Search for a Light Sterile Neutrino at Daya Bay

cosmology. Sterile neutrinos with eV or sub-eV mass have been shown to help reconcile the tensions in the cosmological data between neutrinos, their presence could be detected via the modification to the latter oscillatory behavior. Various searches for active-sterile neutrino mixing in the mass-squared splitting $|\Delta m^2_{31}| \lesssim 0.1 \text{ eV}^2$ region, which was largely unexplored.

Measurements in the past decades have revealed large mixing between the flavor and mass eigenstates of neutrinos. The neutrino mixing framework [1–3] with three flavors has been successful in explaining most experimental results, and several-percent precision has been attained in the determination of the neutrino mixing angles and the mass splittings. Despite this great progress, there is still room for other generations of neutrinos to exist. Fits to precision electroweak measurements [4,5] have limited the number of light active neutrino flavors to three, although other light neutrinos may exist as long as they do not participate in standard V-A interactions. These neutrinos, which arise in extensions of the standard model that incorporate neutrino masses, are typically referred to as sterile neutrinos [2].

In addition to being well motivated from the theoretical standpoint, sterile neutrinos are among the leading candidates to resolve outstanding puzzles in astronomy and cosmology. Sterile neutrinos with $\sim$keV masses are good candidates for nonbaryonic dark matter [6,7]. Light sterile neutrinos with eV or sub-eV mass have been shown to help reconcile the tensions in the cosmological data between current measurements of the present and early Universe [8] as well as between cosmic microwave background and lensing measurements [9]. The recent $B$-mode polarization data from BICEP2 [10] has spurred even more discussion in this area [11–14].

If light sterile neutrinos mix with the three active neutrinos, their presence could be detected via the modification to the latter’s oscillatory behavior. Various searches for active-sterile neutrino mixing in the mass-squared splitting $|\Delta m^2_{31}| \lesssim 0.1 \text{ eV}^2$ region have been carried out in this way. The LSND [15] and MiniBooNE [16,17] experiments observed excesses of electron (anti-)neutrino events in their muon (anti-)neutrino beams, which could be interpreted as sterile neutrino oscillation with $|\Delta m^2| \sim 1 \text{ eV}^2$. However, these results are in tension [18–21] with the limits derived from other appearance [22–25] or disappearance searches [26–36]. Moreover, a reanalysis of the measured vs predicted electron antineutrino events from previous reactor experiments has revealed a deficit of about 6% [37,38]. Although the significance of this effect is still under discussion [39,40], it is compatible with the so-called gallium anomaly [41–43] in that both

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can be explained by introducing a sterile neutrino with $|\Delta m^2| > 0.5$ eV$^2$ [44]. Until now, however, the $|\Delta m^2| < 0.1$ eV$^2$ region has remained largely unexplored.

This Letter describes a search for a light sterile neutrino via its mixing with the active neutrinos using more than 300,000 reactor antineutrino interactions collected in the Daya Bay Reactor Antineutrino Experiment. This data set was recorded during the six-detector data period from December 2011 to July 2012. Since the antineutrino detectors are located at baselines ranging from a few hundred to almost two thousand meters away from the reactor cores, Daya Bay is most sensitive to active-sterile neutrino mixing in the $10^{-3}$ eV$^2 < |\Delta m^2| < 0.3$ eV$^2$ range. In this region, a positive signal for active-sterile neutrino mixing would predominantly manifest itself as an additional spectral distortion with a frequency different from the one due to the atmospheric mass splitting.

This work used a minimal extension of the standard model: the 3(active) + 1(sterile) neutrino mixing model. In this model, if the neutrino mass is much smaller than its momentum, the probability that an $\bar{\nu}_e$ produced with energy $E$ is detected as an $\bar{\nu}_e$ after traveling a distance $L$ is given by

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - 4 \sum_{i=1}^{3} \sum_{j>i}^{4} |U_{ei}|^2 |U_{ej}|^2 \sin^2 \Delta_{ij}. \tag{1}$$

Here $U_{ei}$ is the element of the neutrino mixing matrix for the flavor eigenstate $\nu_e$ and the mass eigenstate $\nu_i$. $\Delta_{ji} = 1.267 \Delta m^2_{ji} (\text{eV}^2) [L(\text{m})/E(\text{MeV})]$ with $\Delta m^2_{ji} = m_j^2 - m_i^2$ being the mass-squared difference between the mass eigenstates $\nu_j$ and $\nu_i$. Using the parametrization of Ref. [34], $U_{ei}$ can be expressed in terms of the neutrino mixing angles $\theta_{14}$, $\theta_{13}$, and $\theta_{12}$,

$$U_{e1} = \cos \theta_{14} \cos \theta_{13} \cos \theta_{12},$$
$$U_{e2} = \cos \theta_{14} \cos \theta_{13} \sin \theta_{12},$$
$$U_{e3} = \cos \theta_{14} \sin \theta_{13},$$
$$U_{e4} = \sin \theta_{14}. \tag{2}$$

If $\theta_{14} = 0$, the probability returns to the expression for three-neutrino oscillation.

The Daya Bay experiment has two near underground experimental halls (EH1 and EH2) and one far hall (EH3). Each hall houses functionally identical, three-zone antineutrino detectors submerged in pools of ultrapure water segmented into two optically decoupled regions. The water pools are instrumented with photomultiplier tubes to tag cosmic-ray-induced interactions. Reactor antineutrinos were detected via the inverse $\beta$-decay (IBD) reaction ($\bar{\nu}_e + p \rightarrow e^+ + n$). The coincidence of the prompt ($e^+$ ionization and annihilation) and delayed ($n$ capture on Gd) signals efficiently suppressed the backgrounds, which amounted to less than 2% (5%) of the entire candidate samples in the near (far) halls [45]. The prompt signal measured the $\bar{\nu}_e$ energy with an energy resolution $\sigma_E/E \approx 8\%$ at 1 MeV. More details on the reconstruction and detector performance can be found in Ref. [46]. A summary of the IBD candidates used in this analysis, together with the baselines of the three experimental halls to each pair of reactors, is shown in Table I.

The uncertainty in the absolute energy scale of positrons was estimated to be about 1.5% through a combination of the uncertainties of calibration data and various energy models [45]. This quantity had a negligible effect on the sensitivity of the sterile neutrino search due to the relative nature of the measurement with functionally identical detectors. The uncertainty of the relative energy scale was determined from the relative response of all antineutrino detectors to various calibration sources that spanned the IBD positron energy range, and was found to be 0.35%. The predicted $\bar{\nu}_e$ flux took into account the daily live-time-corrected thermal power, the fission fractions of each isotope as provided by the reactor company, the fission energies, and the number of antineutrinos produced per fission per isotope [47].

The precision of the measured baselines was about 2 cm with both the GPS and total station [48]. The geometric effect due to the finite size of the reactor cores and the antineutrino detectors, whose dimensions are comparable to the oscillation length at $|\Delta m^2| \sim \text{eV}^2$, was assessed by assuming that antineutrinos were produced and interacted uniformly in these volumes. The impact was found to be unimportant in the range of $\Delta m^2$ where Daya Bay is most sensitive ($|\Delta m^2| < 0.3$ eV$^2$). Higher order effects, such as the nonuniform production of antineutrinos inside the reactor cores due to a particular reactor fuel burning history, also had a negligible impact on the final result.

The greatest sensitivity to $\sin^2 2\theta_{14}$ in the $|\Delta m^2_{41}| < 0.3$ eV$^2$ range came from the relative measurements between multiple EHS at different baselines. Figure 1 shows the ratios of the observed prompt energy spectra at EH2 (EH3) and the three-neutrino best-fit prediction from the EH1 spectrum [45]. The data are compared with the 3+1 neutrino oscillation with $\sin^2 2\theta_{14} = 0.1$ and two representative $|\Delta m^2_{41}|$ values, illustrating that the sensitivity at $|\Delta m^2_{41}| = 4 \times 10^{-3}$ ($4 \times 10^{-3}$) eV$^2$ came primarily from the relative spectral shape comparison between EH1 and EH2 (EH3). Sensitivities for various combinations of the data sets from different EHS were estimated with the method described later in this Letter, and are shown in

<table>
<thead>
<tr>
<th>Location</th>
<th>IBD candidates</th>
<th>Mean distance to reactor core (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>EH1</td>
<td>203 809</td>
<td>365 860 1310</td>
</tr>
<tr>
<td>EH2</td>
<td>92 912</td>
<td>1345 479 528</td>
</tr>
<tr>
<td>EH3</td>
<td>41 589</td>
<td>1908 1536 1541</td>
</tr>
</tbody>
</table>

### TABLE I. Total number of IBD candidates and baselines of the three experimental halls to the reactor pairs.
and Mueller flux models. The rate uncertainty of the was described in the recent Daya Bay spectral analysis. The data from the three halls, in a fashion similar to what predicted reactor antineutrino spectra to simultaneously fit the reactor flux uncertainties as given in the Huber backgrounds, and with a covariance matrix encapsulating A binned log-likelihood method was adopted with nuisance j in the measurement between the two near halls, while the sensitivity region originated predominantly from the relative meas-

Fig. 2. The sensitivity in the 0.01 eV^2 < |Δm^2_{41}| < 0.3 eV^2 region originated predominantly from the relative measurement between the two near halls, while the sensitivity in the |Δm^2_{31}| < 0.01 eV^2 region arose primarily from the comparison between the near and far halls. The high-

The uncertainty of the reactor flux model’s normalization had a marginal impact in the |Δm^2_{41}| < 0.3 eV^2 region. For |Δm^2_{31}| > 0.3 eV^2, spectral distortion features are smeared out and the relative measurement loses its discriminatory power. The sensitivity in this region can be regained by comparing the event rates of the Daya Bay near halls with the flux model prediction, which will be reported in a future publication. In this Letter, we focus on the |Δm^2_{41}| < 0.3 eV^2 region.

Three independent analyses were conducted, each with a different treatment of the predicted reactor antineutrino flux and systematic errors. The first analysis used the predicted reactor antineutrino spectra to simultaneously fit the data from the three halls, in a fashion similar to what was described in the recent Daya Bay spectral analysis. A binned log-likelihood method was adopted with nuisance parameters constrained with the detector response and the backgrounds, and with a covariance matrix encapsulating the reactor flux uncertainties as given in the Huber and Mueller flux models. The rate uncertainty of the absolute reactor \bar{\nu}_e flux was enlarged to 5% based on Ref. [40]. The fit used sin^2 2θ_{12} = 0.857 ± 0.024, Δm^2_{31} = (7.50 ± 0.20) × 10^{-5} eV^2, and Δm^2_{32} = (2.41 ± 0.10) × 10^{-3} eV^2. The values of sin^2 2θ_{14}, sin^2 2θ_{15} and |Δm^2_{41}| were unconstrained. For the 3 + 1 neutrino model, a global minimum of \chi^2_{3ν}/NDF = 158.8/153 was obtained, while the minimum for the three-neutrino model was \chi^2_{3ν}/NDF = 162.6/155, where NDF represents number of degrees of freedom. We used the Δχ^2 = \chi^2_{3ν} - \chi^2_{3ν} distribution obtained from three-neutrino Monte Carlo samples that incorporated both statistical and systematic variations to obtain a p-value [52] of 0.74 for Δχ^2 = 3.8. The data were thus found to be consistent with the three-neutrino model, and there was no significant evidence for sterile neutrino mixing.

The second analysis performed a purely relative comparison between data at the near and far halls. The observed prompt energy spectra of the near halls were extrapolated to the far hall and compared with observation. This process was done independently for each prompt energy bin, by first unfolding it into the corresponding true antineutrino energy spectrum and then extrapolating to the far hall based on the known baselines and the reactor power profiles. A covariance matrix, generated from a large Monte Carlo data set incorporating both statistical and systematic variations, was used to
account for all uncertainties. The resulting $p$-value was 0.87. More details about this approach can be found in Ref. [53].

The third analysis exploited both rate and spectral information in a way that is similar to the first method but using a covariance matrix. This matrix was calculated based on standard uncertainty propagation methods, without an extensive generation of Monte Carlo samples. The obtained $p$-value was 0.74.

The various analyses have complementary strengths. Those that incorporated reactor antineutrino flux constraints had a slightly higher reach in sensitivity, particularly for higher values of $|\Delta m_{41}^2|$. The purely relative analysis was more robust against uncertainties in the predicted reactor antineutrino flux. The different treatments of systematic uncertainties provided a thorough cross-check of the results, which were found to be consistent for all the analyses in the region where the relative spectral measurement dominated the sensitivity ($|\Delta m_{41}^2| < 0.3$ eV$^2$). As evidenced by the reported $p$-values, no significant signature for sterile neutrino mixing was found by any of the methods.

Two methods were adopted to set the exclusion limits in the $(|\Delta m_{41}^2|, \sin^2 2\theta_{14})$ space. The first one was a frequentist approach with a likelihood ratio as the ordering principle, as proposed by Feldman and Cousins [54]. For each point $\eta \equiv (|\Delta m_{41}^2|, \sin^2 2\theta_{14})$, the value $\Delta \chi^2(\eta)$ encompassing a fraction $\alpha$ of the events in the $\chi^2(\eta) - \chi^2(\eta_{\text{best}})$ distribution was determined, where $\eta_{\text{best}}$ was the best-fit point. This distribution was obtained by fitting a large number of simulated experiments that included statistical and systematic variations. To reduce the number of computations, the simulated experiments were generated with a fixed value of $\sin^2 2\theta_{13} = 0.09$ [45], after it was verified that the dependency of $\Delta \chi^2(\eta)$ on this parameter was negligible. The point $\eta$ was then declared to be inside the $\alpha$-confidence level (C.L.) acceptance region if $\Delta \chi^2_{\text{data}}(\eta) < \Delta \chi^2_{\text{C.L.}}(\eta)$.

The second method was the confidence levels CL$_s$ statistical method [55] described in detail in Ref. [56]. A two-hypothesis test was performed in the $(\sin^2 2\theta_{14}, |\Delta m_{41}^2|)$ phase space with the null hypothesis $H_0$ (3-$\nu$ model) and the alternative hypothesis $H_{1}$ (3 + 1-$\nu$ model with fixed value of $\sin^2 2\theta_{14}$ and $|\Delta m_{41}^2|$). The value of $\theta_{13}$ was fixed with the best-fit value of the data for each hypothesis. Since both hypotheses have fixed values of $\sin^2 2\theta_{14}$ and $|\Delta m_{41}^2|$, their $\chi^2$ difference follows a Gaussian distribution. The mean and variance of these Gaussian distributions were calculated from Asimov data sets without statistical or systematic fluctuations, which avoided massive computing. The CL$_s$ value is defined by

$$\text{CL}_s = \frac{1 - p_1}{1 - p_0},$$

where $p_0$ and $p_1$ are the $p$-values for the 3-$\nu$ and 3 + 1-$\nu$ hypotheses models respectively. The condition of $\text{CL}_s \leq 0.05$ was required to set the 95% CL$_s$ exclusion regions.

The 95% confidence level contour from the Feldman-Cousins method and the 95% CL$_s$ method’s exclusion contour are shown in Fig. 3 [57]. The two methods gave comparable results. The detailed structure is due to the finite statistics of the data. The impact of varying the bin size of the IBD prompt energy spectrum from 200 to 500 keV was negligible. Moreover, the choice of mass ordering in both the three- and four-neutrino scenarios had a marginal impact on the results. For comparison, Bugey’s 90% C.L. exclusion on $\bar{\nu}_e$ disappearance obtained from their ratio of the positron energy spectra measured at 40/15 m [32] is also shown. Our result presently provides the most stringent limits on sterile neutrino mixing at $|\Delta m_{41}^2| < 0.1$ eV$^2$ using the electron antineutrino disappearance channel. This result is complementary to those from the $\nu_\mu \rightarrow \nu_e$ and $\nu_\mu \rightarrow \nu_\tau$ oscillation channels. While the $\bar{\nu}_e$ appearance mode constrains the product of $|U_{e4}|^2$ and $|U_{\mu 4}|^2$, the $\nu_\mu$ and $\bar{\nu}_e$ disappearance modes constrain $|U_{e4}|^2$ and $|U_{\mu 4}|^2$, respectively.

In summary, we report on a sterile neutrino search based on a minimal extension of the standard model, the 3( active) + 1(sterile) neutrino mixing model, in the Daya Bay Reactor Antineutrino Experiment using the electron-antineutrino disappearance channel. The analysis used the

![Figure 3](color online). Exclusion contours for the neutrino oscillation parameters $\sin^2 2\theta_{14}$ and $|\Delta m_{41}^2|$. Normal mass hierarchy is assumed for both $\Delta m_{31}^2$ and $\Delta m_{41}^2$. The red long-dashed curve represents the 95% C.L. exclusion contour with Feldman-Cousins method [54]. The black solid curve represents the 95% CL$_s$ exclusion contour [55]. The parameter space to the right side of the contours is excluded. For comparison, Bugey’s [32] 90% C.L. limit on $\bar{\nu}_e$ disappearance is also shown as the green dashed curve.
relative event rate and the spectral comparison of three far and three near antineutrino detectors at different baselines from six nuclear reactors. The data are in good agreement with the three-neutrino model. The current precision is dominated by statistics. With at least three more years of additional data, the sensitivity to $\sin^2 2\theta_{14}$ is expected to improve by a factor of two for most $|\Delta m^2_{41}|$ values. The current result already yields the world’s most stringent limits on $\sin^2 2\theta_{14}$ in the $|\Delta m^2_{41}| < 0.1$ eV$^2$ region.

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values are consistent, and the results presented here are not very sensitive to this parameter.

52. The $p$-value is the probability of obtaining a test statistic result at least as extreme as the observed one.

53. Y. Nakajima and J. P. Ochoa-Ricoux (to be published).


