:

1. compact and light hardware,
2. flexible and reliable software, and
3. low power consumption.
With the adoption of the recently available 16-b embedded microcontroller, the hardware count and size of the controller can be greatly reduced. The Intel-8095 microcontroller is chosen because it includes the following features [29]:

1) 8 kilobytes of EPROM (for EPROM version),
2) 232 bytes of RAM,
3) 8 channels of 10-b A/D converter,
4) 8 pins of high-speed pulse I/O,
5) 4 16-b software timers, and
6) 8 interrupt sources.

As illustrated in Fig. 9, the driver command and feedback signals are inputted via the built-in A/D converter while the PWM gating signals are outputted through six high-speed output units of the microcontroller.

Since the efficiency-optimizing control and the PWM pattern are calculated in real time, the software is written in MCS-96 assembly language. The software implementation of the efficiency-optimizing control algorithm is illustrated in Fig. 10. The initial PWM output voltage is determined by the product of the frequency command and the predefined volt/hertz ratio. For a very low frequency operation, boosting voltage is required. A self-searching process is then performed by changing the voltage magnitude with an appropriate step size $|\Delta V|$. A test is made to check whether the input power has increased or decreased. An increase causes the search direction to reverse by using the block $\Delta V = -\Delta V$ while the search direction is unchanged if the input power decreases. The voltage step size should be fine enough to permit closer convergence to the optimum. If four consecutive steps are taken in the same direction, the step size is enlarged by four times via the block $V = V + 4 \times \Delta V$ so as to permit faster convergence to the optimum.

VI. EXPERIMENTAL RESULTS

As the mathematical model of the PMSM is based on the classical model of synchronous machines, it is well-known that the evaluation of accurate model parameters, especially the single-valued resistor corresponding to iron loss, requires tedious experimental tests. In fact, even though the parameters can be experimentally determined, most of them may vary significantly with the operating conditions, namely the operating frequency, current, and temperature. Hence, it is useless to compare the idealized simulation results with the experimental results. Therefore, the aim of the experimental test is to verify the efficiency-optimizing control strategy for the PMSM.

The drive system was tested on a laboratory test bed. The waveforms of the EAPWM line voltage and motor line current, operating at 100 Hz are shown in Fig. 11. It can be found that the frequency ratio is selected as 12, which is a compromise between the switching loss and harmonic distortion. Fig. 12 shows the recorded motor speed, dc battery current, and motor line current. It can be observed that when steady state has been attained, the dc battery current and the motor line current are successively diminished to optimal values, while the motor speed is unchanged. Since the battery voltage is almost constant within the recording period, the input power is diminishing when delivering constant output power, leading to efficiency optimization of the inverter-motor set.

VII. CONCLUSION

In this project, an advanced PMSM drive system for a battery-powered mini-EV is presented. The design process of the PMSM adopts the electromagnetic approach, which can provide knowledge of critical areas and a tool for optimization, while the mathematical modeling of the PMSM employs a classical circuit approach, which is convenient to design the control strategy. With the employment of computer-aided
design, the proposed PMSM adopting a new rotor geometry, which possesses high power density, high efficiency, smooth torque, and convenient speed regulation, is tailor-made for the mini-EV. Although, in principle, the proposed PMSM can be readily scaled upward to fit the needs of a regular on-road EV with a motor of the order of 50 kW, the economical benefit will be diminished because of the relatively expensive magnet material. The power-transistorized PWM inverter adopts a newly proposed algorithm, which is particularly suitable for a nonconstant battery voltage source. The controller hardware is based on a single-chip microcontroller, while the control software is to implement an efficiency-optimizing control strategy. The experimental results show that the proposed drive system works well for the mini-EV.

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REFERENCES


