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A low-frequency noise model with carrier generation-recombination process for pentacene organic thin-film transistor

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By including the generation-recombination process of charge carriers in conduction channel, a model for low-frequency noise in pentacene organic thin-film transistors (OTFTs) is proposed. In this model, the slope and magnitude of power spectral density for low-frequency noise are related to the traps in the gate dielectric and accumulation layer of the OTFT for the first time. The model can well fit the measured low-frequency noise data of pentacene OTFTs with HfO₂ or HfLaO gate dielectric, which validates this model, thus providing an estimate on the densities of traps in the gate dielectric and accumulation layer. It is revealed that the traps in the accumulation layer are much more than those in the gate dielectric, and so dominate the low-frequency noise of pentacene OTFTs. © 2013 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4816103>]

I. INTRODUCTION

Organic thin-film transistors (OTFTs) have gained considerable interest due to their potential application in large-area flexible displays and sensor arrays.^{1,2} Among various organic semiconductors, pentacene has higher carrier mobility than others, reaching well above 1 cm²/V·s.^{3,4} Hence, it has been widely employed as the active layer in the OTFTs. Flicker noise, also called $1/f$ noise because its power spectral density (PSD) varies as $1/f^\alpha$ with α close or equal to unity, occurs in almost all semiconductor devices in the low-frequency region.⁵ In the last several decades, the flicker noise in the metal-oxide-semiconductor field-effect transistors (MOSFETs) has been intensively studied.^{6–8} For the flicker noise in the silicon MOSFET, the exponent α is close to one in most cases. Assuming the probability of an electron penetrating into the oxide decreases exponentially with the distance from the oxide-semiconductor interface and the traps are uniformly or exponentially distributed in the oxide, the value of the slope of the PSD of the low-frequency noise (LFN) of MOSFETs can be explained.^{9–11} It is clear that pentacene OTFTs are quite different from the conventional MOSFET. The carrier mobility of OTFTs is much lower than that of silicon MOSFET. Moreover, there are many traps in the pentacene grains and the grain boundaries of pentacene OTFTs.^{12,13} However, in the flicker noise model for the conventional MOSFET based on single-crystal silicon, traps are assumed to exist only in the oxide near the interface.^{11,14}

At present, flicker noise models for the silicon MOSFET are frequently employed to interpret the noise data measured in the pentacene OTFTs.^{15,16} Considering the difference between the OTFT and conventional inorganic MOSFET, it is necessary to bring forward a model for the flicker noise in the OTFTs. Several papers reported that the PSD of LFN in OTFTs significantly deviated from the $1/f$ noise model for

the MOSFET.^{17–20} Both the magnitude and slope of the PSD are still not well modeled from the physics foundation. Previous reports have mentioned that the traps in the grain boundaries dominate the LFN in OTFTs and even proposed that the traps in the boundaries could affect the slope of the PSD.^{15,20,21} However, the relation between the slope and the traps in OTFTs is still not yet provided by any model. In this work, we propose a model based on the generation-recombination (GR) process of charge carriers in the accumulation layer and gate dielectric to explain the slope and magnitude of the PSD measured for pentacene OTFTs.

To verify the proposed model, pentacene OTFTs with HfO₂ or HfLaO gate dielectric were fabricated. After silicon substrates were cleaned by the standard RCA method, HfO₂ was deposited by atomic layer deposition (ALD) with a thickness of 40.0 nm at a substrate temperature of 300 °C, while HfLaO was prepared by sputtering with a thickness of 39.8 nm at room temperature. Then, only the HfLaO film was annealed in N₂ at 400 °C for 10 min to achieve higher film quality. After that, a 30-nm pentacene film was deposited at a rate of 1.1 nm/min in high vacuum (4×10^{-6} torr) on the two dielectrics. Finally, drain and source electrodes were evaporated on the pentacene film by gold evaporation through a shadow mask to form the OTFTs. The width and length of the channel on the shadow mask were 200 μ m and 30 μ m, respectively. HP 4145B semiconductor parameter analyzer, Berkeley Technology Associates FET Noise Analyzer Model 9603, and HP 35665A Dynamic Signal Analyzer were used to measure the transfer characteristics and noise spectrum of the pentacene OTFTs. All the measurements were conducted at room temperature (300 K) in air, and under an electrically shielded environment.

II. DERIVATION OF THE NOISE MODEL

From Fig. 1, the elemental volumes, $\Delta\Lambda$ and $\Delta\Lambda'$, in the gate dielectric and accumulation layer, respectively, can be written as

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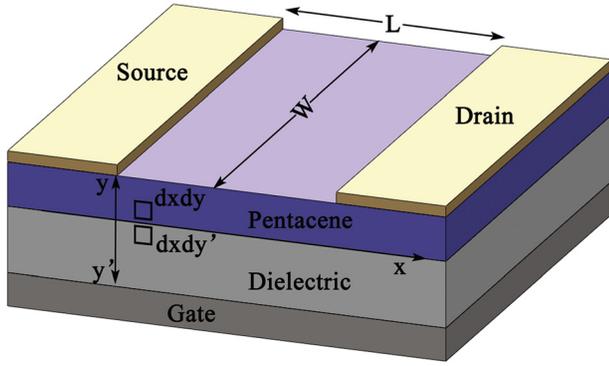


FIG. 1. Structure of the pentacene OTFT used in this study.

$$\Delta\Lambda = W dx dy, \quad (1a)$$

$$\Delta\Lambda' = W dx dy', \quad (1b)$$

where W is the channel width.

Based on the carrier GR process, the frequency spectrum of the mean-squared fluctuation in the number of trapped carriers in an elemental volume is given by²²

(in the gate dielectric)

$$S_{\Delta\Lambda\delta n_{td}}(f) = \frac{4\tau_d}{1 + (2\pi f)^2 \tau_d^2} N_{td} f_{id} f_{idp} \Delta\Lambda, \quad (2a)$$

(in the accumulation layer)

$$S_{\Delta\Lambda'\delta n_{tb}}(f) = \frac{4\tau_b}{1 + (2\pi f)^2 \tau_b^2} N_{tb} f_{ib} f_{ibp} \Delta\Lambda', \quad (2b)$$

where

$$f_{id} = 1 - f_{idp} = [1 + \exp(E - E_{fd})/kT]^{-1}$$

$$f_{ib} = 1 - f_{ibp} = [1 + \exp(E - E_{fb})/kT]^{-1}$$

δn_{td} , the fluctuation in trapped carrier density in gate dielectric

δn_{tb} , the fluctuation in trapped carrier density in accumulation layer

N_{td} , the density of traps in gate dielectric

N_{tb} , the density of traps in accumulation layer

k , the Boltzmann's constant (8.617×10^{-5} eV K⁻¹)

T , the temperature

E_{fd} , the quasi-Fermi level in gate dielectric

E_{fb} , the quasi-Fermi level in accumulation layer

f_{id} , the occupancy function in gate dielectric

f_{ib} , the occupancy function in accumulation layer

τ_d , the decay time in gate dielectric

τ_b , the decay time in accumulation layer

Since the fluctuations in carrier number caused by the traps in the gate dielectric and accumulation layer are independent, in the volume $\Delta\Lambda$ and $\Delta\Lambda'$, the PSD of the mean-squared fluctuation in current, $\langle(\delta I_D)^2\rangle$, at the point x along the channel can be expressed as (see Appendix A),

$$S_{\delta I_D}(f) = \frac{4\mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} \left[\frac{\tau_d}{1 + (2\pi f)^2 \tau_d^2} N_{td} f_{id} f_{idp} dy dV + \frac{\tau_b}{1 + (2\pi f)^2 \tau_b^2} N_{tb} f_{ib} f_{ibp} dy' dV \right]. \quad (3)$$

The total PSD of the LFN in the drain current is then obtained by integrating the Eq. (3):

$$S_{I_D}(f) = \frac{4\mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} \times \left[\int_0^{V_d} \int_{E_v}^{E_c} \int_0^{t_d} \frac{\tau_d(E, V, y)}{1 + (2\pi f)^2 \tau_d^2(E, V, y)} N_{td} f_{id} f_{idp} dy dE dV + \int_0^{V_d} \int_{E_v}^{E_c} \int_0^{t_b} \frac{\tau_b(E, V, y')}{1 + (2\pi f)^2 \tau_b^2(E, V, y')} N_{tb} f_{ib} f_{ibp} dy' dE dV \right], \quad (4)$$

where t_b is the thickness of the accumulation layer (0.9 nm),²³ t_d is the distance inside the oxide over which the traps are distributed, and $E_c - E_v$ is the bandgap energy of pentacene.

For evaluating the integral in Eq. (4), two assumptions have to be made:

- (i) The decay time τ_b in the accumulation layer is constant and in the gate dielectric is given by^{6,24} $\tau_d(E, V, y) = \tau_{d0} \exp(\gamma y)$ with $\gamma = 4\pi/h\sqrt{2m^* \Phi_B}$, where m^* is the effective hole mass ($= 3m_0$ ²⁵), Φ_B is the barrier height ($= 1.3$ eV), h is the Planck's constant, τ_{d0} is life time at the interface, and γ is the tunneling coefficient ($= 2 \times 10^8$ cm⁻¹).^{10,26}
- (ii) The traps are assumed to be uniformly distributed in the bandgap of pentacene.²⁴ With these two assumptions, carrying out the integration in Eq. (4) yields (see Appendix B)

$$S_{I_D}(f) = \frac{A}{f} + \frac{\tau_b B}{1 + (2\pi f \tau_b)^2}, \quad (5)$$

with

$$A = \frac{kTV_d \mu q^2 I_D}{\gamma C_{ox} L^2 |V_G - V_{th}|} N_{td}, \quad (6)$$

and

$$B = \frac{4kTV_d t_b \tau_b \mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} N_{tb}. \quad (7)$$

The first term in Eq. (5) results from carrier-number fluctuation caused by the traps in the dielectric and is consistent with other noise models based on carrier-number fluctuation for conventional transistors.¹⁴ On the other hand, the second term refers to the GR noise caused by the traps in the conducting accumulation layer. For the first time, the GR noise caused by the pentacene film has been considered and formulated in the noise model for OTFT.

III. RESULTS AND DISCUSSION

The carrier mobility and threshold voltage of the OTFTs are extracted from their I-V characteristics shown in Fig. 2 and listed in Table I. On the other hand, the method for extracting the noise parameters of the OTFTs is based on the differential evolution algorithm.²⁷ The coefficients A, B, and τ_b can be optimally extracted by fitting Eq. (5) with the measured noise spectra in Fig. 3, and their values are listed in Table I. Then, by putting the extracted values of A and B into Eqs. (6) and (7), respectively, N_{td} and N_{tb} can be calculated and are listed in Table I.

Table I also lists the interface-trap density of the OTFTs (N_T and N_{SS}), where N_T is extracted by the traditional noise model for silicon MOSFET based on carrier-number fluctuation¹⁵

$$\frac{S_{I_D}(f)}{I_D^2} = \frac{g_m^2}{I_D^2} \frac{q^2 k T N_T}{W L C_{ox}^2 f^\alpha}, \quad (8)$$

and N_{SS} is calculated from the sub-threshold swing (SS) of the OTFTs based on¹²

$$N_{ss} = \frac{C_{ox}}{q t_b} \left[\frac{SS \cdot q}{k T \ln 10} - 1 \right]. \quad (9)$$

So, with the same order of magnitude for N_T and N_{SS} , the interface-trap density extracted from the traditional noise model is consistent with that extracted from the current-voltage characteristics of the OTFTs. However, both Eqs. (8) and (9) can only give the effective trap density at the interface because they do not differentiate between the traps in the gate dielectric and accumulation layer.

Unlike the MOSFET based on crystalline silicon, there are many defects in the conducting layer of OTFT. The charge transport mechanisms in organic materials have been described by Coropceanu *et al.*²⁸ and Lin *et al.*²⁹ The polaron models have been employed to explain the transport mechanism, in which the total carrier mobility can be expressed to a good approximation as a sum of two contributions,

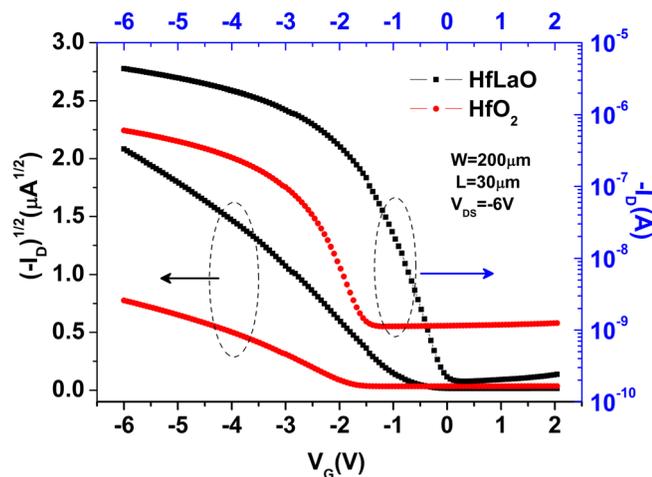


FIG. 2. Transfer characteristics of the OTFTs with sputtered HfLaO and ALD HfO₂ as gate dielectric at $V_D = -5$ V.

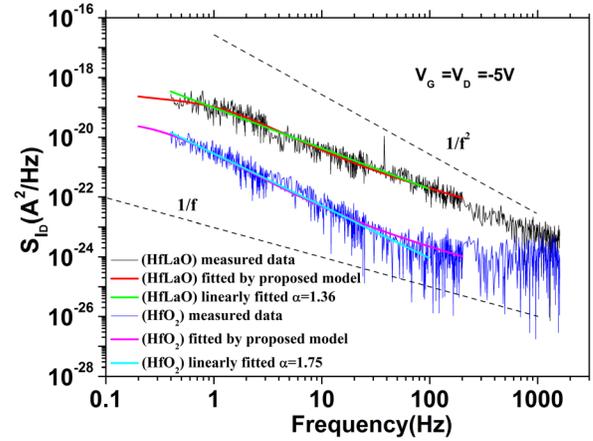


FIG. 3. PSD of drain-current noise for the OTFTs with sputtered HfLaO and ALD HfO₂ as gate dielectric. The linearly fitted slope based on a traditional noise model is 1.34 and 1.75, respectively. On the other hand, the proposed model can better fit the measured data.

$$\mu = \mu_{tun} + \mu_{hop}, \quad (10)$$

where μ_{tun} is tunneling mobility and μ_{hop} is hopping mobility. At room temperature, the hopping term dominates the mobility, and the mobility exhibits temperature-activated transport. In this study, measurements on the properties of devices are done at room temperature, and thus the hopping conduction should dominate the charge transport in the channel. Therefore, the noise spectrum can be used to quantify the defect density as listed in Table I.

The calculated results by this model are in good agreement with the measured PSD of both OTFTs in the low-frequency region as shown in Fig. 3. In the high-frequency region (above 100 Hz for the OTFT with HfO₂ gate dielectric and 1000 Hz for the one with HfLaO gate dielectric), the low-frequency noise is overshadowed by thermal noise. Based on Eq. (8), the slope of PSD (α) in the low-frequency region can be extracted as 1.75 and 1.34 for the OTFTs with HfO₂ and HfLaO gate dielectric, respectively. However, α is only a fitting parameter without any physical meaning. The proposed model in this work can well fit the slope by including the traps in the accumulation layer, and thus can well explain why the slope significantly deviates

TABLE I. Parameters of the Pentacene OTFTs.

Dielectric	HfLaO	HfO ₂
Capacitance C_{ox} ($\mu\text{F}/\text{cm}^2$)	0.240	0.312
Threshold voltage V_{th} (V)	-0.587	-1.85
Drain current I_D (μA) ($V_G = V_D = -5$ V)	4.31	0.661
Carrier mobility μ ($\text{cm}^2/\text{V}\cdot\text{s}$)	0.358	0.0815
Subthreshold swing (V/dec)	0.585	0.569
A ($\times 10^{-22}$ A ²)	36.7	0.105
B ($\times 10^{-20}$ A ² s ⁻¹)	31.7	4.49
τ_b (s)	0.139	0.390
N_{td} ($\times 10^{20}$ eV ⁻¹ cm ⁻³)	13.7	1.04
N_{tb} ($\times 10^{22}$ eV ⁻¹ cm ⁻³)	1.18	6.37
N_T ($\times 10^{20}$ eV ⁻¹ cm ⁻³)	3.48	6.08
N_{SS} ($\times 10^{20}$ eV ⁻¹ cm ⁻³)	1.85	1.47

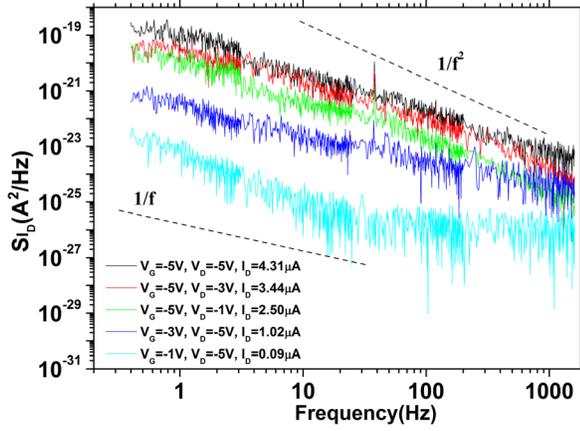


FIG. 4. PSD of drain-current noise for the OTFT with sputtered HfLaO as gate dielectric at various drain biases and gate voltages.

from the value of unity in the $1/f$ noise model. As shown in Table I, the density of the traps in the accumulation layer is higher than that in the gate dielectric. This can explain why the slope is significantly larger than one and verify that the traps in the pentacene accumulation layer dominate the LFN. The slope is determined by the ratio of the trap densities in the conducting layer and gate dielectric and also the decay time in the conducting layer. Compared with the OTFT with HfLaO gate dielectric, the one with HfO₂ gate dielectric has higher density of traps in the accumulation layer, but lower density of traps in the gate dielectric. This is because the ALD technique can result in higher-quality dielectric film with less traps but pentacene film grown on HfLaO has been demonstrated to have larger grains.³⁰ Therefore, the slope of the LFN for the OTFT with HfO₂ gate dielectric is larger. Moreover, the density of traps in the accumulation layer is also in good agreement with those in the literature.^{12,31,32} The extracted density of traps in the HfO₂ gate dielectric is also comparable with those reported in Refs. 33–35.

The PSD of drain-current noise for the OTFT with HfLaO gate dielectric is measured at various drain biases and gate voltages and shown in Fig. 4. As we move from the lowest curve to the highest curve, the magnitude of the drain current increases (see the legends in Fig. 4). Therefore, the magnitude of the PSD scales with the drain current in the channel, as predicted by Eq. (5) of the proposed model.

IV. CONCLUSION

Based on the GR process in organic semiconductor and gate dielectric, we have developed a microscopic model which provides a quantitative interpretation of the LFN for the pentacene OTFTs. The model reveals the relation between the density of traps in the pentacene accumulation layer and the slope of the PSD, and fits the measured noise spectrum well in both its slope and magnitude. The density of traps extracted by this model in the accumulation layer is much higher than that in the gate dielectric, and thus dominates the low-frequency noise of the pentacene OTFTs. In

conclusion, this model can well explain the LFN measured for the pentacene OTFTs.

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APPENDIX A: PROOF OF PSD IN ELEMENTAL VOLUMES

The carrier number $\Delta N(t)$ in the volume $\Delta\Lambda$ and $\Delta\Lambda'$ at the point x along the channel can be written as:³⁶

$$\Delta N(t) = \overline{\Delta N} + \delta N(t), \quad (\text{A1})$$

where $\overline{\Delta N}$ is the mean value or steady-state value of the carrier number, and $\delta N(t)$ is the fluctuation in carrier number in the volume $\Delta\Lambda$ and $\Delta\Lambda'$ caused by the traps in the gate dielectric and accumulation layer.

Since the fluctuations in carrier number are much smaller than the carrier number in the channel, the impact of the fluctuations in carrier number can be linearized as³⁷

$$\delta N = \delta N_d + \delta N_b, \quad (\text{A2})$$

where δN_d and δN_b are fluctuations in carrier number caused by traps in the gate dielectric and accumulation layer in the elemental volumes $\Delta\Lambda$ and $\Delta\Lambda'$, respectively.

Assuming that (1) δN_d and δN_b are due to wide-sense stationary processes with time-averaged value equal to zero, i.e., $\langle \delta N_d \rangle = 0$ and $\langle \delta N_b \rangle = 0$; (2) the two random processes are mutually independent because they separately occur in the accumulation layer and gate dielectric,

$$\langle (\delta N)^2 \rangle = \langle (\delta N_d)^2 \rangle + \langle (\delta N_b)^2 \rangle, \quad (\text{A3})$$

where $\langle \rangle$ denotes the time-averaged value.

Assuming that all the current in the channel can flow to the drain terminal, the mean-squared fluctuation in current at a distance x along the channel in the volume $\Delta\Lambda$ and $\Delta\Lambda'$ can be given by³⁷

$$\langle (\delta I_D)^2 \rangle = \left(\frac{I_D}{N} \right)^2 \langle (\delta N)^2 \rangle, \quad (\text{A4})$$

where I_D is the current in the channel and N is the total carrier number in the channel. Therefore, the PSD of $\langle (\delta I_D)^2 \rangle$ is

$$S_{\delta I_D}(f) = \left(\frac{I_D}{N} \right)^2 [S_{\delta N_d}(f) + S_{\delta N_b}(f)], \quad (\text{A5})$$

where $S_{\delta N_d}(f)$ and $S_{\delta N_b}(f)$ are the frequency spectra of $\langle (\delta N_d)^2 \rangle$ and $\langle (\delta N_b)^2 \rangle$, respectively.

In the elemental volumes $\Delta\Lambda$ and $\Delta\Lambda'$, the mean-square fluctuations in carrier number caused by traps in the gate dielectric and in the accumulation layer are, respectively, given by

$$\langle(\delta N_d)^2\rangle = \langle(\Delta\Lambda'\delta n_{td})^2\rangle, \quad (\text{A6a})$$

$$\langle(\delta N_b)^2\rangle = \langle(\Delta\Lambda\delta n_{tb})^2\rangle. \quad (\text{A6b})$$

From the simple MOSFET theory, it can be shown that

$$I_D = qp(x)\mu \frac{dV(x)}{dx}, \quad (\text{A7})$$

where q is the electron charge, μ is the carrier mobility, $V(x)$ is the electric potential along the channel, and $p(x)$ is the carrier density per unit length in the channel at the point x .

The total carrier number N in the channel can be given by

$$N = \frac{WLC_{ox}}{q} |V_G - V_{th}|, \quad (\text{A8})$$

where C_{ox} is the oxide capacitance per unit area, L is the channel length, V_G is the gate voltage, and V_{th} is the threshold voltage of the OTFT.

In the volume $\Delta\Lambda$ and $\Delta\Lambda'$, the PSD of the mean-squared fluctuation in current, $\langle(\delta I_D)^2\rangle$, at the point x along the channel can be derived by using Eqs. (1), (2), and (A4)–(A8) as

$$S_{\delta I_D}(f) = \frac{4\mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} \left[\frac{\tau_d}{1 + (2\pi f)^2 \tau_d^2} N_{td} f_{td} f_{tdp} dy dV + \frac{\tau_b}{1 + (2\pi f)^2 \tau_b^2} N_{tb} f_{tb} f_{tbp} dy' dV \right]. \quad (\text{A9})$$

APPENDIX B: INTEGRAL OF PSD

$$\begin{aligned} S_{I_D}(f) &= \frac{4\mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} \left[\int_0^{V_d} \int_{E_v}^{E_c} \int_0^{t_d} \frac{\tau_d(E, V, y)}{1 + (2\pi f)^2 \tau_d^2(E, V, y)} N_{td} f_{td} f_{tdp} dy dE dV + \int_0^{V_d} \int_{E_v}^{E_c} \int_0^{t_b} \frac{\tau_b(E, V, y')}{1 + (2\pi f)^2 \tau_b^2(E, V, y')} N_{tb} f_{tb} f_{tbp} dy' dE dV \right] \\ &= \frac{4\mu q^2 I_D}{C_{ox} L^2 |V_G - V_{th}|} \left[\int_0^{V_d} dV \int_{E_v}^{E_c} N_{td} f_{td} f_{tdp} dE \int_0^{t_d} \frac{\tau_{d0} \exp(\gamma y)}{1 + (2\pi f)^2 \tau_{d0}^2 \exp(\gamma y)} dy + \int_0^{V_d} dV \int_{E_v}^{E_c} N_{tb} f_{tb} f_{tbp} dE \int_0^{t_b} \frac{\tau_b}{1 + (2\pi f)^2 \tau_b^2} dy' \right]. \end{aligned} \quad (\text{B1})$$

Assuming that the traps are uniformly distributed in the bandgap of pentacene,

$$\int_{E_v}^{E_c} N_{td} f_{td} (1 - f_{tdp}) dE \approx N_{td} kT, \quad (\text{B2})$$

and

$$\int_{E_v}^{E_c} N_{tb} f_{tb} (1 - f_{tbp}) dE \approx N_{tb} kT. \quad (\text{B3})$$

Since the decay time τ_b in the accumulation layer is constant,

$$\int_0^{t_b} \frac{\tau_b}{1 + (2\pi f)^2 \tau_b^2} dy' = \frac{t_b \tau_b}{1 + (2\pi f)^2 \tau_b^2}. \quad (\text{B4})$$

In the gate dielectric, τ_d is given by

$$\tau_d(E, V, y) = \tau_{d0} \exp(\gamma y), \quad (\text{B5})$$

and

$$\begin{aligned} &\int_0^{t_d} \frac{\tau_{d0} \exp(\gamma y)}{1 + (2\pi f)^2 \tau_{d0}^2 \exp(\gamma y)} dy, \\ &= \frac{1}{2\pi f \gamma} (\arctan[2\pi f \tau_{d0} \exp(\gamma t_d)] - \arctan(2\pi f \tau_{d0})). \end{aligned} \quad (\text{B6})$$

Typical value of τ_{d0} is about 10^{-8} s and for the traps in the dielectric distributed over a distance of about $t_d = 2$ nm, γt_d is about 40.²⁴ Thus, for the low-frequency region, the first term inside the bracket on the right-hand side can be approximated by $\pi/2$, while the second term is about zero. Therefore,

$$\int_0^{t_d} \frac{\tau_{d0} \exp(\gamma y)}{1 + (2\pi f)^2 \tau_{d0}^2 \exp(\gamma y)} dy \approx \frac{1}{4f\gamma}, \quad (\text{B7})$$

and $S_{I_D}(f)$ can be expressed by

$$\begin{aligned} S_{I_D}(f) &= \frac{kTV_d \mu q^2 I_D N_{td}}{\gamma C_{ox} L^2 |V_G - V_{th}| f} \\ &+ \frac{4kTV_d t_b \tau_b \mu q^2 I_D N_{tb}}{C_{ox} L^2 |V_G - V_{th}|} \frac{\tau_b}{1 + (2\pi f \tau_b)^2}. \end{aligned} \quad (\text{B8})$$

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