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<td><strong>Citation</strong></td>
<td>Proceedings of the Institution of Civil Engineers: Structures and Buildings, 2016, v. 169 n. 2, p. 81-95</td>
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<td><strong>Issued Date</strong></td>
<td>2016</td>
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<tr>
<td><strong>URL</strong></td>
<td><a href="http://hdl.handle.net/10722/229140">http://hdl.handle.net/10722/229140</a></td>
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Design of bolted side-plated reinforced-concrete beams with partial interaction

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Existing reinforced-concrete (RC) beams can be effectively strengthened by anchoring steel plates to the side faces of the beams using bolts, which is known as the bolted side-plating (BSP) technique. Previous studies have found that the performance of BSP beams is primarily controlled by the degree of partial interaction at the steel–RC interface, which can be conveniently quantified by the strain and curvature factors. In this paper, a new simplified flexural design procedure for BSP beams taking into account partial interaction is presented. Some optimum ranges of strain and curvature factors are first introduced to the flexural design of BSP beams. By ensuring the flexural capacity of a BSP beam is higher than the design moment, the preliminary size of steel plates and the arrangement of bolts can be determined. Following this, the maximum design slips and minimum design strain and curvature factors are calculated and back-checked to ensure the target flexural capacity of the BSP beam has been achieved. An example is presented to illustrate the effectiveness of the optimised design method for BSP beams, considering the effect of partial interaction under realistic loading conditions.

Notation

- \( A_p \): cross-section area of the steel plates
- \( A_s \): cross-section area of the reinforcement
- \( A_{kc} \): cross-section area of the compressive reinforcement
- \( A_{ta} \): cross-section area of the tensile reinforcement
- \( b \): breadth of the RC beam
- \( c \): depth of the neutral axis
- \( D_c \): depth of the RC beam
- \( D_p \): depth of the steel plates
- \( D_{sh} \): depth of the secondary beam
- \( D_{sl} \): depth of the floor slab
- \( d_b \): nominal diameter of the anchor bolts
- \( d_{lc} \): lever arm between the tensile reinforcement and the compressive block of the RC beam section
- \( E_p \): Young’s modulus of the steel plates
- \( E_s \): Young’s modulus of the reinforcement
- \( (EA)_c \): axial stiffness of the unstrengthened RC beam
- \( (EA)_p \): axial stiffness of the steel plates
- \( (Ed)_c \): flexural stiffness of the unstrengthened RC beam
- \( (Ed)_p \): flexural stiffness of the steel plates
- \( F \), \( F_i \): total external load (ith point load, \( i = 1, 2, 3 \ldots \))
- \( F_p \): peak total external load
- \( F_{p,exp} \): peak total external load (experimental)
- \( F_{p,the} \): peak total external load (theoretical)
- \( f_c \): compressive strength of the concrete
- \( f_{ck} \): characteristic compressive strength of the concrete
- \( f_{ub} \): ultimate tensile strength of the anchor bolts
- \( f_y \): yield strength of the reinforcement
- \( f_{yp} \): yield strength of the steel plates
- \( h \): depth of the RC beam
- \( h_c \): depth of the compressive reinforcement
- \( h_t \): depth of the tensile reinforcement
- \( h_{sb} \): depth of the bottom edge of the steel plates
- \( h_{tp} \): depth of the top edge of the steel plates
- \( I_p \): second moment of area of the steel plates
- \( i_c \): effective radius of gyration of the RC beam
- \( i_{cp} \): separation between the centroids of the RC beam and the steel plate
- \( i_p \): effective radius of gyration of the steel plates
- \( K_p \): shear stiffness of the anchor bolts
- \( k_{tm} \): stiffness of the connecting media
- \( L \): clear span of the RC beam
- \( L_s \): shear span
- \( M_d \): design moment caused by the external loads
- \( M_G \): bending moment caused by the permanent loads
- \( M_Q \): bending moment caused by the variable loads
- \( M_u \): flexural strength of the BSP beam
- \( M_{BSP} \): flexural strength of the BSP beam
- \( M_{ARC} \): flexural strength of the RC beam
- \( M_{BSPFI} \): flexural strength of the BSP beam under full interaction assumption
- \( N_p \): tension force of the steel plate
- \( N_u \): resultant axial force of the BSP beam corresponding to \( M_u \)
number of anchor bolts in a shear span
parameter including the stiffness components of the BSP beams
distributed external transverse load
distributed external transverse load on the steel plates
shear force of an anchor bolt
yield shear force of an anchor bolt
shear deformation of the anchor bolts
longitudinal bolt spacing
yield shear deformation of the anchor bolts
longitudinal slip on the plate–RC interface
transverse slip on the plate–RC interface
thickness of one steel plate
centroidal level of the steel plates
unique value for the strain and the curvature factors
modifier in the computation of the bolt shear strength
strain factor \( \frac{\varepsilon_p y_p}{\varepsilon_c y_c} \)
curvature factor \( \frac{\phi_p}{\phi_c} \)
ratio between the stiffness of the bolt connection and the RC beam
flexural stiffness ratio between the steel plates and the RC beam
partial safety factor for the bolt connection
partial safety factor for the concrete material
partial safety factor for the actions caused by the permanent loads
partial safety factor for the bolt material
partial safety factor for the actions caused by the variable loads
partial safety factor for the steel material
strain of the concrete or the RC beam
strain at the peak compressive stress in the concrete
ultimate compressive strain of the concrete
longitudinal strain of the RC beam
strain of the steel plates
strain at the bottom edge of the steel plates
strain at the top edge of the steel plates
longitudinal strain of the steel plates
strain of the reinforcement
strain of the compressive reinforcement
strain of the tensile reinforcement
yield strain of the reinforcement
yield strain of the steel plate
factor defining the effective strength of the concrete
factor for the effective depth of the concrete compression zone
parameter used to compute the longitudinal slip and the strain factor
dimensionless shear transfer ratio at the supports
steel ratio of the tensile reinforcement
balanced tensile steel ratio
stress of the concrete
stress of the steel plates
stress of the reinforcement
curvature of the RC beam
curvature of the steel plates

1. Introduction

Bolting steel plates to reinforced-concrete (RC) beams has become a widely accepted retrofitting technique over the past several decades due to the minimal additional space occupied and convenience of installation (Li, 2013). Furthermore, bolting steel plates can avoid serious debonding and peeling failures at the ends of the steel plates (Roberts and Haji-Kazemi, 1989; Souici et al., 2013; Su and Zhu, 2005) when compared with bonding steel plates or fibre-reinforced polymers with adhesive mortar (Adhikary et al., 2000; Buyukozturk et al., 2004; Hamoush and Ahmad, 1990).

Theoretically, steel plates can be bolted to either the soffit or the side faces of RC beams for strengthening purposes. Although attaching steel plates to the beam soffits can effectively increase the flexural strength and stiffness of a beam, it can lead to a substantial decrease in the ductility capacity of the strengthened beam due to over-reinforcement problems (Foley and Buckhouse, 1999; Roberts and Haji-Kazemi, 1989). To preserve the flexural ductility of the strengthened beam, steel plates anchored to the side faces of RC beams, the so-called bolted side-plating (BSP) technique (Hamoush and Ahmad, 1990; Subedi and Baglin, 1998), is preferred. Previous experimental studies (Li et al., 2013; Siu, 2009; Su et al., 2010) have demonstrated that BSP beams possess increased flexural strength without a notable decrease in the ductility capacity.

However, the behaviour of BSP beams is much more complex than that of bolting soffit plating beams, as it is controlled not only by longitudinal but also by transverse slips at the plate–RC interface (Johnson and Molenstra, 1991; Oehlers et al., 1997; Siu and Su, 2011). Local buckling of side-plated RC beams also needs to be taken into account (Smith et al., 1999a), and the effect of local buckling on the ultimate strength was assessed by a series of experiments (Smith et al., 1999b). A variation on the formulation of the Ritz method using linear combinations of harmonic functions was adopted for the consideration of the plate local buckling coefficients (Smith et al., 2000; Su et al., 2010). Siu and Su (2009) and Su and Siu (2007) developed numerical procedures for predicting the non-linear load–deformation response of bolt groups, and proposed an analytical model by introducing Newmark’s model (Newmark et al., 1951) to solve the longitudinal partial interaction of BSP beams under several symmetrical loading conditions (Siu, 2009; Siu and Su, 2010). Su et al. (2014) further extended this analytical model to handle more complicated asymmetrical loading conditions.

Li et al. (2013) and Su et al. (2013) conducted experimental and numerical studies to investigate the slip of steel plates. The transverse slip was found to be much smaller than the
longitudinal slip, and was very difficult to measure accurately in the tests. Various assumptions had been made by different researchers on the distribution of the transverse bolt shear, to simplify the complex nature of the transverse slips. By assuming that all shear connectors yielded in the longitudinal direction and that the shear connectors at the mid-span resisted all the vertical loads acting on the side-plate of simply supported BSP beams, Oehler et al. (1997) related the degree of transverse partial interaction with the elastic stiffness and the number of anchoring bolts utilised. Based on this model, Nguyen et al. (2001) derived a relationship between the longitudinal and transverse partial interactions. Li (2013) proposed a simplified piecewise linear shear transfer model based on the force superposition principle and simplification of shear transfer profiles derived from a previous numerical study (Su et al., 2013). The proposed model was capable of predicting transverse shear transfer behaviour during the entire loading process for BSP beams under four-point bending.

Siu and Su (2010) developed a two-alpha approach to analyse the sectional behaviour of BSP beams, in which the degree of partial interaction was measured in the longitudinal and the transverse directions by two indicators, as follows (see Figure 1 for details)

1. \[ \alpha_\varepsilon = \frac{\epsilon_p y_p}{\epsilon_c y_c} \leq 1 \]

2. \[ \alpha_\phi = \frac{\phi_p}{\phi_c} \leq 1 \]

where the strain factor \((\alpha_\varepsilon)\) is the ratio between the longitudinal strains of the steel plates and the RC beam \((\epsilon_p y_p, \epsilon_c y_c)\), respectively at the centroidal level of the steel plates \((y_p)\), and is used to indicate the degree of longitudinal partial interaction caused by the longitudinal slip \((S_\varepsilon)\). The curvature factor \((\alpha_\phi)\) is the ratio between the curvatures of the steel plates and the RC beam \((\phi_p, \phi_c)\), respectively, and is used to indicate the degree of transverse partial interaction caused by the transverse slip \((S_\phi)\). Lo et al. (2014) conducted a computer simulation to evaluate the performance of BSP beams by indicating the degree of partial interaction in terms of these two factors. The simulation revealed that the influence of the partial interaction on the overall performance was significant, and 90% of the full strengthening capacity was already achieved when the strain or the curvature factor was chosen to be no less than 0.6. This proposed value for the two factors is of great importance in simplifying the design procedure of BSP beams.

The aforementioned research findings demonstrate that the behaviour of BSP beams is very different from that of conventional RC beams and bonded side-plated RC beams. Hence, the traditional analysis and design methods of conventional RC beams are not applicable to BSP beams. In light of this situation, a new design procedure is proposed in this paper. First, the design formulas used to compute the flexural strength of conventional RC beams are modified by introducing the recommended optimum strain and curvature factors proposed by the authors (Lo et al., 2014), to take into account the partial interactions in both the longitudinal and transverse directions. Second, design equations are derived for estimating the dimensions of steel plates and the bolt arrangements. Finally, the maximum plate–RC slips and the minimum strain and curvature factors are back-checked (Li, 2013), to ensure that those factors and slips are within the recommended design limits. A worked example is given to illustrate the strengthening design of both lightly and moderately reinforced RC beams subjected to various loading arrangements.

2. Design model

2.1 Assumptions

When computing the ultimate moment resistance of a BSP beam section, the following assumptions are employed.

- The bond–slip effect of both tensile and compressive reinforcement is ignored; that is, the strain in the reinforcing bars is the same as that in the surrounding concrete.
- The cross-sections of both the steel plates and the RC beam remain in plane after deformation.
- The tensile strength of concrete is ignored; the compressive stress of concrete, and the tensile and compressive stresses in reinforcing steel and plate steel are derived from the design stress–strain relations given in the Eurocodes (BSI, 2004).
- The shear strength of anchor bolts can be computed according to the Eurocodes (BSI, 2005).

2.2 Material models

The stress–strain relation for the design of concrete material in the Eurocodes (BSI, 2004) is adopted, as shown in Figure 2.

\[ \sigma_c = \begin{cases} f_c & 0 \leq \epsilon_c \leq \epsilon_{\phi 0} \\ f_c \left[ 1 - \left( 1 - \frac{\epsilon_c}{\epsilon_{\phi 0}} \right)^2 \right] & \epsilon_{\phi 0} \leq \epsilon_c \leq \epsilon_{cu} \end{cases} \]
where $\sigma_c$ is the stress at strain $\varepsilon_c$, $\varepsilon_{c0}$ is the strain at the maximum strength $f_c$ and $\varepsilon_{cu}$ is the ultimate strain.

Both the reinforcement and steel plates are considered as elasto-plastic materials (BSI, 2004), as shown in Figure 3.

4. $\sigma_s = \begin{cases} E_s \varepsilon_s \quad |\varepsilon_s| < \varepsilon_y \\ f_y \quad |\varepsilon_s| \geq \varepsilon_y \end{cases}$ where $E_s = f_y/\varepsilon_y$

5. $\sigma_p = \begin{cases} E_p \varepsilon_p \quad |\varepsilon_p| < \varepsilon_{yp} \\ f_{yp} \quad |\varepsilon_p| \geq \varepsilon_{yp} \end{cases}$ where $E_p = f_{yp}/\varepsilon_{yp}$

As the failure of anchor bolts in shear is associated predominantly with limited ductility, a simple elastic shear force–slip relation is adopted for anchor bolts, as shown in Figure 4, and whose maximum slip in BSP beams should always be less than $S_{by}$

6. $R_b = K_b S \quad S \leq S_{by}$ where $\begin{cases} K_b = R_{by}/S_{by} \\ R_{by} = \alpha f_{ub} \pi d_b^2/4 \end{cases}$

where $f_{ub}$ and $d_b$ are the ultimate tensile strength and the nominal diameter of the anchor bolts, respectively, and $\alpha$ is a modifier with a value of 0·5 or 0·6 chosen in accordance with the Eurocodes (BSI, 2005).

2.3 Sectional analysis and flexural strength

It has been found (Lo et al., 2014) that 90% of the full strengthening capacity can be achieved when the strain or the curvature factor is chosen to be not less than 0·6. Therefore, for brevity, a unique value ($\alpha = 0·6$) is chosen for both $a_s$ and $a_p$.

7. $\alpha_s = \alpha_p = \alpha = 0·6$

Thus, the cross-sectional strain profile of the BSP beam in Figure 1(b) can be simplified, as illustrated in Figure 5(b). In order to obtain the flexural strength, the cross-sectional stress profile at the ultimate limit state is also illustrated in Figure 5(c). The concrete strain at the compressive surface reaches the ultimate strain $\varepsilon_{cu}$ and therefore the curvature of the RC beam can be expressed by the depth of the neutral axis ($c$) as

8. $\phi_c = \frac{\varepsilon_{cu}}{c}$

The strains of the compressive and tensile reinforcement can be written in terms of their depths ($h_c$ and $h_0$) as follows.

9. $\varepsilon_{cu} = \phi_c(c - h_c)$

10. $\varepsilon_{ut} = \phi_c(h_0 - c)$
The strains of the steel plates at their top and bottom edges are

11. \[ \varepsilon_{pt} = \alpha \varepsilon_{cu} (c - h_{pt}) \]

12. \[ \varepsilon_{pb} = \alpha \varepsilon_{cu} (h_{pb} - c) \]

For a satisfactory strengthening design, the outermost layer of the tensile reinforcement should yield before concrete crushing occurs; thus, its tensile stress is the yield strength \( f_y \) at the ultimate limit state. By substituting the strains in Equations 9–12 into the material constitutive relations, the internal sectional axial force \( N_u \) and bending moment \( M_u \) can be obtained. Furthermore, the pure bending condition should be satisfied as

\[
N_u = \eta f_y b c + E_p A_p \frac{\varepsilon_{cu}}{c} (c - h_c)
\]

\[
- f_y A_a + E_p A_p \frac{\varepsilon_{cu}}{c} (c - h_{pt})^2
\]

\[
- E_p A_p \frac{\varepsilon_{cu}}{c} (h_{pb} - c)^2 = 0
\]

where \( b \) is the breadth of the RC beam, \( \lambda \) is a factor defining the effective depth of the concrete compression zone and \( \eta \) is a factor defining the effective strength, as shown in Figure 5(c); values of 0.8 and 1.0 are adopted for \( \lambda \) and \( \eta \), respectively, if the concrete grade is lower than C50 according to the Eurocodes (BSI, 2004).

It can be seen that \( c \) is the only unknown in Equation 13; a solution of this quadratic equation to yield the neutral axis depth \( c \) is attainable as

\[
c = \frac{\sqrt{B^2 - 4AC} - B}{2A}
\]

where \[
\begin{align*}
A &= \eta f_y b \\
B &= E_p A_p \varepsilon_{cu} - f_y A_a + 2 E_p A_p \varepsilon_{cu} (h_{pb} - h_{pt}) \\
C &= - E_p A_p \varepsilon_{cu} h_c + E_p A_p \varepsilon_{cu} (h_{pb}^2 - h_{pt}^2)
\end{align*}
\]

Then, the ultimate moment resistance \( (M_u) \) can be expressed as

\[
M_u = \eta f_y b c^2 \left(1 - \frac{c^2}{h_c^2}\right) + E_p A_p \frac{\varepsilon_{cu}}{c} (c - h_c)^2 + f_y A_a (h_0 - c) + \frac{2}{3} E_p A_p \frac{\varepsilon_{cu}}{c} (h_{pb} - c)^3
\]

2.4 Verification by experimental results

For a BSP beam subjected to four-point bending, the peak load can be expressed conveniently as \( F_p = 2M_d L_s \) (where \( L_s \) is the shear span). The results extracted from a previous experimental study (Li et al., 2013) were employed to verify the aforementioned sectional analysis method, as shown in Table 1. It is evident that the proposed sectional analysis method can predict the peak load of the specimens with a satisfactory mean discrepancy of approximately 5.2%.
In most cases of a real strengthening design of BSP beams, yielding occurs at the compressive reinforcement and the bottom edge of steel plates but not on the top edge of the steel plates (i.e. $\varepsilon_{\text{sc}} > \varepsilon_{\text{pb}}$ and $\varepsilon_{\text{pt}} < \varepsilon_{\text{yp}}$); thus, the design flexural strength ($M_u$) can be determined as

$$M_u = \frac{1}{\gamma_c} \eta f_{i} b \lambda c^2 \left(1 - \frac{\lambda}{2}\right) + \frac{1}{\gamma_t} \left[E_i A_i \frac{c}{c} \left(e - h_c\right)^2 \right] + f_s A_s (h_0 - c) + \frac{1}{\gamma_s} \left(2 f_y t \left(\frac{c}{\lambda} + \frac{e_{\text{sc}}}{\lambda_{\text{cu}}}ight) \right)^3 \left(\frac{h_{\text{pb}}}{c} - c\right)^2 - \frac{1}{3} \left(\frac{c_{\text{sc}}}{\lambda_{\text{cu}} \lambda_{\text{pt}}}ight)^2 \}
$$

where $M_{ci}$ and $\gamma_c$ are the partial factors for the concrete and steel material, respectively.

In some cases, yielding also occurs at the top edge of the steel plates (i.e. $\varepsilon_{\text{pt}} > \varepsilon_{\text{yp}}$), and thus the design flexural strength ($M_u$) can be determined as

$$M_u = \frac{1}{\gamma_c} \eta f_{i} b \lambda c^2 \left(1 - \frac{\lambda}{2}\right) + \frac{1}{\gamma_t} \left[E_i A_i \frac{c}{c} \left(e - h_c\right)^2 \right] + f_s A_s (h_0 - c) + \frac{1}{\gamma_s} \left(2 f_y t \left(\frac{c}{\lambda} + \frac{e_{\text{sc}}}{\lambda_{\text{cu}}}ight) \right)^3 \left(\frac{h_{\text{pb}}}{c} - c\right)^2 - \frac{2}{3} \left(\frac{c_{\text{sc}}}{\lambda_{\text{cu}} \lambda_{\text{pt}}}ight)^2 \}
$$

where the coefficients $\gamma_c$ and $\gamma$ are the partial factors for the concrete and steel material, respectively.
20. where

\[
\begin{align*}
A &= \frac{1}{\gamma_b} \left[ \eta_c h_b + \frac{1}{\gamma_s} \right] \\
B &= \frac{1}{\gamma_s} \left[ 2f_{yp} (h_{pb} + h_{pe}) + f_y (A_{at} - A_{wc}) \right]
\end{align*}
\]

It is noted that in the simplified design procedure both the target strain and curvature factors may be taken as \( \alpha = 0.6 \) in Equations 17–20. A trial-and-error procedure might be needed to determine the plate thickness (\( t_b \)) by implementing the prerequisite that the design flexural strength \( (M_a) \) should be greater than the bending moment \( (M_d) \) caused by external loads; that is

\[ M_a \geq M_d \]

21. After evaluating the limitation of the size of steel plates, the thickness and depth (i.e. \( 2t_b \) and \( D_0 \)) of the steel plates can be chosen from the practical and available inventory. The type and transverse slips between the steel plates and the RC beams, should be checked in terms of the maximum longitudinal and transverse slips \( (S_{lc,max} \text{ and } S_{tc,max}) \), and the minimum strain and curvature factors \( (\alpha_{e,min} \text{ and } \alpha_{p,min}) \), as follows.

\[
\sqrt{S_{lc,max}^2 + S_{tc,max}^2} \leq S_{by}
\]

22. Estimation of the number of bolts

To ensure the occurrence of ductile axial yielding of plates prior to the brittle shear failure of bolts, the number of anchor bolts \( (n_b) \) can be estimated by the inequality

\[
\frac{1}{4} \frac{R_{by}}{\gamma_{M2}} \geq \frac{f_y (h_{pb} - h_{pe}) t_b}{\gamma_s}
\]

where \( R_{by} \) is the yield shear force of an anchor bolt (see Equation 6); \( \gamma_{M2} \) is the partial safety factor for bolts, with a value of 1.25 recommended by the Eurocodes (BSI, 2005); and \( \gamma_s \) is a coefficient that takes into account the varying distribution of bolt shear force along the beam span. A value for \( \gamma_s \) from 1.5 to 2.0 can be chosen, because the shear transfer profiles are between triangular and parabolic, as shown in the literature (Li, 2013). The leading constant 1/4 on the left-hand side of the equation is adopted as there are two steel plates and two shear spans for each plate in a BSP beam.

23. Verification of the partial interaction

The partial interaction, which is caused by the longitudinal and transverse slips between the steel plates and the RC beams, is highly dependent not only on the beam geometry but also on the load arrangement, and, thus, should be verified according to each specific case.

24. The expressions for \( S_{lc,max} \) and \( S_{tc,max} \) are mainly controlled by the depth of the steel plates used in BSP beams (Li, 2013). The steel plates in a BSP beam retrofit the RC beam by both their flexural stiffness \( \phi_F EI_p \) and the additional eccentric-compression-force effect \( \phi_D N_p \). The proportions of these two effects can be identified by the modulus ratio \( I_p : A_p c_p^2 \), which is the ratio between the second moment of the area of the steel plates with regard to the plate centroid \( (I_p) \) and the RC centroid \( (A_p c_p^2) \), as shown in Figure 7.

\[
I_p : A_p c_p^2 = \frac{2f_y D_1}{12} : \frac{2f_y D_2}{3} (\frac{D_0}{3})^2 = \frac{1}{12} \frac{D_0}{D_2} < \frac{1}{3}
\]

For shallow steel plates with a depth \( D_p / D_2 < 1/3 \), the modulus ratio \( I_p : A_p c_p^2 \) is less than 1/12; thus, the error caused by neglecting the flexural stiffness \( (EI_p) \) and treating the plates as additional tensile reinforcement bars might be acceptable. However, for deep steel plates with a depth \( D_p / D_2 > 1/2 \), the modulus ratio \( I_p : A_p c_p^2 \) is greater than 1/3; thus, their flexural stiffness can no longer be ignored.

25. For a BSP beam under four-point bending, the maximum longitudinal and transverse slips occur at the plate end, the minimum strain factor occurs at the loading point and the minimum curvature factor occurs at the midspan. Their magnitudes are given by the expressions (Li, 2013)

\[
S_{lc,max} |_{x=0} = \frac{F_{tcp}}{p^2 (EI_p) \left[ 1 + \frac{1}{2 \cos h(pL/3) - 1} \right]}
\]

\[
S_{tc,max} |_{x=0} = \left\{ \begin{array}{ll}
\frac{FL^3}{(EI)_c} 0.032L^2 \beta_y (1 + \beta_p^{-1}) - 44.4 & \frac{D_p}{D_2} < \frac{1}{3} \\
\frac{FL^3}{(EI)_c} 0.025L^2 \beta_y (1 + \beta_p^{-1}) - 44.4 & \frac{D_p}{D_2} > \frac{1}{2}
\end{array} \right.
\]

\[
\frac{D_p}{D_2} > \frac{1}{2}
\]
Definition of (a) shallow and (b) deep steel plates

For a BSP beam under a uniformly distributed load, the maximum longitudinal and transverse slips occur at the plate end, and the minimum strain and curvature factors occur at the midspan. Their magnitudes are given by the expressions (Li, 2013)

\[ \alpha_{s,\min} |_{x=L/3} = \left( 1 + \frac{(EA)p}{k_m} \right) \left( \frac{L[L\cos h(pL/3)-1]}{3p \sin h(pL/3)} - (1/p^2) \right) \]

\[ \alpha_{p,\min} |_{x=L/2} = \begin{cases} 18 + 0.8 \beta_p &- 2500 \beta_p - 6500 \beta_p - 1 \beta_p \left( \frac{D_p}{D_c} \right) < \frac{1}{3} \\ 36 + 2.7 \beta_p &- 6500 \beta_p - 1 \beta_p \left( \frac{D_p}{D_c} \right) > \frac{1}{2} \end{cases} \]

\[ S_{u,\max} |_{x=0} = \frac{q k_p}{p^3[EI]_c + (EI)_p} \left[ \frac{pL}{2} - \tan h \left( \frac{pL}{2} \right) \right] \]

\[ S_{u,\max} |_{x=0} = \frac{\xi_S q L^4}{L^4p^m(EI)_c} \]

\[ \alpha_{s,\min} |_{x=L/2} = \left( 1 + \frac{(EA)p}{k_m} \right) \left( \frac{L^2/8[1 - \sec h(pL/2)]}{(1/p^2)} \right) \]

\[ \alpha_{p,\min} |_{x=L/2} = \begin{cases} 0.72 L^4p^m \left[ 5400 \beta_p + L^4p^m(\beta_p + 1) \right] / D &\frac{D_p}{D_c} < \frac{1}{3} \\ 0.63 L^4p^m \left[ 10300 \beta_p + L^4p^m(\beta_p + 1) \right] / D &\frac{D_p}{D_c} > \frac{1}{2} \end{cases} \]

3.4 General strengthening strategies and preliminary design

The flexural strength of an RC beam can be simply expressed as

\[ M = (f_s/g)A_s d_{ci} \]

where \( d_{ci} \) is the lever arm controlled by the depth of the beam \( (h) \). Therefore, the flexural strength of an RC beam can be enhanced by increasing either the strength of tensile reinforcement \( (f_s A_s) \) or the depth of the beam \( (h) \). In the structural design, either of these two measures can be used, but the measures are highly controlled by the position of each RC beam within the whole structure. Figure 8 shows different types of RC beams in a typical plan and elevation layout of an...
RC building. Figure 9 presents the available BSP strengthening schemes for different types of RC beams.

As an under-reinforced beam performs differently for different tensile steel ratios, the following definition of lightly and moderately reinforced beams is adopted in the subsequent discussion. A lightly reinforced beam, whose tensile steel ratio is less than 1/3 of the balance steel ratio (\(\rho_{st} < (1/3)\rho_{stb}\)), fails in a ductile mode. In most cases, its flexural strength is less than 40% of that of the balanced reinforced beam; thus, it can be enhanced significantly by adding external reinforcement, with a small sacrifice in ductility. In contrast, a moderately reinforced beam, whose reinforced degree is greater than 2/3 (\(\rho_{st} \rho_{stb} > 2/3\)), fails in a brittle mode. Its flexural strength is usually more than 80% of that of the balanced reinforced beam; thus, adding external tensile reinforcement cannot increase its flexural strength significantly but can cause a very brittle failure with little ductility.

As shown in Figure 8, type 1 beams are usually main girders with a very large clear span. Large clear heights are typically not required because the space under these beams is usually occupied by infilled walls or furniture. However, the external loads imposed on these beams are usually of great magnitude, including those transferred from floor slabs, secondary beams and infilled walls. Furthermore, as the ductility capacity principle of 'strong column, weak beam' is usually required for main girders by design codes, a steel ratio of less than 2/3 of the balance steel ratio (\(\rho_{st} < (2/3)\rho_{stb}\)) is usually preferable. Therefore, type 1 beams are usually designed with a large beam depth, but are lightly reinforced to achieve significant flexural strength and ductility. Although the depth of the beam is great, there are limited areas on the side faces for use of the side-bolted steel plates, due to connections with secondary beams. When a load-bearing capacity greater than the original design is required, the strengthening technique of BSP beams with shallow steel plates is especially suitable for type 1 beams, as shown in Figure 9(a). The shallow steel plates serve as additional external tensile reinforcement, and increase the degree of reinforcement, thus enhancing the flexural strength. The main failure mode of type 1 beams strengthened with shallow steel plates is the yielding of the tensile reinforcement and the bolted plates.

The degree of strengthening of type 1 beams is governed by the difference between the current steel ratio and the preferred steel ratio (\((2/3)(\rho_{stb} - \rho_{st})\)). This is because, although thicker steel plates can always be chosen to achieve greater reinforcement, the required ductility capacity in the design code should always be guaranteed. The available area on the side faces is also a parameter controlling the strengthening effect. This is because the degree of partial interaction is limited by the available number of anchor bolts, which is mainly governed by the available side face area, as the minimum bolt spacing is strictly regulated in the design codes.

As shown in Figure 8, type 2 beams are usually secondary beams or main girders with a shorter beam span and are subjected to lighter external loads. For these beams, large clear heights below the beams are usually required for the installation of equipment, pipelines and ceilings. Therefore, type 2 beams are usually designed to be shallow with a modest beam depth, but are moderately reinforced with large tensile reinforcement (\(A_{st}\)). For type 2 beams, using deep steel plates can increase both their tensile and compressive reinforcement, and thus enhance their flexural strength without any notable reduction in ductility, as shown in Figure 9(b).

As the use of deep steel plates increases both the tensile and compressive reinforcement, the tensile steel ratio (\(\rho_{st}\)) is no longer an obstacle to the strengthening effect of type 2 beams.
The available side face area becomes the key parameter, as it controls both the available plate depth and the maximum number of anchor bolts.

Lastly, buckling in the compressive region of the deep steel plates is the greatest potential risk for type 2 strengthened beams. It should be suppressed by taking appropriate measures, such as increasing the number of anchor bolts, or installing or welding steel angles to the compressive edge of the steel plates.

4. Worked example

4.1 Current state of the structure requiring strengthening

For brevity and illustration, let us assume that Figure 8(a) shows the plan layout of a prefabricated RC structure factory building, and that all beams are simply supported. The originally designed live load was 5 kN/m², but this now needs to be increased to 12 kN/m² as a result of a change in use. Therefore, proper retrofitting measures should be applied to the structure. For illustration, only the strengthening designs of a main girder and a secondary beam, labelled beam 1 and beam 2 in Figure 8(a), are discussed herein. Simplified models are shown in Figure 10, and the section details are given in Figure 11.

The originally designed loads before any change in use can be computed as

\[ F_1 = 219 \text{ kN} \quad q_2 = 32.8 \text{ kN} \text{ m} \]

Thus, the originally designed moments on beams 1 and 2 are

\[ M_{d1} = 525.7 \text{ kN m} \quad M_{d2} = 147.6 \text{ kN m} \]

The designed material properties are

\[ f_{ck} = 30 \text{ MPa} \quad f_y = 460 \text{ MPa} \quad E_s = 200 \text{ GPa} \]

The section properties of beams 1 and 2, respectively, are

\[ h_{0,1} = 667 \text{ mm} \quad A_{0,1} = 232,050 \text{ mm}^2 \quad A_{sc,1} = 942 \text{ mm}^2 \]
\[ \rho_{st,1} = 1.06\% \]
\[ h_{0,2} = 367 \text{ mm} \quad A_{0,2} = 72,600 \text{ mm}^2 \quad A_{sc,2} = 632 \text{ mm}^2 \]
\[ A_{st,1} = 1,256 \text{ mm}^2 \quad \rho_{st,2} = 1.73\% \]

The original flexural strengths of beams 1 and 2 can be computed by using the design formulas in the Eurocodes (BSI, 2004) as

\[ M_{d1} = 615.2 \text{ kN m} \quad M_{d2} = 166.1 \text{ kN m} \]

Therefore, the originally designed structure is safe before a change in use for bearing moments less than the flexural strengths, as follows

\[ M_{d1} = 525.7 \text{ kN m} < M_{d1} = 615.2 \text{ kN m} \]

\[ M_{d2} = 147.6 \text{ kN m} < M_{d2} = 166.1 \text{ kN m} \]

However, as the live load increases to 12 kN/m² due to a change in use, the actual loads are

\[ F_1 = 380.3 \text{ kN m} \quad q_2 = 59.7 \text{ kN} \text{ m} \]
Thus, the design moments on beams 1 and 2 increase significantly, as follows

46.  \( M_{d,1} = 912.8 \, \text{kN} \, \text{m} \quad M_{d,2} = 268.5 \, \text{kN} \, \text{m} \)

Therefore, the original RC beams 1 and 2 are unsafe following a change in use, because the design moments are much greater than the flexural strengths, as follows

47.  \( M_{d,1} = 912.8 \, \text{kN} \, \text{m} \gg M_{\text{Flex},1} = 615.2 \, \text{kN} \, \text{m} \)

48.  \( M_{d,2} = 268.5 \, \text{kN} \, \text{m} \gg M_{\text{Flex},2} = 166.1 \, \text{kN} \, \text{m} \)

4.2 Arrangement of steel plates

As the top part of the side faces of beam 1 is occupied by the secondary beams, and only the bottom part is available for the installation of steel plates, a shallow plate depth of \( D_{p,1} = 250 \, \text{mm} \) is chosen. On the other hand, considering the moderate steel ratio \( (\rho_{u,2} = 1.73\%) \) of beam 2, the largest possible plate depth of \( D_{p,2} = 300 \, \text{mm} \) is chosen. A trial plate thickness of \( t_p = 6 \, \text{mm} \) is also chosen for both beams, and can be adjusted accordingly where insufficient flexural strength is proved.

By taking the optimum strain and curvature factors \( \alpha = 0.6 \) and using Equations 17 and 18, the designed flexural strengths can be computed for beams 1 and 2, respectively, as

49.  
\[
A_1 = 1.420 \times 10^4 \quad B_1 = -5.973 \times 10^5 \\
C_1 = 5.380 \times 10^5 \quad c_1 = 289 \, \text{mm}
\]

50.  \( \Rightarrow M_{\text{ub},1} = 1039.7 \, \text{kN} \, \text{m} \)

\[
\begin{cases}
\varepsilon_{\text{ac}} = 0.0031 > \varepsilon_y = 0.002 \\
-\varepsilon_{\text{pt}} = 0.0011 < \varepsilon_{\text{yp}} = 0.0017 \\
\varepsilon_{\text{pb}} = 0.0029 > \varepsilon_{\text{yp}} = 0.0017
\end{cases}
\]

\( \Rightarrow \) Equations 17 and 18 are suitable

51.  
\[
A_2 = 1.180 \times 10^4 \quad B_2 = -2.181 \times 10^6 \\
C_2 = 2.651 \times 10^5 \quad c_2 = 199 \, \text{mm}
\]

52.  \( \Rightarrow M_{\text{ub},2} = 277.7 \, \text{kN} \, \text{m} \)

53.  \( \Rightarrow M_{\text{ub},2} = 277.7 \, \text{kN} \, \text{m} \)

54.  \[
\begin{cases}
\varepsilon_{\text{ac}} = 0.0029 > \varepsilon_y = 0.002 \\
\varepsilon_{\text{pt}} = 0.0010 < \varepsilon_{\text{yp}} = 0.0017 \\
\varepsilon_{\text{pb}} = 0.0023 > \varepsilon_{\text{yp}} = 0.0017
\end{cases}
\]

\( \Rightarrow \) Equations 17 and 18 are suitable

Thus, beams 1 and 2 are safe after a change in use, as the bearing moments are less than the flexural strengths, as follows

55.  \( M_{d,1} = 912.8 \, \text{kN} \, \text{m} < M_{\text{ub},1} = 1039.7 \, \text{kN} \, \text{m} \)

56.  \( M_{d,2} = 268.5 \, \text{kN} \, \text{m} < M_{\text{ub},2} = 277.8 \, \text{kN} \, \text{m} \)

Furthermore, it is evident from Equation 51 that the top edge of the shallow steel plates are inverse to our pre-set sign convention, which means that all sections of the shallow steel plates are subjected to a tension force.

4.3 Arrangement of anchor bolts

Anchor bolts of grade 5.8 (\( f_{\text{ub}} = 500 \, \text{MPa} \), \( S_{\text{by}} = 1.5 \, \text{mm} \)) with a diameter of 12 mm can be chosen for this strengthening design. The yield shear force of an anchor bolt is

57.  \( R_{\text{by}} = 0.5 \times 500 \times \pi \times \frac{12^2}{4} = 28.3 \, \text{kN} \)

Substituting Equation 57 and the geometry and material properties of the steel plates into Equation 22 gives the estimated number of anchor bolts as, respectively

58.  \[
\frac{1}{4} n_{b,1} = 2.0 \times \frac{(1/1.15) \times 355 \times (700 - 450) \times 6}{(1/1.25) \times 28.3 \times 10^3} = 41 \, \text{pieces}
\]

59.  \[
\frac{1}{4} n_{b,2} = 2.0 \times \frac{(1/1.15) \times 355 \times (400 - 100) \times 6}{(1/1.25) \times 28.3 \times 10^3} = 50 \, \text{pieces}
\]

Because the depth of the steel plates for beam 1 is 250 mm, two rows of anchor bolts can be used, and the corresponding
computed bolt spacing is

60. \[ S_{b1} = \frac{7200}{241/2} = 176\, \text{mm} \]

Of course, the computed bolt spacing is an approximate estimation, and two rows of bolts with a bolt spacing of \( S_{b1} = 150\, \text{mm} \) is actually chosen for fabrication convenience; thus, the total number of bolts for beam 1 is

61. \[ n_{b1} = 2 \times 2 \times \left( \frac{7200}{150} + 1 \right) = 196 \text{ pieces} \]

Because the depth of steel plates for beam 2 is 300 mm, three rows of anchor bolts can be used, and the corresponding computed bolt spacing is

62. \[ S_{b2} = \frac{7200}{50/3} = 216\, \text{mm} \]

For fabrication convenience, three rows of bolts with a bolt spacing of \( S_{b2} = 150\, \text{mm} \) are actually chosen; thus, the total number of bolts for beam 2 is

63. \[ n_{b2} = 2 \times 3 \times \left( \frac{7200}{150} + 1 \right) = 296 \text{ pieces} \]

The bolt spacing in the vertical direction can be arranged to correspond with the steel structure design codes, and the final strengthening layouts are shown in Figure 11.

4.4 Verification of partial interaction

The stiffnesses of the RC beams, the steel plates and the bolt connections, along with the corresponding stiffness ratios, are computed according to their geometry and material properties for beams 1 and 2 as, respectively

64. \[
\begin{align*}
(EA)_{p1} &= 6.30 \times 10^8\, \text{N} \\
(EL)_{p1} &= 3.28 \times 10^{12}\, \text{N mm}^2 \\
\beta_{p1} &= 6.30 \times 10^8 \quad 1.66 \times 10^7 = 0.38 \\
\beta_{p1} &= 3.28 \times 10^{12} \\
9.04 \times 10^{13} = 0.036
\end{align*}
\]

65. \[
\begin{align*}
(EA)_{p2} &= 7.56 \times 10^8\, \text{N} \\
(EL)_{p2} &= 5.67 \times 10^{12}\, \text{N mm}^2 \\
\beta_{p2} &= 7.56 \times 10^8 \quad 6.91 \times 10^7 = 1.09 \\
\beta_{p2} &= 5.67 \times 10^{12} \quad 1.25 \times 10^{13} = 0.454
\end{align*}
\]

66. \[ K_b = \frac{28.3 \times 10^3}{1.5} = 18900\, \text{N/mm} \]

67. \[
\begin{align*}
\beta_{m1} &= 2 \times 18900 \quad 150 = 251\, \text{N/mm}^2 \\
\beta_{m2} &= 9.04 \times 10^{13} = 2.78 \times 10^{-12}\, \text{mm}^{-4}
\end{align*}
\]

68. \[
\begin{align*}
\beta_{m2} &= 3 \times 18900 \quad 150 = 378\, \text{N/mm}^2 \\
\beta_{m2} &= 3.0 \times 10^{-11}\, \text{mm}^{-4}
\end{align*}
\]

The parameters \( p \) and \( \xi_p \), which are used for computation of the longitudinal slips and strain factors, can be computed for beams 1 and 2 as, respectively

69. \[ i_{c1} = 234\, \text{mm} \quad i_{p1} = 72\, \text{mm} \quad i_{p1} = 225\, \text{mm} \]

70. \[ i_{c2} = 135\, \text{mm} \quad i_{p2} = 87\, \text{mm} \quad i_{p2} = 50\, \text{mm} \]

71. \[ p_1 = \sqrt{2.78 \times 10^{-12} \left( \frac{234^2 + 72^2}{0.036 + 1} + 225^2 \right)} = 8.28 \times 10^{-4} \]

72. \[ p_1 = \sqrt{2.78 \times 10^{-12} \left( \frac{234^2 + 72^2}{0.036 + 1} + 225^2 \right)} = 8.28 \times 10^{-4} \]

73. \[ L_1 = 7200\, \text{mm} \quad L_2 = 6000\, \text{mm} \]

The peak loads for beams 1 and 2 can be derived from the ultimate flexural strength \( (M_u) \) as

74. \[ F_{p1} = \frac{1039.7}{7.2/3} = 433.1\, \text{kN} \]
Then, the maximum longitudinal slips ($S_{l,max}$) at the peak loads can be obtained for beams 1 and 2 by using Equations 26 and 30, respectively.

76. $S_{l,max,1}|_{x=0} = 1.47 \text{ mm} \quad S_{l,max,2}|_{x=0} = 0.31 \text{ mm}$

The maximum transverse slips ($S_{r,max}$) at the peak loads can also be obtained for beams 1 and 2, by using Equations 27 and 31, respectively.

77. $S_{r,max,1}|_{x=0} = 0.26 \text{ mm} \quad S_{r,max,2}|_{x=0} = 1.11 \text{ mm}$

Therefore, the resultant slips can be verified as follows

78. $\zeta = 25L^2q_p \beta_p^2 \left[ \frac{2}{3} \frac{1}{2} + L^2 \beta_p^2 (\beta_p + 1) \right] / C = 6.90$

79. $C_2 = L^4 q_p \beta_p^2 (\beta_p + 1)^2 + 16900 \beta_p$

Therefore, the resultant slips can be obtained for beams 1 and 2, by using Equations 28, 29, 32 and 33, respectively.

80. $D_2 = L^2 q_p \beta_p^2 (\beta_p + 1) (\beta_p + 0.65) + 14600 \beta_p$

It is evident from Equations 81–86 that the maximum resultant slips and the minimum strain and curvature factors can satisfy the requirements, despite the minimum curvature factors being slightly less than the required limit. This strengthening arrangement will still be acceptable, owing to the conservatism in the flexural strengths (see Equations 55 and 56) and the insensitive variation of the flexural strength as the strain and curvature factors when $\alpha_{e,min}$ and $\alpha_{r,min}$ are greater than 0·5, as mentioned in the literature (Li, 2013). Of course, further computation shows that the actual flexural strengths of beams 1 and 2 ($M_{uBSP,1}$ and $M_{uBSP,2}$, based on the actual $\alpha_{e,min}$ and $\alpha_{r,min}$) are still conservative. For brevity, the computation is omitted, and the results are

87. $M_{d,1} = 912.8 \text{ kNm} < M_{uBSP,1} = 1037.1 \text{ kNm}$

88. $M_{d,2} = 268.5 \text{ kNm} < M_{uBSP,2} = 275.3 \text{ kNm}$

4.5 Discussion of the strengthening effectiveness and efficiency

Taking $M_d$ and $M_{d'}$ to be the design moments before and after a change in use and $M_{uBSP}$ and $M_{uBSP'}$ to be the flexural strengths before and after strengthening, the corresponding design safety margins and enhancement percentages are tabulated in Table 2. The flexural strengths under a full-interaction assumption ($M_{uBSP,F1}$), together with the corresponding design safety margins and enhancement percentages, are also computed for comparison.

The original flexural strengths of beams 1 and 2 are much lower than the required design moments after a change in use (the design safety margins are 0·67 and 0·62, respectively), and thus both beams need to be strengthened (the required enhancements are 48% and 62%, respectively). After appropriate strengthening is employed (see Figure 11), the actual enhancements are greater than the requirements (69% > 48% and 66% > 62%, respectively), and thus the structure is safe (the design safety margins are 1·14 and 1·03, respectively).
It is also evident that the utmost enhancements when a full interaction assumption is employed are just slightly greater than the actual enhancements (71% > 69% and 73% > 66% for beams 1 and 2, respectively). Strength losses due to partial interaction are negligible (only 1% and 4%, respectively), and the actual strengthening capacity is greater than 90% of the full strengthening capacity, and thus is very satisfactory (97% and 90%, respectively). Therefore, the stiffness of the bolt connection is sufficient, and it is neither necessary nor economical to arrange too many anchor bolts in the strengthening of these two BSP beams.

5. Conclusions

In this paper, a new flexural design procedure has been proposed for strengthening of RC beams using the BSP technique. The modified flexural strength design formulas, which involve the influence of partial interaction, are presented. By adopting some optimum strain and curvature factors in the flexural capacity checking of BSP beams, the plate dimensions and the bolt arrangement can be determined. The main findings of this study can be summarised as follows.

- The load capacity of BSP beams would be overestimated if an assumption of full interaction was employed in the calculation. On the other hand, more accurate results can be obtained by taking the partial interaction in the plate–RC interface into account.
- The strain and curvature factors are used to quantify the longitudinal and transverse partial interaction. Only minor modification is needed for the conventional flexural strength formula of RC beams to cover the computation of the flexural strength of BSP beams, by employing the recommended strain and curvature factors.
- A strain or curvature factor of 0.6 can attain optimal enhancement with a reasonable number of anchor bolts; excessive connection is neither economical nor necessary.
- The recommended strain and curvature factors facilitate the strengthening design considerably, by dividing the design procedure into two parts: (a) evaluation of the plate size using the modified flexural strength formulas; (b) evaluation of the required number of bolts by the plate size, followed by verification of the degree of partial interaction using the simplified formulas.
- The worked example shows the effectiveness and efficiency of the proposed design procedure in the strengthening design of RC beams using the BSP technique. This new design approach is not only easy to use but also offers greater accuracy than design methods using the assumption of full interaction.

Acknowledgements

The research described here received financial support from the Research Grants Council of the Hong Kong SAR (Project No. HKU7166/08E and HKU7151/10E) and the National Natural Science Foundation of China (Project No. 51408436).

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