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Mitigation of Low-Frequency Current Ripple in Fuel-Cell Inverter Systems Through Waveform Control

Guo-Rong Zhu, Member, IEEE, Siew-Chong Tan, Senior Member, IEEE, Yu Chen, Member, IEEE, and Chi K. Tse, Fellow, IEEE

Abstract—Fuel-cell power systems comprising single-phase dc/ac inverters draw low-frequency ac ripple currents at twice the output frequency from the fuel cell. Such a 100/120 Hz ripple current may create instability in the fuel-cell system, lower its efficiency, and shorten the lifetime of a fuel cell stack. This paper presents a waveform control method that can mitigate such a low-frequency ripple current being drawn from the fuel cell while the fuel-cell system delivers ac power to the load through a differential inverter. This is possible because with the proposed solution, the pulsation component (cause of ac ripple current) of the output ac power will be supplied mainly by the two output capacitors of the differential inverter while the average dc output power is supplied by the fuel cell. Theoretical analysis, simulation, and experimental results are provided to explain the operation and showcase the performance of the approach. Results validate that the proposed solution can achieve significant mitigation of the current ripple as well as high-quality output voltage without extra hardware. Application of the solution is targeted at systems where current ripple mitigation is required, such as for the purpose of eliminating electrolytic capacitor in photovoltaic and LED systems.

Index Terms—Active method, decouple, fuel cell, low-frequency current ripple, pulsation power, waveform control.

I. INTRODUCTION

THE conversion of dc power into ac power through a single-phase inverter will typically introduce a low-frequency current ripple (at twice the ac output voltage frequency) at the dc input side of the power conversion system. In a typical 50-Hz or 60-Hz single-phase inverter system, the ripple is, respectively, 100 and 120 Hz [2]. The presence of such a ripple is detrimental and damaging to a dc source made up of fuel cells. As pointed out in [2]–[8], the various disadvantages include: 1) significant wastage in fuel consumption [2], [3]; 2) oxygen starvation leading to reduced maximum power generation [4], [5]; 3) poor dynamic response [6]; 4) nuisance tripping at heavy load [7]; and 5) shortening of fuel cell’s lifetime [4], [8].

For this reason, the issues and standards concerning the limitation of the low-frequency current ripple are often specified in technical reports and manufacturers’ manuals [9], [10]. According to [9], it is recommended that the 100/120 Hz ripple component be limited to within 15% of the total output and the 60 Hz ripple component be limited to within 10% at 10–100% loads for an overall improved efficiency and fuel cell’s lifetime. The Ballard Nexa 1.2-kW PEMFC is set to a 120 Hz current ripple limit of up to 35% of the peak-to-peak value, or up to 24.7% of the root mean square (rms) value [10]. Consequently, the subject of mitigating low-frequency input current ripple of inverters has become an important topic in fuel-cell power system research.

In particular, various passive energy storage compensation methods have been proposed in [11], which involve the incorporation of a large dc capacitor, passive-resonant circuit, or battery at the dc line. The drawback of this approach is that the product size and cost will be increased. Alternative solutions involving active harmonic filter compensation using an external converter were also proposed to mitigate the low-frequency current ripple [12]–[21]. While these methods are feasible, they also require extra hardware and are typically not preferred.

On the other hand, it is also possible to mitigate the current ripple through the use of active control methods, e.g., by using a dual-loop control [1] or by using a moving-average filter [22]. These methods do not incur extra component cost and can reduce the low-frequency ripple during steady state, thereby allowing the reduction of the storage capacitance. However, these methods can achieve only partial mitigation of the low-frequency ripple and generate large overshoots during load transients, which will induce oscillation that will lead to slow dynamic response at the dc bus.

In this paper, an approach of mitigating low-frequency current ripple of fuel-cell power systems through the application of waveform control on differential power inverters is proposed.
A comparative study on the proposed waveform control and the traditional control method without waveform control used in [20] and [21], under the same topology, is performed. It will be clearly illustrated in this paper that the proposed solution achieves significant suppression of the low-frequency current ripple without any additional component, circuit, or electrolytic capacitor, therefore maintaining the overall size and cost. Additionally, the current stress of the switch is decreased and the total efficiency is improved with the use of waveform control.

II. FUEL-CELL SYSTEMS BASED ON DIFFERENTIAL INVERTERS

A. Overview

Differential inverters have been widely applied to ac applications powered by dc sources, e.g., in fuel-cell inverter systems, due to its advantages of high efficiency, reduced size, and low cost [23]–[30]. Fig. 1 shows a diagram of a fuel-cell system with a differential inverter. Here, \( v_{in} \) and \( i_{in} \), respectively, represent the input voltage and current of the differential inverter, which is also the output voltage and current of the fuel cell. The output voltage and current of the inverter, which are both ac sinusoidal quantities, are depicted as \( v_o \) and \( i_o \), respectively. \( v_o \) is the difference of \( v_{c1} \) and \( v_{c2} \), which are the voltages of the inverter’s output capacitors \( C_1 \) and \( C_2 \), respectively.

B. Analysis

A differential inverter is an inverter made up of two identical bidirectional dc/dc (i.e., buck, boost, or buck–boost) converters to deliver in a single stage, either a boost, a buck, or a buck–boost operation together with the voltage inverter function. Based upon the dc/dc converter type, each converter will generate a dc-biased ac output voltage that is higher or lower than the fuel cells voltage of which when the outputs of the two dc/dc converters are combined, only a pure ac output voltage is generated. In conventional practice, a voltage control will be applied on the respective converter to ensure that the output voltage of each converter and their combined output voltage will be, respectively

\[
v_{c1} = V_d + \frac{1}{2} V_{max} \sin(\omega t)
\]

(1)

\[
v_{c2} = V_d + \frac{1}{2} V_{max} \sin(\omega t - \pi)
\]

(2)

and

\[
v_o = v_{c1} - v_{c2} = V_{max} \sin(\omega t)
\]

(3)

where \( v_{c1} \) and \( v_{c2} \) are the output voltages of the two dc/dc converters, \( V_{max} \) is the amplitude of the output voltage \( v_o \), \( \omega \) is the line frequency, and \( V_d \) is the dc-biased voltage of \( v_{c1} \) and \( v_{c2} \). From (3), it can be observed that the required output is as desired, i.e., comprising only the ac component.

For a single-phase fuel-cell inverter system operating with unity power factor, the ideal output current can be written as

\[
i_o = I_{max} \sin(\omega t)
\]

(4)

where \( I_{max} \) is the amplitude of the output current \( i_o \). Multiplying (3) with (4) gives the output power \( p_o \) as

\[
p_o = \frac{1}{2} V_{max} I_{max} (1 - \cos(2\omega t)).
\]

(5)

The double-line-frequency component of the power is reflected in the \( \cos(2\omega t) \) term. On the other hand, the output power of the fuel cell can be expressed as

\[
p_{dc} = V_{in} (I_{indc} + i_{inac})
\]

(6)

where \( I_{indc} \) and \( i_{inac} \) are the dc and ac components of the current, respectively. Assuming 100% power efficiency and that the fuel-cell voltage is constant, \( I_{indc} \) will be

\[
I_{indc} = \frac{V_{max} I_{max}}{2V_{in}}.
\]

(7)

From (5)–(7), the ac component \( i_{inac} \) is

\[
i_{inac} = \frac{V_{max} I_{max}}{2V_{in}} \cos(2\omega t).
\]

(8)

As given in (8), the \( 2\omega t \) ripple current drawn from the fuel cell can be significant if no capacitor is installed at the dc side to provide energy buffering. Fig. 2(a) shows the waveforms of a differential inverter operating with unity power factor as described in this section.

C. Altering of the Waveforms of a Differential Inverter

From (3), it can be seen that it is possible to individually control the output voltages of the dc/dc converters of the differential inverter, i.e., \( v_{c1} \) and \( v_{c2} \), such that they differ from (1) and (2), while still maintaining a pure sinusoidal output voltage \( v_o \). For example, the component \( F(t) \) can be added to (1) and (2) to give

\[
v_{c1} = V_d + \frac{1}{2} V_{max} \sin(\omega t) + F(t)
\]

(9)

and

\[
v_{c2} = V_d + \frac{1}{2} V_{max} \sin(\omega t - \pi) + F(t).
\]

(10)

However, \( v_o = v_{c1} - v_{c2} = V_{max} \sin(\omega t) \) will still be equivalent to (3). The ability to alter \( v_{c1} \) and \( v_{c2} \) brought up the question as to whether the adding of such compensating components can mitigate the input current ripple given in (8) and shown in Fig. 2(a). We found that this is hypothetically possible. If \( v_{c1} \) and \( v_{c2} \) are controlled such that they behave the way as shown.

Fig. 1. Diagram of a fuel cell with a differential inverter.

![Diagram of a fuel cell with a differential inverter.](image-url)
III. PROPOSED WAVEFORM CONTROL METHOD

In this paper, a boost-type differential inverter made up of two bidirectional boost converters (see Fig. 3) is adopted as the case study example in the fuel-cell system for describing the proposed waveform control. Here, $V_{in}$ is the dc input voltage, $L_1$ and $L_2$ are the power inductors, $T_1$–$T_4$ are the power switches, $D_1$ and $D_2$ are the free-wheeling diodes, $C_1$ and $C_2$ are the output capacitors, and $R$ is the load resistance.

If the capacitor voltages of the two boost converters can be, respectively, controlled as

$$v_{c1} = V_d + \frac{1}{2}V_{\max} \sin(\omega t) + B \sin(2\omega t + \varphi) \tag{11}$$

and

$$v_{c2} = V_d + \frac{1}{2}V_{\max} \sin(\omega t - \pi) + B \sin(2\omega t + \varphi) \tag{12}$$

then $v_o$ will be equivalent to (3). The objective of the waveform control method is to ensure that the capacitor voltages follow precisely (11) and (12). According to [31], to maximize the efficiency of the converter, the minimum dc bias for the converters is

$$V_d > \frac{1}{2}V_{\max} + V_{in} + B. \tag{13}$$

Since $i = C \frac{dv}{dt}$, the currents of capacitors $C_1$ and $C_2$ (for $C = C_1 = C_2$) can be found from (11) and (12) as

$$i_{c1} = C\omega \frac{1}{2}V_{\max} \cos(\omega t) + 2C\omega B \cos(2\omega t + \varphi) \tag{14}$$

and

$$i_{c2} = -C\omega \frac{1}{2}V_{\max} \cos(\omega t) + 2C\omega B \cos(2\omega t + \varphi). \tag{15}$$

Accordingly, from Fig. 3

$$i_1 = i_o + i_{c1} = I_{\max} \sin(\omega t) + C\omega \frac{1}{2}V_{\max} \cos(\omega t)$$
$$+ 2C\omega B \cos(2\omega t + \varphi) \tag{16}$$

$$i_2 = -i_o + i_{c2} = -I_{\max} \sin(\omega t) - C\omega \frac{1}{2}V_{\max} \cos(\omega t)$$
$$+ 2C\omega B \cos(2\omega t + \varphi). \tag{17}$$

Then, the inductor currents will be

$$i_{L1} = \frac{i_1}{1 - d_1} = \frac{i_1 v_{c1}}{v_{in}} \tag{18}$$

and

$$i_{L2} = \frac{i_2}{1 - d_2} = \frac{i_2 v_{c2}}{v_{in}} \tag{19}$$

where $d_1$ and $d_2$ are, respectively, the duty cycles of $T_1$ and $T_3$. Therefore, the input current of the inverter, which is the sum of $i_{L1}$ and $i_{L2}$, will be

$$i_{in} = \frac{V_{\max}I_{\max} + 2B^2C\omega \sin(4\omega t + \varphi) - V_{\max}I_{\max} \cos(2\omega t)}{2V_{in}}$$
$$+ \frac{\frac{1}{2}V_{\max}^2 \omega C \sin(2\omega t) + 8V_d BC \omega \cos(2\omega t + \varphi)}{2V_{in}}. \tag{20}$$

From (20), there are three components in the input current $i_{in}$. They are the dc part $\frac{V_{\max}I_{\max}}{2V_{in}}$ which is identical to (7), the component at $4\omega$ which is $\frac{2B^2C\omega \sin(4\omega t + \varphi)}{2V_{in}}$, and the low-frequency component at $2\omega$ which is

$$i_{in(2\omega)} = \frac{-V_{\max}I_{\max} \cos(2\omega t) + \frac{1}{2}V_{\max}^2 \omega C \sin(2\omega t)}{2V_{in}}$$
$$+ \frac{8V_d BC \omega \cos(2\omega t + \varphi)}{2V_{in}}. \tag{21}$$
From (21), it can be seen that if we set

\[-V_{\text{max}} I_{\text{max}} \cos(2\omega t) + \frac{1}{2} V_{\text{max}}^2 \omega C \sin(2\omega t) + 8V_d BC \omega \cos(2\omega t + \varphi) = 0\]  

(22)

then \(i_{\sin(2\omega)} = 0\). This means that there will not be a \(2\omega\) component in the input current \(i_{\sin}\). From (22), amplitude \(B\) is derived as

\[B = \frac{V_{\text{max}}}{8V_d \omega C} \sqrt{I_{\text{max}}^2 + \omega^2 C^2 V_{\text{max}}^2 / 4}\]  

(23)

and the phase angle \(\varphi\) is derived as

\[\varphi = \frac{\pi}{2} - \sin^{-1} \frac{I_{\text{max}}}{\sqrt{I_{\text{max}}^2 + \omega^2 C^2 V_{\text{max}}^2 / 4}}\]  

(24)

By ensuring that the capacitor voltages track precisely (11) and (12), of which \(B\) and \(\varphi\) are calculated from (23) and (24), the low-frequency current ripple of the inverter will be mitigated.

IV. ANALYSIS ON THE WAVEFORM CONTROL METHOD

A. Characteristics of Waveform Control

According to (23), the capacitor \(C\) and its dc offset voltage \(V_d\) are inversely proportional to \(B\). At the same time, \(V_d\) and \(B\) should satisfy the inequality given in (13). Additionally, with the boost differential inverter, a large amplitude of \(V_d\) and \(B\) would mean a big duty cycle, which may lead the converter to operate at the saturation region of the duty cycle. The size of \(C\) is also an important factor that will increase the overall size and cost of the system. Thus, with all these constraints in mind, the three parameters must be optimized and designed accordingly to the application.

Fig. 4 shows a 3-D plot of the relationship of \(C\), \(V_d\), and \(B\) calculated with \(P_o = 170\) W at \(f = 50\) Hz and \(V_{\text{max}} = \sqrt{2} \times 110\) V using (23). It can be seen that \(C = 15\) \(\mu\)F, \(V_d = 213\) V, and \(B = 43\) V. According to (24), it can be calculated that \(\varphi = 0.1659\). Thus, \(v_{c1} = 213 + 77.75 \sin(\omega t) + 43 \sin(2\omega t + 0.1659)\) and \(v_{c2} = 213 - 77.75 \sin(\omega t) + 43 \sin(2\omega t + 0.1659)\).

Fig. 5(a)–(f) shows the simulated operating waveforms of the boost inverter with a sinusoidal ac output voltage.

Fig. 5(a) and (d) shows, respectively, the waveforms of the duty cycle signal without waveform control and with the proposed waveform control, where \(d_1\) and \(d_2\) are the duty cycles of the two bidirectional boost converters. From the figures, it can be seen that the output voltage is zero at approximately \(d_1 = d_2 = 0.58\). The range of \(d_1\) and \(d_2\) for the boost inverter without waveform control is 0.33–0.69 and that with waveform control is 0.15–0.7. Both ranges are well within the practical limits of the boost converter.

Fig. 5(b) and (e) shows the waveforms of \(v_{c1}\), \(v_{c2}\), and \(v_o\) of the boost differential inverter without waveform control and with waveform control, respectively. It can be seen that the output voltage \(v_o\) is sinusoidal in both cases even though in the case of waveform control, \(v_{c1}\) and \(v_{c2}\) are distorted with a double-line-frequency component.

Fig. 5(c) and (f) shows the waveforms of \(i_{L1}\), \(i_{L2}\), and \(i_{\text{in}}\) of the inverter without waveform control and with waveform control, respectively. In the case of no waveform control, the input current \(i_{\text{in}}\) contains a high level of double-line-frequency ripple. Conversely, with the proposed waveform control, the ripple of the input current is significantly mitigated. The ripple is at four times the line frequency and the amplitude is reduced to less than 10% of that without waveform control, from 3.8 to 0.38 \(A_{\text{rms}}\).

B. Voltage and Current Stresses With Waveform Control

The maximum capacitor voltage of the inverter with the waveform control is \(v_{c1\text{max}} = v_{c2\text{max}} = 314\) V [see Fig. 5(e)] and it is higher than that of the inverter without waveform control which is \(v_{c1\text{max}} = v_{c2\text{max}} = 213 + 77.75 = 290.75\) V [see Fig. 5(b)]. Hence, the voltage stress on the power components is higher with waveform control than without waveform control.

The maximum inductor current of the inverter with waveform control is \(i_{L1\text{max}} = i_{L2\text{max}} = 6.37\) A [see Fig. 5(f)] and it is lower than that of the inverter without waveform control which is \(i_{L1\text{max}} = i_{L2\text{max}} = 7.18\) A [see Fig. 5(c)]. Hence, the current stress on the power components is lower with the waveform control than without waveform control. Additionally, the inductor current waveform is more symmetrical with the waveform control and this allows the full utilization of the bidirectional converter. According to (11), (12), (18), and (19), the relationship of \(V_d\), \(B\), and \(v_{c\text{max}}\) can be shown in Fig. 6(a) and (b), respectively. From the figures, we can see that the voltage and current stresses increase with a decreasing \(B\) and an increasing \(V_d\). The point \(V_d = 213\) V, \(B = 43\) V, \(v_{c\text{max}} = 314\) V given in Fig. 6(a) and the point \(V_d = 213\) V, \(B = 43\) V, \(i_{L\text{max}} = 6.37\) A given in Fig. 6(b) match the point in Fig. 4 when \(C = 15\) \(\mu\)F.

Therefore, to reduce the voltage and current stresses of all power components in the topology, a large \(B\) and a small \(V_d\) is suggested.
C. Flow Path of a Double-Line-Frequency Current Component

The flow path of the double-line-frequency current in the power circuit can have a significant impact on the power efficiency and it must be carefully studied. By substituting (23) and (24) into (18) and (19), we have

\[ i_{L1_w} = I_D + A_{w} \sin(\omega t + \theta_1) + A_{3w} \sin(3\omega t + \theta_3) + A_{4w} \sin(4\omega t + \theta_4) \]  

\[ i_{L2_w} = I_D + A_{w} \sin(\omega t + \theta_2) + A_{3w} \sin(3\omega t + \theta_2) + A_{4w} \sin(4\omega t + \theta_4) \]
on the other hand, without waveform control [20], [21], the expressions of the inductors currents can be derived as
\[ i_{L1t} = I_D + A_{w1} \sin(\omega t + \varphi_1) + A_{2w1} \sin(2\omega t + \varphi_2) \] (30)
and
\[ i_{L2t} = I_D - A_{w1} \sin(\omega t + \varphi_1) + A_{2w1} \sin(2\omega t + \varphi_2) \] (31)
where the coefficients \( A_{w1} \) and \( A_{2w1} \) are the amplitudes of the fundamental and harmonic components of the inductor currents, and they can be expressed as
\[ A_{w1} = \frac{V_d}{V_{in}} \sqrt{(\omega CV_{max}/2)^2 + (I_{max})^2} \] (32)
\[ A_{2w1} = \frac{\sqrt{(\omega CV_{max}/8)^2 + (V_{max}I_{max}/4)^2}}{V_{in}}. \] (33)

From (1) and (2), the expressions of the capacitor currents without waveform control can be derived as
\[ i_{c1t} = C\omega \frac{1}{2} V_{max} \cos(\omega t) \] (34)
and
\[ i_{c2t} = -C\omega \frac{1}{2} V_{max} \cos(\omega t). \] (35)

Equations (30), (31), (34), and (35) clearly show that the double-line-frequency current component will mainly flow through \( L_1 \) and \( L_2 \) instead of \( C_1 \) and \( C_2 \), as depicted in Fig. 7(b).

Since the inductor is usually a more lossy device (comprising core loss and a higher conductive loss) as compared to the capacitor, it is justifiable to conclude that the current flow path of the double-line-frequency current given in Fig. 7(b) is more power dissipative than that in Fig. 7(a). Such a conclusion is further verified by the circuit-simulation results given in Fig. 8, which shows the double-line-frequency current component flowing through each of the main circuit components. From the figure, it is shown that without waveform control, the double-line-frequency current component will mainly flow through \( C_1 \), \( C_2 \), \( T_1 \), \( T_2 \), \( T_3 \), and \( T_4 \) whereas without waveform control, the double-line-frequency current component will mainly flow through \( T_1 \), \( T_2 \), \( T_3 \), and \( T_4 \) whereas without waveform control, the double-line-frequency current component will mainly flow through \( L_1 \), \( L_2 \), \( L_3 \), and the fuel cell. This coincides with the theoretical deduction illustrated in Fig. 7. Besides, the double-line-frequency current component flowing through \( T_1 \), \( T_2 \), \( T_3 \), and \( T_4 \) will be more balanced with waveform control than that without waveform control.

\[ A_{w1} = \sqrt{\frac{V_{max}^6 \omega^2 C^2}{4096V_{in}^2 V_d^2} + \frac{31V_{max}^4 I_{max}^2}{512V_d^2 V_{in}^2} - \frac{V_{max}^3 \omega^2 C^2}{64V_d^2} - \frac{7V_{max}^2 I_{max}^2}{16V_{in}^2} + \frac{V_{max}^2 I_{max}^2}{16\omega^2 C^2 V_d^2 V_{in}^2} + \frac{\omega^2 C^2 V_d^2 V_{in}^2}{4V_{in}}} \] (27)
\[ A_{3w1} = \frac{V_{max}}{8V_d V_{in}} \sqrt{\frac{5V_{max} I_{max}^2}{8} + \frac{9V_{max}^2 \omega^2 C^2}{64} + \frac{I_{max}^4}{4\omega^2 C^2}} \] (28)
\[ A_{4w1} = \frac{V_{max}^2 I_{max}^2}{64\omega CV_d V_{in}} + \frac{V_{max}^4 \omega C}{256V_d V_{in}} \] (29)
D. Effect of Capacitance Tolerance

Since the values of the capacitors $C_1$ and $C_2$ can affect the computation of the proposed waveform control, the effect of using a difference capacitance from that originally assumed in the computation on the control performance must be investigated. First, the parameters $C_1$ and $C_2$ in (23) and (24) are chosen as $C_1 = C_2 = 15 \, \mu F$ for the voltage reference calculation adopted in waveform control. Then, a circuit simulation with $C_1$ and $C_2$ in the power stage varying from 5 to 25 \, \mu F is performed. The simulated results are given in Fig. 9. It is observed that a larger deviation of the capacitor value from the assumed value of 15 \, \mu F leads to a poorer compensation of the double-line-frequency component. Yet, as the tolerance of the film capacitor is usually less than 10\%, the effect of capacitance tolerance on the compensation capability is small (less than 8.19\%), as given in Fig. 9.

E. Further Remarks

The adoption of the proposed waveform control method to mitigate the low-frequency input current ripple will alter the original behavior of the differential inverter without waveform control. The following are important points to consider in terms of the adoption of waveform control:

1) there is no change in the desired ac output voltage even though the voltages of the capacitors themselves are altered;
2) the energy stored by the capacitors, which is a function of the voltages, is made up of a dc component and a double-line-frequency component;
3) DC energy is stored by the two capacitors while they supply ac energy to the output load. Consequently, the low-frequency power pulsation caused by ac output is absorbed by the capacitors while the fuel cells kept a constant supply of dc power to the capacitors;
4) as the capacitor voltages $v_{c1}$ and $v_{c2}$ are much higher than the dc input voltage $v_{in}$, the energy transfer will occur when the voltage fluctuation on $C_1$ and $C_2$ is increased.

An interesting point to take note is that since the capacitor voltages can be large without affecting the desired ac output voltage, both capacitors can be minimized without increasing the ripple voltage on the dc input. The advantage is that film capacitors can be used instead of electrolytic capacitors to improve reliability. The practical limit is the voltage rating of the capacitors.

Another important point is that with the use of differential inverter, one may take an issue with the fuel cell having a floating ground that is in common with the high-frequency differential inverter [20], [21]. Note that as the output voltage of most fuel cells is relatively low as compared to the ac output requirement, there is no requirement for the fuel cell’s output be grounded to the earth. However, if the metallic part of the fuel-cell system is exposed, then such a requirement is present [32]. In the case of differential inverters being used in applications where the ac output is connected to a single load, the fuel cell can be directly grounded to the earth, if necessary. On the other hand, as the output voltage of most fuel cells is relatively low as compared to the ac output requirement, it is typically necessary to include an isolated front-end boost stage before the differential inverter.

In this case, the fuel cell can also be grounded to the earth, if needed.
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V. EXPERIMENTAL RESULTS AND DISCUSSIONS

A. Control Block and Experimental Setup

To validate the proposed waveform control method, the boost differential inverter prototype as shown in Fig. 3 was implemented. The specifications of the prototype are given in Table I. The control platform is implemented using TMS320LF2812.

In this study, the boost inverter is based on a dual-loop control, of which each boost converter is controlled by means of an inner inductor current control loop and an outer output voltage control loop. An overview of the control block is shown in Fig. 10. Both control loops are designed using the averaged continuous-time model of the boost converter topology.

The principle of the control mechanism is as follows. First, the ac output voltage reference is split into the two respective voltage references $v_{c1\text{ref}}$ and $v_{c2\text{ref}}$ of the two boost converters as given in (23) and (24). The references $v_{c1\text{ref}}$ and $v_{c2\text{ref}}$ are compared with the feedback voltages $v_{c1}$ and $v_{c2}$ of the converters and fed into a proportional-integral (PI) (outer-loop) compensator, which generates the reference currents $i_{L1\text{ref}}$ and $i_{L2\text{ref}}$ for the inductor current control. These current references are compared with the feedback currents of the inductors $L_1$ and $L_2$ and are fed into another PI (inner-loop) compensator, which is followed by a pulse-width modulator (PWM) to produce the desired duty cycles $d_1$ and $d_2$. The duty cycles are controlled between 0.1 and 0.7 to generate the voltages as described in (3), (11), and (12). With this control, the inverter is capable of maintaining a stable and reliable operating condition by means of limiting the inductor current.

It is possible for the output of the differential inverter to contain a dc offset component due to control time delays and practical imperfections. Such an offset is prohibited and should be minimized when the inverter is to be connected to the grid [33]. In this work, the dc offset voltage compensation loop is included in the control, as shown in the control block given in Fig. 10. By introducing a dc current control loop into the controlled system, the dc offset voltage of the output will be regulated to zero. The control block diagram in Fig. 10 including

| TABLE I |
| SPECIFICATIONS OF A BOOST DIFFERENTIAL INVERTER |

<table>
<thead>
<tr>
<th>Input voltage $V_{in}$</th>
<th>90 V</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output voltage (RMS)</td>
<td>110 V</td>
</tr>
<tr>
<td>Rated power $P_e$</td>
<td>170 W</td>
</tr>
<tr>
<td>Fundamental frequency $f$</td>
<td>50 Hz</td>
</tr>
<tr>
<td>Switch frequency $f_s$</td>
<td>20 kHz</td>
</tr>
<tr>
<td>Inductors ($L_1$, $L_2$)</td>
<td>300 µH, 10 A</td>
</tr>
<tr>
<td>Capacitors ($C_1$, $C_2$)</td>
<td>15 µF, 800 V, film cap.</td>
</tr>
</tbody>
</table>

Fig. 10. Overview of the control block diagram of the differential inverter.
the digital PI controller is implemented using the DSP unit TMS320LF2812.

B. Under a Resistive Load

Fig. 11(a)–(d) shows the voltage and current waveforms of the boost inverter operating at rated power under a pure resistive \( R \) load for both cases of with and without waveform control. Fig. 11(a) and (c) shows the waveforms of the capacitor voltages, output voltage, and load current of the inverter, respectively, without waveform control and with waveform control. It is illustrated that the same output voltage and load current can be obtained from both control methods even though the capacitor voltages are different. Fig. 11(b) and (d) shows the waveforms of the inductor current and the input current of the inverter, respectively, without waveform control and with waveform control. It is illustrated that with the proposed waveform control method, the input current ripple is mitigated to a magnitude of less than 13% (from 4 to 0.5 A) of the ripple obtained without waveform control.

Fig. 12(a) and (b) shows, respectively, the frequency spectrum characteristic of the input current of the inverter without waveform control and with waveform control. For the case of no waveform control, the 100 Hz current ripple (amplitude of 1.11 A) is 48.1% of dc current (2.31 A). However, for the case of waveform control, the 100 Hz current ripple (amplitude of 0.07 A) is only 3% of dc current (2.37 A), which is well within the limits suggested in [9]. The 200 Hz current ripple of the inverter without waveform control is 1.1% of dc current (amplitude of 0.026 A) and with waveform control is 5% of dc current (amplitude of 0.1176 A). However, this has only negligible effect on the fuel cells.

Fig. 12(c) and (d) shows, respectively, the frequency spectrum characteristic of the output voltage of the inverter without waveform control and with waveform control. Here, the total harmonic distortion (THD) of the output voltage of the inverter without waveform control is 1.089% and with waveform control is 2.36%. Both are within the limit of the ac grid requirements [34].

C. Under a Resistive-Capacitive Load

To further show the validity of the proposed method, other load conditions are tested. Here, \( RC \) load is chosen. Fig. 13(a)–(d) shows the voltage and current waveforms of the boost inverter operating at rated power under a resistive-capacitive \( RC \) load. Fig. 13(a) and (c) shows, respectively, the waveforms of the capacitor voltages, output voltage, and load current of the inverter, respectively, without waveform control and with waveform control. It is illustrated that with the proposed waveform control method, the input current ripple is mitigated
Fig. 12. Input current and output voltage frequency characteristics under pure resistive load \((R = 70.5 \, \Omega)\). (a) Input current without waveform method. (b) Input current with the proposed method. (c) Output voltage without waveform method. (d) Output voltage with the proposed method.

to a magnitude of less than 40\% (from 4 to 1.6 A) of the ripple that is obtained without waveform control.

Fig. 14(a) and (b) shows, respectively, the frequency spectrum characteristic of the input current of the inverter without waveform control and with waveform control. For the case of no waveform control, the 100 Hz current ripple (amplitude of 1.01 A) is 55.4\% of dc current (1.82 A). However, for the case of with waveform control, the 100 Hz current ripple (amplitude of 0.22 A) is only 11.9\% of dc current (1.84 A), which is well within the limits suggested in [9]. The 200 Hz current ripple of the inverter without waveform control is 0.79\% of dc current (amplitude of 0.015 A) and with waveform control is 8.9\% of dc current (amplitude of 0.1647 A). This has negligible effect on the fuel cells.

Fig. 14(c) and (d) shows, respectively, the frequency spectrum characteristic of the output voltage of the inverter without waveform control and with waveform control. Here, the THD of output voltage of the inverter without waveform control is 0.69\% and with waveform control is 2.55\%, which are within the limit [34].

D. Comparative Study of Waveform Control Versus No Waveform Control With Circuit Modification

As mentioned, without waveform control, the double-line-frequency current component will not flow through capacitors \(C_1\) and \(C_2\). Therefore, a change in their capacitance values will not affect the current ripple. Consequently, the mitigation of the double-line-frequency component of the input current of the inverter without waveform control can be achieved only through the application of an extra device (e.g., by inserting an input capacitor to the inverter) or the use of an auxiliary converter that can alter the flow path of this component.

In this section, a comparative study on the addition of an input capacitor to the inverter without waveform control as compared to the use of waveform control is performed. Here, the double-line-frequency ripple levels under various configurations are performed. With the same capacitances \(C_1 = C_2 = 15 \, \mu F\) and the same load \((R = 70.5 \, \Omega)\), the output voltage and input current waveform of the inverter for four separate cases are given in Fig. 15. The configurations of the four cases are as follows—Case I: without waveform control (no input capacitor); Case II: without waveform control but with 220 \(\mu F\) input electrolytic capacitor; Case III: without waveform control but with 2240 \(\mu F\) input electrolytic capacitor; Case IV: with proposed waveform control (no input capacitor).

From Fig. 15, it is shown that the output voltage \(v_o\) can be controlled as sinusoidal; however, the peak-to-peak (double-line-frequency component) of the input current is, respectively, 4, 3.8, 3.4, and 0.5 A in the four cases. With the same set of \(C_1\) and \(C_2\) values, the use of the proposed waveform control method produces the minimal current ripple. The input current
Fig. 13. Voltage and current waveforms of the inverter under a resistive-capacitive load \((R = 70.5 \, \Omega, C = 65 \, \mu F)\). (a) The voltage waveform without waveform control method. (b) The current waveform without waveform control method. (c) The voltage waveform with the proposed method. (d) The current waveform with the proposed method.

Fig. 14. Input current and output voltage frequency characteristics under resistive-capacitive load \((R = 70.5 \, \Omega, C = 65 \, \mu F)\). (a) Input current without waveform method. (b) Input current with the proposed method. (c) Output voltage without waveform method. (d) Output voltage with the proposed method.
VI. CONCLUSION

A waveform control method for mitigating low-frequency current ripple in fuel-cell inverter systems is proposed in this paper. The mechanism of the proposed method is analyzed, discussed, and experimentally verified. It is shown that with the proposed method, the low-frequency power pulsation caused by ac output is absorbed by the capacitors while the fuel cells kept a constant supply of dc power to the capacitors, thereby eliminating the effect of low-frequency ripple from affecting the properties of fuel cells. Since capacitor voltages can be large without affecting the desired ac output voltage, capacitors of the inverter can be minimized. This allows the use of film capacitors over electrolytic capacitors, thereby improving the inverter's lifetime. The proposed method is applicable in systems where current ripple mitigation is required, such as for the purpose of eliminating electrolytic capacitor in PV and LED systems.

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