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<td><strong>Author(s)</strong></td>
<td>Chan, SC; Tsui, KM; Wu, HC; Hou, Y; Wu, YC; Wu, FF</td>
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<tr>
<td><strong>Citation</strong></td>
<td>IEEE Signal Processing Magazine, Special Issue on Signal Processing Techniques for Smart Grid, 2012</td>
</tr>
<tr>
<td><strong>Issued Date</strong></td>
<td>2012</td>
</tr>
<tr>
<td><strong>URL</strong></td>
<td><a href="http://hdl.handle.net/10722/164066">http://hdl.handle.net/10722/164066</a></td>
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Load/Price Forecasting and Managing Demand Response for Smart Grids

With the promises of smart grids, power can be more efficiently and reliably generated, transmitted, and consumed over conventional electricity systems. Through the two-way flow of information between suppliers and consumers, the grids can also adapt more readily to the increased penetration of renewable energy sources and encourage users’ participation in energy savings and cooperation through the demand-response (DR) mechanism. An important issue in smart grids is therefore how to manage DR to reduce peak electricity load and hence future investment in thermal generations and transmission networks, and better utilize renewable energies to reduce our dependence on hydrocarbon. Effective DR depends critically on demand management and price/load/renewable energy forecasting, which call for sophisticated signal processing and optimization techniques. The objectives of this article are to: 1) introduce to the signal processing community the concept of smart grids, especially on the problems of price/load forecasting and DR management (DRM) and optimization, 2) highlight related signal processing applications and state-of-the-art methodologies, and 3) share the authors’ research experience through concrete examples on price predictions and DRM and optimization, with emphasis on recursive online solutions and future challenges.

SMART GRID

MOTIVATION

The efficient utilization, control, and exploration of various energy resources have always been subjects of great concern to our society. Conventional power systems are optimized to generate electricity, based primarily on fossil-fueled centralized generating stations, and move it through a one-way transmission and distribution (T&D) system to the consumers. However, to further improve cost-effectiveness and reliability in production and delivery of electricity to
meet the growing demand and to reduce the production of greenhouse gas emissions, there is a need to transform gradually the existing power systems or power grids to “smarter” ones that incorporate advanced technologies to offer better flexibility, reliability, and security with large-scale integration of various renewable energies and support of the growing fleet of electric vehicles to reduce the dependence of oil and hydrocarbon. This calls for a “smart grid,” which allows efficient, flexible and reliable two-way flow of energy and information for better coordination between suppliers and customers and control of the power grids (see [11] and Figure 1 for an illustration). This also allows better utilization of existing assets to maintain long-term sustainability.

Apart from the economic benefit brought along by the increased energy efficiency, there is also an urgent global need to reduce carbon emissions such as carbon dioxide, which is closely tied up with the generation and hence consumption of electricity [1]. Generally, this can be reduced by using clean (or cleaner) energy sources and the control of electricity consumption or demands at the users’ side. Technologies for reducing carbon dioxide in electricity generation using coal such as carbon capture and sequestration will continue to evolve and be deployed. Alternate energy sources with much less carbon emissions include natural gas, hydro, geothermal, wind, solar and nuclear energies, among which wind and solar have received much attention because of no pollution and minimal environmental impact. There is already a high penetration of wind farms in Europe amounting to two-thirds of the world’s capacity. In the United States, Texas has relatively high wind penetration. Rooftop as well as large-scale solar photovoltaic panels are also widely deployed. However, unlike conventional forms of generation, these distributed wind and solar energies are variable in nature and cannot be controlled. Their integration to the grid not only requires specific technology [2], [3] but also efficient control strategies for reliable grid operation, since the grid must always maintain a real-time (RT) balance of load and generation.

**IMPACT OF RENEWABLE ENERGY TO FUTURE GRIDS**

In conventional power systems, electricity is generated centrally using thermo and limited renewable resources, which are then transmitted at high voltages through transmission lines to minimize energy lost. The voltage is then stepped down at substations using transformers to feed the distribution networks of the customers. Broadly speaking, conventional power systems can be broken into generation, transmission, substation, distribution, and the customer, which do not
interact much with each other to simplify design and control. The aggregate load is usually highly predictable and hence the thermo generators and other spinning reserve can be scheduled a day ahead to satisfy the predicted load demand after taking into physical constraints arising from transmission capacity and physical on/off and ramp up/down time of thermo and other generators. This problem is commonly referred to as the unit-commitment (UC) problem [4]. RT adjustment is then performed the next day to meet RT demand. This process is generally deterministic and controllable and is now employed on a daily basis in power markets of the United States (see the section “Demand-Response Management and Optimization” for more details). With increased usage of renewable energies in the future, the operation of the power system will become more dynamic and stochastic in nature. In fact, it is expected to provide 20% of the U.S. electricity market by 2030 [5]. This open problem not only calls for reliable wind/solar power forecasting methods, increased use of high-capacity electricity storage, and a flexible grid to deliver the intermittent energy to end users, but also sophisticated scheduling and optimization algorithm to harvest these free energies, while maintaining reliable and stable grid operation.

Currently, frequent wind entailments were reported in [6] and [7] due to limited local transmission capacity and low loads. A wind curtailment of 380,000 MWh amounting to approximately US$21.4 million was reported in Texas at the McCamey area in 2002. Therefore, there is a growing trend to employ distributed energy resources (DER) for standalone facilities such as campus, remote units, or even home power generation. DER encompasses a wide range of prime mover technologies, such as internal combustion (IC) engines, gas turbines, microturbines, photovoltaic systems, fuel cells, wind power, and ac storage [8]. Most emerging technologies have an inverter to interface with the electrical distribution system. With increased utilization of renewable energies, DER have potentially lower emissions, lower operating costs, and better power quality (PQ) due to availability of local generators. Moreover, the facilities can also be viewed as demand responsive loads, and their energy consumption from the grid can be curtailed in case of peak load or emergency. In case of power failure, the facilities can even be put in an intentional island mode (called islanding), in which power will be grabbed from distributed resources or local generators until the grid is back online. This not only helps to balance the energy load and the deferral of T&D upgrades but also drastically simplifies the grid’s management of a wide and dynamic set of resources. Moreover, the surplus energy can be fed back into the grid. The integrated energy system, which consists of interconnected loads and DER and can operate in parallel with the grid or in island, is also called a microgrid. Microgrids also facilitate local consumption and distributed storage of renewable energies and alleviate the wind curtailment problem due to T&D network capacity limitation in case of excessive wind generation.

**WHY DEMAND RESPONSE?**

As mentioned earlier, another mission of the smart grid is to facilitate the general public to participate in energy-saving programs through education and electronically available information so as to control their energy consumption and costs. Such cooperative actions can also benefit the power utilities in reducing the peak loads and hence the huge investment in upgrading the grids and greenhouse gas emissions. It is estimated that the capacity to meet demand during the top 100 hours in the year accounts for 10–20% of electricity costs [9], since generation and transmission capacity is provided to meet peak demand that occurs infrequently [10]. Such inefficiency at peak demand can be mitigated by introducing the concept of DR, which generally refers to mechanisms used to encourage consumers to reduce demand, thereby reducing the peak electricity load. Current DR schemes are implemented with commercial as well as residential customers, often through either incentive-based or time-based rates DR schemes [11], [12]. In incentive-based DR, customers enroll voluntarily in certain rewarding programs or schemes and allow the operators to control directly some of their electric appliances such as air conditioners (ACs) to shed loads during peak or emergency. Time-based rates relies on dynamic pricing of electricity to regulate electricity consumption and can take many different forms.

<table>
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<th>TABLE 1</th>
<th>A SUMMARY OF KEY BENEFITS AND CONCEPT OF SMART GRIDS (FROM [16]).</th>
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<tbody>
<tr>
<td><strong>THE GRID</strong></td>
<td>“THE GRID” REFERS TO THE ELECTRIC GRID, A NETWORK OF TRANSMISSION LINES, SUBSTATIONS, TRANSFORMERS, AND MORE THAT DELIVER ELECTRICITY FROM THE POWER PLANT TO YOUR HOME OR BUSINESS.</td>
</tr>
<tr>
<td><strong>WHAT MAKES A GRID “SMART?”</strong></td>
<td>IN SHORT, THE DIGITAL TECHNOLOGY THAT ALLOWS FOR TWO-WAY COMMUNICATION BETWEEN THE UTILITY AND ITS CUSTOMERS, AND THE SENSING ALONG THE TRANSMISSION LINES IS WHAT MAKES THE GRID SMART, LIKE THE INTERNET. THE SMART GRID WILL CONSIST OF CONTROLS, COMPUTERS, AUTOMATION, AND NEW TECHNOLOGIES AND EQUIPMENT WORKING TOGETHER, BUT IN THIS CASE, THESE TECHNOLOGIES WILL WORK WITH THE ELECTRICAL GRID TO RESPOND DIGITALLY TO OUR QUICKLY CHANGING ELECTRIC DEMAND.</td>
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<tr>
<td><strong>BENEFITS ASSOCIATED WITH THE SMART GRID</strong></td>
<td>■ MORE EFFICIENT TRANSMISSION OF ELECTRICITY ■ QUICKER RESTORATION OF ELECTRICITY AFTER POWER DISTURBANCES ■ REDUCED OPERATIONS AND MANAGEMENT COSTS FOR UTILITIES, AND ULTIMATELY LOWER POWER COSTS FOR CONSUMERS ■ REDUCED PEAK DEMAND, WHICH WILL ALSO HELP LOWER ELECTRICITY RATES ■ INCREASED INTEGRATION OF LARGE-SCALE RENEWABLE ENERGY SYSTEMS ■ BETTER INTEGRATION OF CUSTOMER-OWNER POWER GENERATION SYSTEMS, INCLUDING RENEWABLE ENERGY SYSTEMS ■ IMPROVED SECURITY</td>
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ranging from simple schemes such as scheduled time-of-use (TOU) pricing to schemes that set higher prices only during critical peak periods, peak-pricing (PP) to RT-pricing (RTP) at regular intervals based on, say, the wholesale market rates. For appropriate pricing to be released electronically to the consumers and their cooperative response, the consumption at peak hours may be reduced because customers can shift usage to off-peak periods, curtailing less important loads and compromising slightly the quality of services according to their “sensitivity to price.” Although recent studies [13], [14] and pilot studies [15] show great promise of DR, there are, however, still many complications and obstacles in its launching. First, RTP may result in the volatility of the cost of electricity, which may significantly impact low-income customers whom may not be able to shift usage sufficiently to save on their overall bill. Second, advanced metering infrastructure (AMI), so-called “smart meters,” has to be extensively deployed to exchange hourly pricing and other information to support various DR programs, which requires a considerable investment. On the other hand, automated home/building energy management systems (EMS) at commercial and residential customers need to be developed to control their electrical appliances in response to demand requests or RTP (see Tables 1 and 2 for AMI, smart home, and related concepts). This has received much attention in the research and industrial communities and new systems are now rolling out. The development of low-cost integrated home EMS with RT networking, intelligence control, and optimization of electric appliances using advanced digital signal processing techniques (Figure 2) are thus of paramount importance. Finally, many operators are still using fixed electricity pricing and reducing customers’ electricity bills may imply a cut in their revenues, which hinders further development. Therefore, an appropriate DR scheme has yet to be found that can produce a win-win situation, i.e., lowering the costs of both utilities and customers. Fortunately, evidence from recent studies indicates that there is increasing motivation for utilities to deploy DR as they can serve as dynamic loads for better system control and integration of renewable energies. Moreover, we shall show in the section “Demand Response-Management and Optimization” that with effective optimization techniques, users can better respond to RTP and considerable savings in electricity cost and reduction of peak load can be realized.

**KEY BENEFITS**

Some of the key benefits and concept of the smart grid envisioned by the U.S. Department of Energy [16] are summarized in Table 1. A diagram showing the future electricity system is given in Figure 1. In this article, we wish to introduce a general picture of the smart grid to the signal processing community, especially on the important issues of price/load forecasting, management of DR, and highlight some possible signal processing applications. After a brief review of estimation theory and related signal processing challenges for the smart grid in the section “Potential Applications of Signal Processing Techniques to Smart Grids,” we review the state-of-the-art methodologies for price/load forecasting and related prediction problems. Finally, we focus on the various aspects of DRM and optimization. Due to page-length

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**TABLE 2** A SUMMARY OF THE CONCEPT OF SMART METERS, SMART HOME, EMS, HOME POWER GENERATION (FROM [16]), AND MICROGRIDS (FROM [8]).

<table>
<thead>
<tr>
<th>SMART METERS AND HOME EMS</th>
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<tr>
<td><strong>SMART METERS</strong> PROVIDE THE SMART GRID INTERFACE BETWEEN THE CUSTOMERS AND THEIR ENERGY PROVIDERS. THEY OPERATE DIGITALLY AND ALLOW FOR AUTOMATED AND COMPLEX TRANSFERS OF INFORMATION BETWEEN THE TWO PARTIES. FOR INSTANCE, SMART METERS WILL DELIVER SIGNALS FROM ENERGY PROVIDERS THAT CAN HELP THEIR CUSTOMERS CUT ELECTRICITY COSTS AND PROVIDE UTILITIES WITH GREATER INFORMATION ABOUT HOW MUCH ELECTRICITY IS BEING USED THROUGHOUT THEIR SERVICE AREAS. THIS ENERGY INFORMATION COMING TO AND FROM A CUSTOMER’S HOME THROUGH THE SMART METER CAN BE RUN THROUGH A HOME EMS, WHICH WILL ALLOW ONE TO VIEW THE INFORMATION ON A COMPUTER OR HAND-HELD DEVICE. A HOME EMS ALSO ALLOW THE CUSTOMERS TO TRACK THE ENERGY USE IN DETAIL TO BETTER SAVE ENERGY, MONITOR RT INFORMATION AND PRICE SIGNALS FROM THEIR UTILITY, CREATE SETTINGS TO AUTOMATICALLY USE POWER WHEN PRICES ARE LOWEST, AND ALLOW SPECIFIC APPLIANCES AND EQUIPMENT TO TURN OFF AUTOMATICALLY WHEN A LARGE DEMAND THREATENS TO CAUSE AN OUTAGE OR AVOIDING PEAK DEMAND RATES. THIS HELPS TO BALANCE THE ELECTRICITY LOAD AND PREVENT BLACKOUTS. THE UTILITY MAY IN RETURN PROVIDE FINANCIAL INCENTIVES.</td>
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<tr>
<th>SMART HOME AND SMART APPLIANCES</th>
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<tr>
<td>IN A SMART HOME, COMPUTERIZED CONTROLS IN A CONSUMER’S HOME AND APPLIANCES CAN BE SET UP TO RESPOND TO SIGNALS FROM THE ENERGY PROVIDER TO MINIMIZE THEIR ENERGY USE AT TIMES WHEN THE POWER GRID IS UNDER STRESS FROM HIGH DEMAND, OR EVEN TO SHIFT SOME OF THEIR POWER USE TO TIMES WHEN POWER IS AVAILABLE AT A LOWER COST. THESE “SMART APPLIANCES” WILL BE NETWORKED TOGETHER, ALLOWING THE CUSTOMERS TO ACCESS AND OPERATE THEM THROUGH THE EMS. SMART APPLIANCES WILL ALSO BE ABLE TO RESPOND TO SIGNALS FROM YOUR ENERGY PROVIDER TO AVOID USING ENERGY DURING TIMES OF PEAK DEMAND. FOR INSTANCE, A SMART AIR CONDITIONER MIGHT EXTEND ITS CYCLE TIME SLIGHTLY TO REDUCE ITS LOAD ON THE GRID, WHILE GOING UNNOTICED BY THE CUSTOMERS. OF COURSE, THESE SMART APPLIANCES WILL INCLUDE CONSUMER CONTROLS TO OVERRIDE THE AUTOMATED CONTROLS WHEN NEEDED.</td>
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<tr>
<th>HOME POWER GENERATION AND MICROGRIDS</th>
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<tr>
<td>ROOFTOP SOLAR ELECTRIC SYSTEMS AND SMALL WIND TURBINES ARE NOW WIDELY AVAILABLE, AND EVEN SMALL HYDROPOWER SYSTEMS ARE CONSIDERED TO BE INSTALLED ON A NEARBY STREAM. COMPANIES ARE ALSO STARTING TO ROLL OUT HOME FUEL CELL SYSTEMS, WHICH PRODUCE HEAT AND POWER FROM NATURAL GAS, AS CONSUMERS MOVE TOWARD HOME ENERGY GENERATION SYSTEMS WITH THESE DEVICES. THE INTERACTIVE CAPACITY OF THE SMART GRID WILL BECOME MORE AND MORE IMPORTANT. THE SMART GRID, WITH ITS SYSTEM OF CONTROLS AND SMART METERS, WILL HELP TO EFFECTIVELY CONNECT ALL THESE MINIPOWER GENERATING SYSTEMS TO THE GRID, TO PROVIDE DATA ABOUT THEIR OPERATION TO UTILITIES AND OWNERS, AND TO KNOW WHAT SURPLUS ENERGY IS FEEDING BACK INTO THE GRID VERSUS BEING USED ON SITE. A POTENTIAL FEATURE OF THE SMART GRID WILL BE TO ALLOW THE COMMUNITY TO USE THEIR SOLAR ARRAY—AND THEIR NEIGHBORS’—TO KEEP THE LIGHTS ON EVEN WHEN THERE IS NO POWER COMING FROM A UTILITY. CALLED “ISLANDING,” IT WILL ALLOW A HOME TO GRAB POWER FROM DISTRIBUTED RESOURCES UNTIL THE GRID IS BACK ONLINE. HOME POWER GENERATION IS CLOSERLY RELATED TO THE CONCEPT OF MICROGRIDS. ACCORDING TO [8], MICROGRIDS ARE INTEGRATED ENERGY SYSTEMS CONSISTING OF INTERCONNECTED LOADS AND DISTRIBUTED ENERGY RESOURCES WHICH, AS A SYSTEM, CAN OPERATE IN PARALLEL WITH THE GRID OR IN AN INTENTIONAL ISLAND MODE. DYNAMIC ISLANDING IS A KEY FEATURE OF A MICROGRID.</td>
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</table>
To realize the promises of the smart grid, a wide range of communications, electronics, and other related technologies have to be deployed at various levels of the grid. For instance, automatic sensors such as phase measurement units (PMUs) [17] will increasingly be deployed at both T&D levels. Such units allow RT synchronous measurements of voltages and currents at transmission lines and distribution stations. This facilitates reliable detection, isolation, and recovery of faults and greatly simplifies distributed state estimations in power systems [18] to offer better monitoring for system stability, optimization, and recovery (self-healing). Moreover, with increased state estimation at the distribution level, the PQ of customers can be improved by detecting PQ events such as voltage dwells and take appropriate recovery actions. Both parametric and nonparametric estimation methods have been proposed to estimate important parameters such as frequency, amplitudes, and transients of power signals [19].

Time-critical communication technologies are also required to transmit reliably data and control information across the grid for proper operation. The large amount of information exchange between the users and suppliers also calls for an efficient compression method and secure transmission schemes. On the consumer side, low-cost and low-power automated home EMS with networked smart electric appliances possessing DR capability also need to be developed. Energy efficient methodologies at the circuits and systems level remain prime movers to reduce power consumption.

**COMMUNICATIONS OF SMART DEVICES**

An important signal processing application to the smart grid is advanced communications technology to facilitate information exchange between smart devices. For instance, wireless networks are popular because of their cost effectiveness. However, the network reliability and throughput are often affected by network congestion. A multigate mesh network architecture recently reported in [71] utilizes a timer-based multipath diversity routing scheme so that the transmission path and gateways can be flexibly chosen to reduce interference from other signals. Moreover, a novel backpressure-based packet scheduling scheme is used to balance the network traffic among multiple pathways. These methods significantly improve network reliability and reduce network congestion. On the other hand, power line communication (PLC) technology is gaining popularity for its low deployment cost and network latency. It exploits the existing power grid so that the deployment cost can be greatly reduced. Since the communication channel is owned by the utility, network security and latency can be directly controlled. A recent review in [72] shows that the PLC can be applied to different components of the smart grid, from high-voltage lines to smart meters down to and within the home.

With advances in these secure transmission schemes, the network throughput can be improved so that it is possible to exchange a large amount of information between the users and suppliers. This calls for efficient signal processing algorithms to analyze the information so that decisions can be made by the home EMS in a shorter time interval to provide finer control of appliances and achieve better DR on the customers’ side, and a more accurate prediction of the users’ demand can be performed to better coordinate the power resources at the utility side.

**TIME-SERIES ANALYSIS FOR FORECASTING AND ANALYSIS**

According to [20], a fully realized grid will be self-healing, flexible, predictive, interactive, optimized, and secure. To be able to predict the behaviors of the grid and customers, one needs to establish appropriate models and estimate the corresponding parameters from measurements using statistical estimation techniques. Based on these models, one can then make prediction of its behavior in the future. This is also closely related to machine learning, event detection, and time-series

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**TO BE ABLE TO PREDICT THE BEHAVIORS OF THE GRID AND CUSTOMERS, ONE NEEDS TO ESTABLISH APPROPRIATE MODELS AND ESTIMATE THE CORRESPONDING PARAMETERS FROM MEASUREMENTS USING STATISTICAL ESTIMATION TECHNIQUES.**
analysis. Here, we provide a brief review of estimation theory for time series and highlight their potential applications in smart grid systems. They can be integrated with other time-series analysis tools such as artificial neural networks (ANNs) and support vector machines (SVMs) [73].

Most electric appliances such as ACs, heaters, and ventilation units can be described by differential equations [21], [22] involving device-specific as well as environment parameters. In the digital domain, its evolution behaviors can therefore be described by the discrete-time nonlinear state-space models (SSMs) in (1a) and (1b), where \( x_k, u_k, z_k \) are respectively the state, input, and observation vectors at the \( k \)th time instant of the dynamical system.

**Nonlinear SSM**

\[
\begin{align*}
\text{State equation} & : x_k = \mathbf{h}(x_{k-1}, u_k) + w_k \quad (1a) \\
\text{Measurement equation} & : z_k = \mathbf{g}(x_k, u_k) + v_k \quad (1b)
\end{align*}
\]

State equation \( x_k = A_k x_{k-1} + B_k u_k + w_k \) \( (2a) \)

Measurement equation \( z_k = C_k x_k + D_k u_k + v_k \) \( (2b) \)

Equation (1a) is called the state equation, and it describes the evolution of the states as a function of the previous state and input through the nonlinear vector function \( \mathbf{h}(\cdot) \) and \( w_k \) with probability density function (pdf) \( p_w(\cdot) \), represents the modeling errors and other disturbance. Equation (1b) is called the measurement equation, which describes the relationship between the states to be measured either directly or indirectly and the measurements or observations through the nonlinear vector function \( \mathbf{g}(\cdot) \) with \( v_k \) representing the measurement noise with pdf \( p_v(\cdot) \). and \( v_k \) are usually assumed to be mutually independent. For linear discrete-time state-space systems, (1a) and (1b) will reduce to (2a) and (2b), where \( A_k \) and \( B_k \) are respectively the state transition matrix and the control input matrix, and \( C_k \) and \( D_k \) denote the observation model which maps the state and input spaces into the observation space. For time-series problems, the control input \( u_k \) is usually omitted. The state vector \( x_k \) and hence matrix \( C_k \) will depend on the particular model used. For example, in the linear model \( z_k = w_k' x_k + v_k \), where \( u_k \) is the input and \( x_k \) are the parameters to be determined. If \( u_k = [z_{k-1}, z_{k-2}, \ldots, z_{k-L}]^T \), we obtained an \( L \)th order AR model and \( x_k \) contains the AR coefficients. Let \( Z_k \) be the set of measurements up to the \( k \)th time instance, then the a priori probability of \( x_k \) given the posterior density at the \( (k-1) \)th time instant \( p(x_k|Z_{k-1}) \) can be expressed as (3).

**Bayesian Kalman Filter**

**Predict**

\[
p(x_k|Z_{k-1}) = \int p(x_k|x_{k-1}) p(x_{k-1}|Z_{k-1}) \, dx_{k-1}
\]

\[
= \int p(x_{k-1}|Z_{k-1}) p(x_k|x_{k-1}) \, dx_{k-1}
\]

**Update**

\[
p(x_k|Z_k) = c_k p(x_k|Z_{k-1}) p(Z_k|x_k) / p(Z_k|x_{k-1})
\]

\[
c_k^{-1} = \int p(z_k|x_k)p(x_k|Z_{k-1}) \, dx_k
\]

Kalman Filter

\[
\hat{x}_{k|k-1} = A_k \hat{x}_{k-1|k-1}
\]

\[
P_{k|k-1} = A_k P_{k-1|k-1} A_k^T + Q_k
\]

Bayesian Kalman Filter

**Predict**

\[
p(x_k|Z_{k-1}) = c_k p(x_k|x_{k-1}) p(x_{k-1}|Z_{k-1})
\]

**Update**

\[
p(x_k|Z_k) = c_k p(x_k|Z_{k-1}) p(Z_k|x_k) / p(Z_k|x_{k-1})
\]

\[
c_k^{-1} = \int p(z_k|x_k)p(x_k|Z_{k-1}) \, dx_k
\]

In other words, we can “predict” the density of \( x_k \) from the state equation and posterior density obtained at the previous iteration. After receiving the \( k \)th measurement, one can utilize Bayes’ rule to “update” the posterior density of the state as in (4). This process can be repeated for each new incoming measurement to form a recursive online algorithm called the Bayesian Kalman filtering (BKF) algorithm [23], [24]. If \( v_k \) and \( w_k \) are zero mean Gaussian distributed, then (3) and (4) can be simplified analytically to the conventional Kalman filter (KF) [25] shown in (5) and (6), where \( Q_k \) and \( R_k \) are the covariance of \( v_k \) and \( w_k \), respectively. The subscripts in \( \hat{x}_{k|k-1} \) and \( \hat{x}_{k|k} \), etc., are used to denote quantities after prediction and update.

For time-series analysis, the state equation may be unknown, and it is either imposed as prior information or estimated online from past estimates using the expectation-maximization (EM) algorithm [26]. A common approach is to choose \( A_k \) as the identity matrix where \( \hat{x}_{k|k} \) is constrained around the previous iterate. If \( A_k \) is chosen to be zero, the variation of \( \hat{x}_{k|k} \) will be constrained depending on the pdf of \( v_k \). If \( v_k \) is zero, one obtains the recursively least squares algorithm (RLS) where a linear model is fitted solely from the measurements. For \( v_k \) Gaussian distributed, it represents a prior \( L_2 \) regularization on \( \hat{x}_{k|k} \), and one gets a \( L_2 \) regularized RLS. For Laplacian distribution, a prior \( L_1 \) regularization will be imposed [27] and one gets a \( L_1 \) regularized RLS algorithm that enhances sparsity. If one chooses the Huber worse case distribution, the regularization function will become a Huber function. Other function such as smoothly clipped absolute deviation (SCAD) [28], [29] can also be used to avoid biased estimate. This establishes the relationship between robust statistics and regularization and the M-estimate regularization like SCAD can be viewed as a robust measure of complexity of \( \hat{x}_{k|k} \). On the other hand, if the pdf of \( v_k \) is chosen as Laplacian or Huber worst-case distribution, increased robustness of the estimates can be obtained in the presence of outliers, which is directly related to robust statistics where the M-estimate function is used as cost function for data fitting, etc. [30]. Further simplification can be obtained if the prediction residual or error \( z_k - C_k \hat{x}_{k|k-1} \) in (5) is replaced by \( \psi(z_k - C_k \hat{x}_{k|k-1}) \).
where $\varphi(e)$ is a robust score function that de-emphasizes abnormally large residual to reduce the sensitivity of the algorithm to outliers [31]. Without the state equation, one gets the recursive least M-estimate (RLM) algorithm [32]. We will illustrate more applications of these algorithms on forecasting electricity price in the next section.

In general, these problems cannot be solved directly using the conventional KF in (4) and (5). One needs to resort to (2) and (3) by computing the integral using Monte Carlo techniques by representing the pdf say as histograms. It gives rise to a class of KF algorithms called particle filters [33]. However, the complexity grows exponentially with the number of dimension. More recently, it was shown that by modeling the densities as a Gaussian mixture, then (2) and (3) of the BKF can be approximated by simplifying the densities directly [34]. As a result, the arithmetic complexity is significantly reduced and all the above problems can be approximately solved even at high dimension.

**NONSTATIONARITIES IN TIME-SERIES ANALYSIS**

Another problem commonly encountered is the nonstationarities of time series. Such estimation unavoidably involves the selection of a window size or bandwidth to seek an appropriate tradeoff between bias and variance of the estimators. In RLS and KF, this issue is usually addressed by using a forgetting factor [35] or by choosing the covariance matrix of the excitation. Another efficient nonparametric approach is based on local polynomial regression (LPR), which is a popular technique for data smoothing and density estimation [36]. It assumes that the function to be estimated is continuous at high dimension. More recently, it was shown that by modeling the densities as a Gaussian mixture, then (2) and (3) of the BKF can be approximated by simplifying the densities directly [34]. As a result, the arithmetic complexity is significantly reduced and all the above problems can be approximately solved even at high dimension.

Effective DR will depend critically on the ability of load/renewable energies forecasting at the utilities’ side and price forecasting at the market as well as customers’ side. Conventional load/demand forecasting is a reasonably mature field, but with the introduction of RTP, such forecasting has to be done in a much shorter interval of perhaps one hour, half an hour, or even five minutes, since DR introduces interactions between demand and price of electricity and high penetration of renewable energies with variable nature. This also calls for tools that can provide confident intervals instead of just a point estimator to account for the increased uncertainties.

According to a recent review [42], [43], common behavior of electricity prices can be broadly summarized in the following four aspects:

1. strongly seasonal nature of prices
2. mean reversion nature
3. price-dependent volatilities and spikes
4. correlation between electricity price and load.

Different algorithms have been put forward for predicting these characteristics of electricity prices as summarized in Table 3 [44], [45], [73], [74]. Due to the time-varying nature of electricity price/load, batch processing of these algorithms are required to adapt to possible change of trend. This requires high-arithmetic complexity. Here, we introduce new recursive subspace algorithms with low-arithmetic complexity. In this regard, forecasts can be more efficiently computed to cope with the time-critical requirement of RTP.

Previous studies [47] show that day-ahead (DA) hourly prices should not be treated as a single time series, because they are not generated consecutively in DA market clearing. Therefore, it is desirable to slice spot prices into segments of
curves of one-day long, and consider time series of curves. Consequently, the functional principal component analysis (FPCA) was proposed recently in [48] where the prices vector $z(n)$ in a day is approximated by a linear combination of principal components (PCs) and their corresponding scores, called PC scores:

$$
\hat{z}(n+h) = \mu(n) + \sum_{m=1}^{M} \hat{t}_m(n+h)p_m(n) + e(n),
$$

where $n$ indices the days, $\mu(n)$ is the mean, $\hat{t}_m(n+h)$ is the $h$ days ahead forecasted $m$th PC score, $p_m(n)$ is the PC, and $e(n)$ is the modeling error. A major limitation of the FPCA algorithm is that it requires batch eigen-decomposition (ED) of the covariance matrix, which requires high online arithmetic complexity.

Here, we propose to employ an RLM-based robust projection approximation subspace tracking (PAST) [49] and PC tracking algorithms in [50] for recursively tracking the PCs and scores in presence of outliers. The PC scores are further tracked and predicted recursively using the robust KF mentioned above with online adaptive threshold selection (ATS) [51]. Advantages of the proposed robust recursive FPCA (RFPCA) approach are its low online arithmetic complexity, robustness to outliers, and the availability of the confidence interval thanks to the KF framework.

While most of these techniques are based on statistical model, a recent work in [52] proposed a multifactor price model to capture the market fundamentals in the following three time horizons:

**FIG3** Time-frequency representation and separation of impulsive and transient power transients. (a) Simulated 50-Hz power waveforms with an impulsive transient at 40 ms and an oscillatory transient from 95 ms to 125 ms; (b) true 50-Hz voltage component (yellow line) and its estimate reconstructed from ME-RAWLP (black line); (c) true oscillatory transient (yellow line) and its estimate reconstructed from ME-RAWLP (black line); (d) true impulsive transient (yellow line) and its estimate (black line); (e) LS-AWLP; and (f) ME-RAWLP with SCAD regularization.
### Table 3: A Summary of Algorithms for Forecasting Electricity Price/Load, Wind, and Solar Energies

<table>
<thead>
<tr>
<th>Algorithms</th>
<th>Descriptions</th>
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</table>
| **ELECTRICITY PRICE/LOAD FORECASTING [44], [45], [73], [74]** | **SIGNAL PROCESSING-BASED SOLUTIONS**<br>**ARTIFICIAL NEURAL NETWORKS (ANNs)**<br>The predicted price/load is a combination of different approximation functions such as multilayer perception or radial basis functions. The weights of each approximation function are estimated from a set of training data. | **OTHER APPROACHES**
| **SUPPORT VECTOR MACHINES (SVMs)** | The SVM approximates price/load in terms of different kernel functions. The contribution of each kernel function is estimated from training data. | **PRODUCTION COST MODELS AND GAME THEORY MODELS**
| **ARMA, ARMA WITH EXOGENOUS VARIABLES (ARMAX), AND GENERALIZED AUTOREGRESSIVE CONDITIONAL HETEROSEDASTICITY (GARCH).** | In the ARMA, ARMAX, and GARCH, future price/load is expressed in terms of a combination of previous price/load. The ARMA and ARMAX are commonly used to approximate the mean reverting Ornstein-Uhlenbeck (OU) processes [46]. On the other hand, the GARCH model is commonly used to deal with nonstationary property of electricity prices. | **MONTE CARLO SIMULATIONS ARE PERFORMED TO PREDICT THE PRICE/LOAD BY SIMULATING THE STRATEGIC BEHAVIOR OF THE PRODUCER AND THE CONSUMER.**
| **FUNCTIONAL PRINCIPAL COMPONENT ANALYSIS (FPCA)** | The electricity price/load is approximated by a linear combination of PCs. PC scores are computed by projecting the data onto the PCs. Then, parametric time-series models such as ARMA can be applied on the PC scores to perform prediction. | **OTHER APPROACHES**
| **CONTINUOUS TIME MODELS** | Electricity price/load is modeled by a system of stochastic differential equations. | **NUMERICAL WEATHER PREDICTION SIMULATIONS ARE CARRIED OUT TO PREDICT THE WEATHER BASED ON PHYSICS-BASED MODELS THAT ARE RELATED TO CURRENT WEATHER CONDITIONS.**
| **PRODUCTION COST MODELS AND GAME THEORY MODELS** | Monte Carlo simulations are performed to predict the price/load by simulating the strategic behavior of the producer and the consumer. | **OTHER APPROACHES**
| **WIND FORECASTING [75]–[76]** | **SIGNAL PROCESSING-BASED SOLUTIONS**<br>**ANN, SVM**<br>See descriptions above. | **SOLAR FORECASTING [77]–[79]**<br>**ANN, SVM**<br>See descriptions above. | **OTHER APPROACHES**
| **RANDOM FORESTS**<br>A group of predictors are used to predict quantities such as wind speed or direction. The returned predicted value is the mode of the predicted values obtained from individual predictors. | **OTHER APPROACHES**
| **NUMERICAL WEATHER PREDICTION**<br>Simulations are carried out to predict the weather based on physics-based models that are related to current weather conditions. | **OTHER APPROACHES**
| **SOLAR FORECASTING [77]–[79]** | **SIGNAL PROCESSING-BASED SOLUTIONS**<br>**ANN, SVM**<br>See descriptions above. | **OTHER APPROACHES**
| **LINEAR REGRESSION**<br>A linear model is used to perform prediction. The model is built on physical quantities such as radiation, sunshine duration, and latitude of site. | **OTHER APPROACHES**
| **NUMERICAL WEATHER PREDICTION**<br>See descriptions above. | **OTHER APPROACHES**

- **In the short term of one week:** market driving forces are variations of electricity load and generation dispatches.<br>- **In the midterm of one year:** effecting forces are seasonal weather and annual generation planned outage.<br>- **In the long run of multiple years:** significant forces are economic development and generation investment and retirement.

A similar idea can also be applied to the robust RFPCA. For a two-factor model, the price vector can be split into two components as $z(n) = z^{\text{daily}}(n) + z^{\text{weekly}}([n/7])$ and solved separately on a different time horizon. For the daily component $z^{\text{daily}}(n)$, the AR component $y^m(n)$ of its PC score $z^{\text{daily}}_m(n) = y^m(n) + f^m(n)$ can be tracked by the robustKF. On the other hand, the seasonality component $f^m(n) = \sum_{t=0}^{p-1} \beta_t \cos(2\pi mt/S) + \beta_t \sin(2\pi mt/S)$ can be obtained by solving for the periodic components in the Fourier series as in [53]. The weekly component $z^{\text{weekly}}([n/7])$ can be computed similarly. Generally, this concept can be extended to a multifactor model by incorporating models of longer time horizons, such as monthly and yearly models. As an illustration, we now compare the proposed robust RFPCA, FPCA, the auto-regressive model with time varying mean (ARV) in [53], and their multifactor counterparts on predicting the electricity spot price using the electricity price collected from the New England DA energy market in the United States [54], which are hourly locational marginal pricing (LMP) data at the Internal Hub from 1 January 2005 to 31 October 2010. For the proposed and the FPCA algorithms, the same ARV(1) model as in [53] is used to update and predict the PC scores. The number of chosen PCs is $B = 4$, which is determined by the minimum description length (MDL) method. The forgetting factor $\beta$ in a robust PAST algorithm is chosen as 0.99. An initial data block of length ten is used to initialize the robust RFPCA. Whereas for the FPCA and the ARV algorithms, a sliding window of size of 1,000 days is chosen for batch processing. The performance of all algorithms is...
evaluated by the mean absolute percentage error (MAPE)
averaged from $K = 50$ forward validation iterations:
$\text{MAPE} = \frac{1}{K} \sum_{k=1}^{K} \left( \frac{x^{[k]}(n) - \hat{x}^{[k]}(n)}{x^{[k]}(n)} \right)$, where $x^{[k]}(n)$ and $\hat{x}^{[k]}(n)$ are the actual and estimated electricity prices, respectively, at the $k$th FV iteration. Figure 4 shows the MAPE of the DA prediction for the three algorithms. It can be seen that the proposed algorithm generally outperforms the other algorithms. Moreover, the confidence interval of the DA price can be reliably estimated as shown in Figure 5 with a 99% confidence interval. Table 4 shows another comparison between the multifactor extension of the three algorithms and their single-factor counterparts. The weekly ahead price prediction for the multifactor algorithms is generally better than those of their single-factor counterparts. This suggests that the multifactor price model can further improve the accuracy in long-term prediction because the price trends due to different time scales can be separately captured. In general, the above methods can also be applied to load/demand forecasting. Another important and related forecasting problem is wind and solar power forecasting. In particular, wind power forecasting has been identified as an important tool to address the increasing variability and uncertainty, and to more efficiently operate power systems with large wind power penetration. Some common wind and solar forecasting methods are also summarized in Table 3.

**DEMAND-RESPONSE MANAGEMENT AND OPTIMIZATION**

DRM requires the utilities or ISO and the customers to work cooperatively to reduce peak load, improve utilization at off-peak hours, and hence improve efficiency and lower costs. This usually involves complicated and RT optimization at various levels. On the utilities’ side, electricity market and power system operators have to deal with the variability and uncertainty of large-scale wind power generation in their scheduling and dispatch decisions. In an electricity grid, electricity consumption and production must balance at all times; any significant imbalance could cause grid instability or severe voltage fluctuations. Therefore, total generation capacity is sized to correspond to total peak demand with some margin of errors and allowance for contingencies. Operators will generally plan to use the least expensive generating capacity in terms of

<table>
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<th>[TABLE 4] MAPE FOR DIFFERENT ALGORITHMS.</th>
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<tr>
<td><strong>ROBUST RFPCA (PROPOSED)</strong></td>
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<tr>
<td><strong>MULTIFACTOR (PROPOSED)</strong></td>
</tr>
<tr>
<td>ONE DAY AHEAD</td>
</tr>
<tr>
<td>ONE WEEK AHEAD</td>
</tr>
<tr>
<td>TWO WEEKS AHEAD</td>
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<tr>
<td>THREE WEEKS AHEAD</td>
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</table>

(*) For illustrative purpose, the proposed multifactor model is also incorporated into the FPCA. However, it is remarked that the model is not considered in the FPCA reported in [48].
and make appropriate decisions possibly through optimization limitations and other physical constraints. We shall also illustrate the concept with some simple examples later in the section "Utilities—The Unit Commitment Problem States and". A REASONABLE TIME. THE CALCULATED LMP AND MARKET CLEARING PRICES FOR DIFFERENT RESERVES ARE THEN USED IN THE FINANCIAL SETTLEMENT OF THE RT MARKET. WITHIN THE OPERATING HOURS, THE SCED IS RUN TO DISPATCH THE SYSTEM AT A SHORT TIME INTERVAL (SAY, FIVE MINUTES IN MOST ISO/ RTO MARKETS), WHILE RT PRICES FOR ENERGY (LMP) AND OPERATING RESERVES ARE CALCULATED. marginal cost, and use additional capacity from more expensive plants as demand increases. In most cases, DR aims to reduce peak demand to reduce the risk of potential disturbances, avoiding additional capital investment for additional plants as well as avoiding the use of more expensive and/or less efficient operating plants. Another less common use of DR is to increase demand during periods of high supply and/or low demand to maintain grid stability. Energy storage such as pumped-storage hydroelectricity is another way to increase load during periods of low demand for use at later time. To get a better picture of the optimization involved, we briefly review the short-term operation of the power systems and markets in the United States and illustrate the concept with some simple examples later in the section “Utilities—The Unit Commitment Problem and Real-Time Pricing.”

In addition to the UC problem above, the operators have to collect and analyze RT network information and related events such as outages, voltage loss, and maintain a database of demand responsive resources. Depending on the sophistication of the control system, analysis of the demand responsive behavior and compliance with DR requests may have to be performed. Using this information, appropriate price and DR requests can be determined to meet the electricity load, while minimizing costs and observing stability, transmission capacity limitations and other physical constraints. We shall also illustrate with a simple example the kind of optimization involved.

At the customer side, one has to respond to dynamic pricing and make appropriate decisions possibly through optimization approaches. As mentioned in the section “Smart Grid,” examples of dynamic pricing include: RTP, PP, and TOU pricing. In [12], an open automated DR communications specifications (OpenADR) data model was developed to standardize DR communication from the utility or independent system operator (ISO) to commercial and industrial customers [55]. OpenADR is a Web services-based information model that supports all the pricing tariffs above to facilitate customers participating in automated DR programs with building control systems to use the price information as input to their building control systems and automate DR strategies. Alternatively, prices can be mapped into “building operation modes,” to be inputted to the building control systems. Mapping prices to operation modes may facilitate wider customer participation since it simplifies their processing of dynamic pricing signals and carrier communications, allows compatibility with existing DR customers and their DR strategies, and allows interoperability with less-sophisticated or legacy controls. Typical characteristics of the pricing tariffs and short-term power market operation in the United States are also summarized in Table 5.

It comes as no surprise that dynamic pricing comes in different forms, which also forms different business models for load control aggregation [11]. Due to the complicated pricing structure and the RT nature of the price, automated DR at the customer side using an EMS is highly desirable. The detailed optimization differs somewhat for smart home or commercial and industrial users. In the sections “Smart Home and DRM Optimization” and “Microgrid for Commercial and Industrial...
Users,” we will review recent approaches to these problems, propose several new concepts and approaches, and give several illustrations.

Utilities—the unit commitment problem and real-time pricing
To get some ideas about the UC problem, let us examine the typical short-term operation of power systems based on ISO/regional transmission organization (ISO/RTO) markets in the United States [56]. Then we will describe approaches for addressing the variable nature of wind and other renewable power in the UC problem. Moreover, we will illustrate how DR can be taken into account in the dispatch operations to achieve RTP.

Operation of power systems and markets in the United States
In general, the operation includes 1) determination of reserve requirements, 2) DA operations, and 3) RT operations, which are summarized in Table 5. Currently, most intermittent resources such as wind power are not included in the DA operations of most U.S. markets and are considered as price takers in the RT operations. It is expected that they will be integrated to the DA in the future. This poses a considerable problem as the variability and uncertainty of intermittent renewable resources may increase in a short time interval the amount of regulation reserves in the system. An excellent overview of the required reserves due to wind power is reported in [57]. Case studies also confirm that higher wind penetration will need higher degree of backup reserves, which varies from 1% to 2% to around 18%.

Unit commitment problem and pricing with demand response
To address the variability of wind power in UC problem, [58] focused on the risk brought by high wind penetration and developed a risk evaluation method for the short-term operation of power systems. References [59] and [60] employed stochastic optimization to deal with the uncertainty of wind power in the UC problem (see Table 5). Since the pdf of the wind is not easy to obtain, [61] proposed a robust UC model with bounds on wind power generation to capture the intermittent nature of wind energy generation and to derive both the price levels and generator schedule based on DR. The positive effect of DR in the form of RTP

<table>
<thead>
<tr>
<th>TABLE 6</th>
<th>SUMMARY OF GENERATORS’ CONSTRAINTS.</th>
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<tr>
<td>MINIMUM UP</td>
<td>$-y_{i,t-1} + y_{i,t} - y_{i,b} \leq 0$ (\forall t \geq 2, h \in [t, \min{t, t-1, T-1}])</td>
</tr>
<tr>
<td>MINIMUM DOWN</td>
<td>$y_{i,t-1} - y_{i,t} + y_{i,b} \leq 1$ (\forall t \geq 2, h \in [t, \min{t, t-1, T-1}])</td>
</tr>
<tr>
<td>START-UP OPERATION</td>
<td>$-y_{i,t-1} + y_{i,t} - z_{i,t} \leq 0$ (\forall t \geq 2,)</td>
</tr>
<tr>
<td>RAMPING UP</td>
<td>$x_{i,t+1} \leq x_{i,t} + y_{i,t} \Delta t_i + (1 - y_{i,t}) u_t \leq 0$ (\forall t = 1, T-1)</td>
</tr>
<tr>
<td>RAMPING DOWN</td>
<td>$x_{i,t} \leq x_{i,t-1} + y_{i,t-1} \Delta t_i + (1 - y_{i,t-1}) u_t \leq 0$ (\forall t = 1, \ldots, T-1)</td>
</tr>
<tr>
<td>GENERATION CAPACITY</td>
<td>$\sum_{i=1}^{N_C} y_{i,t} \leq u_{y_{i,t}}$ (\forall i, t)</td>
</tr>
</tbody>
</table>
SMART HOME AND DRM OPTIMIZATION

Next we consider the optimization in a smart home, where most electric appliances (smart appliances) are networked together and are controlled by a home EMS as shown in Figure 2. On one side, utilities gather the information such as the consumers’ usage of electricity from the smart meters, and set the price level using, say, the RTP DR algorithm mentioned previously to reduce the peak electricity load. In response to the price signals, the customers can shift their demands automatically or manually with the help of the home EMS to the off-peak hours so as to minimize their electricity payment. To achieve this goal, the home EMS automatically predicts the electricity price and coordinates the operating schedule of smart appliances with the consent of the customers. As rooftop solar electric systems and small wind turbines are widely deployed, the customers may further harvest these free DERs through the automatic coordination of the EMS. It is also envisioned that battery-assisted (BA) smart appliances or high-capacity battery storage devices (fuel cells) will get into the mainstream to allow better utilization of DERs. Moreover, smart appliances may have the ability to reduce its power consumption by slightly compromising their quality of services upon receiving the demand requests from the EMS.

We now briefly review approaches that have been put forward for solving the DR optimization problem and propose a new scheduling algorithm based on $L_1$ regularization technique. The main objective of DR optimization is to minimize the electricity bill or maximize their users’ satisfaction/comfortability by continually monitoring the electricity price information, allocating available resources and actively managing the load of appliances. A number of algorithms such as particle swarm optimization (PSO) [63], linear programming [64], and convex programming [65] have been proposed for DR optimization. Unlike the PSO and other heuristic algorithms that may result in premature convergence, the latter two convex programming approaches are more attractive because the problem can be solved efficiently using interior point methods and the optimality of the solution is guaranteed.

To carry out DR optimization, appropriate models for the appliances are usually required so that proper control (load, charging discharging storage) can be performed using the forecasted electricity price and model-based predicted energy consumption. Examples of these appliances include heating, ventilation, and air-conditioning systems [21], [22]. Another common cost model involved in DR optimization is called the utility function, which measures the users’ satisfaction on the appliances [65], [66]. This function is usually inversely proportional to the amount of energy consumed by the appliances so that the electricity cost can be reduced without significantly discomfort the users. In the convex optimization approach, these models are usually chosen as convex or concave functions to obtain an overall convex problem. In [65], the models of four common types of electric appliances in a household were discussed. The first type is concerned with the temperature-related appliances such as heaters and ACs, the second is the schedule-based (SB) appliances such as plug-in hybrid electric vehicles and washers, the third is related to the essential appliances such as lighting, and the final one is the entertainment appliances such as TVs, video games, and computers.

Each type of the appliances is characterized by its own utility function $U(q_t)$ that measures the user’s satisfaction on the power consumption $q_t$ at time $t$ as well as the constraints of $q_t$. For example, the concave utility function of Type 1 appliances is related to the inside temperature $W^{in}(t)$ and the most comfortable temperature $W^{comp}(t)$ as $U_w(W^{in}(t), W^{comp}(t)) = c_1 - c_2 (W^{in}(t) - W^{comp}(t))^2$ for some positive constants $c_1$ and $c_2$. This in turn can be expressed in terms of $q_t$ using the linear dynamical model $W^{in}(t) = W^{in}(t-1) + \alpha (W^{out}(t) - W^{in}(t-1)) + \beta q_t$, where $\alpha$ and $\beta$ denote the thermal condition surrounding the appliance and $W^{out}(t)$ is the outside temperature. Moreover, additional constraints can be imposed on $q_t$ to specify respectively its operating and temperature ranges as $Q \leq q_t \leq \overline{Q}$ and $W^{comp} \leq W^{out}(t) \leq W^{comp}(t)$.

However, the models of the aforementioned Types 2 and 4 appliances allow them to be switched off during operation
which may not be reasonable in practice. In this tutorial, we assume that they should have run until completion once started. More specifically, suppose that there are $N_S$ such SB appliances, and each of them has to complete its task within a user’s preferred time period $t \in [T_{S,j}, T_{S,i}]$ and has a known load profile $E_{S,j}(t)$ for $t \in [0, k_{S,j} - 1]$, where $k_{S,j}$ is the total number of time slots for the task being completed. Therefore, there are $M_i = k_{S,j} - T_{S,j} - k_{S,i} + 2$ possible schedules and the scheduling problem is to select the best schedule in $E_{S,j}(t - T_{S,j} - m)$, $m = 0, \ldots, M_i - 1$, which depends on the price level within the user’s preferred time period. Alternatively, the load schedule can be written as $E_{S,j}(t) = \sum_{m=0}^{M_i-1} \alpha_{i,m} E_{S,j}(t - T_{S,j} - m)$, where $\alpha_{i,m} = 1$ is the binary decision variable indicating that the schedule is selected when it is equal to one. To ensure that only one schedule is selected at a time, we further impose $\sum_{m=1}^{M_i} \alpha_{i,m} = 1$ (E2).

We can see that the resulting scheduling problem is a combinatorial problem. To solve this difficult problem, we first relax the binary decision variable $\alpha_{i,m}$ to a real-valued variable as $0 \leq \alpha_{i,m} \leq 1$, $\forall i, m$ (E3). Then, we minimize a $L_1$ regularization term in the form of $\sum_{m=1}^{M_i} |\alpha_{i,m}|$ so as to enforce the value of $\alpha_{i,m}$ associated with the best schedule to be as large as possible, while keeping others as close to zero as possible. A major advantage is that the resulting problem is convex.

In addition to the above household appliances, we also consider an appliance equipped with internal batteries, called BA appliances. Suppose that there are $N_B$ such appliances, each of them containing an internal battery that has a charging/discharging power of $b_{i,t}$ at time $t$. Its ability of charging ($b_{i,t} > 0$) or discharging ($b_{i,t} < 0$) offers additional to handle the intermittent renewable energy sources and improves the response to RTP. Following the battery model in [65], the constraints $R_{B,i} \leq b_{i,t} \leq R_{B,i}$ and $0 \leq \sum_{t=1}^{T} b_{i,t} \leq B_i$ (E4) are imposed to restrict the maximum charging rate $(R_{B,i} > 0)$, maximum discharging rate $(R_{B,i} < 0)$, and maximum capacity ($B_i$). Also, to model the possible damage against the battery’s lifetime, the term $F_i(b_{i,t}) = \eta_{i,b} b_{i,t}^2 - \eta_{i,b} b_{i,t+1} + \eta_{i,b} \min(b_{i,t} - \eta_{i,b} B_i, 0)^2$, for some positive constants $\eta_{i,b}$, $k = 1, 2, 3, 4$, is added to the cost function. On the other hand, we assume that each appliance of this type consumes a power of $E_{B,i}(t)$ and allows direct control DR up to $D_{DC,i} E_{B,i}(t)$ at time $t$, where $D_{DC,i}$ is the maximum possible percentage reduction in load. Therefore, the actual DR of the $i$th appliance at time $t$, $d_{i,t}$, is bounded by $0 \leq d_{i,t} \leq D_{DC,i}$ (E5). Similar to previous discussion, we also include a convex function, $G_i(d_{i,t}) = \lambda_i (D_{DC,i} - d_{i,t} + \lambda_i)^{-\lambda}$, in the objective to measure user’s dissatisfaction for some positive constants $\lambda_i$, $k = 1, 2, 3$.

As an illustration, suppose that the smart home shown in Figure 2 consists of

- an AC with identical settings as described in [65]
- $N_S = 2$ SB appliances with $E_{S,j}(t) = \{0.9$ KWh, 0.9 KWh, 0.2 KWh$\}$
- $T_{S,1} = 1$, $T_{S,2} = 18$
- $E_{S,j}(t) = \{1.5$ KWh, 1.5 KWh, 1.5 KWh, 1 KWh$\}$
- $T_{S,2} = 12$ and $T_{S,3} = 22$
- $N_B = 1$ BA appliance with $(R_{B,1}, R_{B,1}, B_1, D_{DC,1})$
- $E_{B,i}(t) = (-250$ Wh, 250 Wh, 800 Wh, 0.3, 2300 Wh$)$
- a renewable energy source, which can deliver a power of $v_t$ up to a predicted maximum time-varying power of $V(t)$ at time $t$
- a connection to the utility which delivers a power of $u_t$ and provides associated RTP information $P_t(u_t)$ at time $t$. The corresponding DR optimization problem can be written as

$$\min \sum_{i=1}^{N_S} P_t(u_i) - \sum_{t=1}^{T} \{U(q_t) + \sum_{i=1}^{N_S} \sum_{m=1}^{M_i} |\alpha_{i,m}|$$

$$+ \sum_{i=1}^{N_B} \sum_{t=1}^{T} \{G_i(d_{i,t}) + F_i(b_{i,t})\}$$

s.t. $u_t + v_t \geq q_t + \sum_{i=1}^{N_S} \sum_{m=1}^{M_i} |\alpha_{i,m}| E_{S,j}(t - T_{S,j} - m)$

$$+ \sum_{i=1}^{N_B} \{(1 - d_{i,t}) E_{B,i}(t) + b_{i,t}\}, \forall i, t$$

$$u_t \leq 0, \forall t; \quad 0 \leq v_t \leq V(t), \forall i, t;$$

(E1)–(E5).

Figure 7 shows electricity allocation of the smart home in response to RTP price by solving the above convex problem. We can see that the BA smart appliance tends to consume more
power and its internal battery is charged up in the case of lower price. Moreover, for the SB appliances, the best schedule with the lowest price within the user’s preferred period can be selected. Here, we note that the Karush-Kuhn-Tucker conditions of the above DR optimization problem suggest that its solution is usually sparse. Also, the largest nonzero coefficient, which may not be exactly equal to one depending on the form of the price and utility functions, tends to indicate the most cost-effective schedule corresponding to the largest cost reduction. This is indicated in the lowest part of Figure 7, where the relaxed decision variables corresponding to the best schedules can be easily singled out. Such schedule will be considered as the solution of target scheduling problem before the relaxation in (E3).

**MICROGRID FOR COMMERCIAL AND INDUSTRIAL USERS**

As mentioned earlier in the section “Smart Grid,” microgrids improve reliability and PQ, allow higher penetration of renewable sources and dynamic islanding, and simplify the control of the grid. If heat generation is required, the use of waste heat through cogeneration or combined cooling heat and power (CCHP) can deliver both electricity and useful heat from an energy source such as natural gas. In [67], the problem of optimal control of DERs with DR under electricity and fuel price uncertainty is studied. Given uncertain electricity and fuel prices modeled by the commonly used mean-reverting (OU) processes [46], a weighted average of the expected annual energy costs and CO2 emissions of the microgrid for various capacity sizes is minimized. The problem is solved via Monte Carlo simulation and dynamic programming (DP) since the discount cost is used for meeting energy loads over a number of test years. Using this stochastic DP (SDP) method, different policies such as doing nothing, DERs with DR and DERs without DR can be compared with different emphasis on costs and CO2 emission. It was found that DERs dominates the case of doing nothing in terms of lower expected energy bills, reduced
CO₂ emissions, and lower condition value-at-risk (cVAR). Moreover, DR makes DERs more attractive, especially when the electricity price becomes more uncertain. It was also found that large distributed generator (DG) unit performs the best in terms of the environment aspect in minimizing CO₂ emissions and medium DG units give the lowest expected cost. This shows the usefulness of microgrids with DER and DR in cost reduction and reducing CO₂ emissions. An important problem, however, is how to control in RT the microgrids under RTP so as to minimize electricity costs and possibly CO₂ emission and how to exercise DR. This is an optimal control problem that can be solved using approximate dynamic programming (ADP) [68]. An alternative approach using a formulation similar to the home EMS described in “Smart Home and DRM Optimization” can also be developed [69]. This approach can also be extended to the power management of an electric vehicle charging station [69]. Next we present some results on the improved frequency regulation of microgrids.

FREQUENCY REGULATION OF MICROGRIDS

In traditional power systems, frequency deviation, which is an indicator of instantaneous imbalance of supply and demand of electricity, is regulated with a hierarchical control framework. The large variation of high wind power penetration poses significant challenges to the traditional load-following frequency regulation methodology, especially for microgrids operating in isolated mode. As the smart grid is equipped with state-of-the-art communication and control technologies, the load response provides a novel approach to balance power systems. By a comprehensive framework with demand and generation as described above, the traditional frequency regulation methodology will be shifted to a novel generation/load-following methodology. The appropriateness of this match has been recognized by the Electric Reliability Council of Texas (ERCOT), which allows load curtailment to supply half of ERCOT’s 2,300 MW spinning reserve requirement. The PJM Interconnection also recently changed its reliability rules to allow loads to supply spinning reserve [70]. Potential resources for load response include ACs, refrigerators, freezers, pumps, electric hot water heaters, washing machines and dryers, storage systems, plug-in electric vehicles, and lighting. For a microgrid, an alternative scheme for frequency regulation may be employed as illustrated in Figure 8 [70], where a wind generator works together with the loads with load response. For example, with wind power output and total load in Figure 9, the frequencies of the microgrid with/without load response are illustrated in Figure 10. It can be seen that the load response also improves significantly the controllability of the microgrid.

ACKNOWLEDGMENTS

This work was supported in part by the National Basic Research Program (2012CB215102) and General Research Fund of Hong Kong Research Grant Council under projects 7124/10E and 7124/11E.

AUTHORS

S.C. Chan (scchan@eee.hku.hk) received the B.Sc. (Eng) and Ph.D. degrees from The University of Hong Kong, Pokfulam, in 1986 and 1992, respectively. Since 1994, he has been with the Department of Electrical and Electronic Engineering, the University of Hong Kong, where he is currently a professor. His research interests include fast transform algorithms, filter design and realization, multirate and biomedical signal processing, communications and array signal processing, high-speed A/D converter architecture, bioinformatics, image-based rendering, and the smart grid. He is currently a member of the Digital Signal Processing Technical Committee of the IEEE Circuits and Systems Society, and he is an associate editor of Journal of Signal Processing Systems and IEEE Transactions on Circuits.
and Systems II. He was the chair of the IEEE Hong Kong Chapter of Signal Processing in 2000–2002, an organizing committee member of the 2003 IEEE International Conference on Acoustics, Speech, and Signal Processing, the 2010 International Conference on Image Processing. He was an associate editor of IEEE Transactions on Circuits and Systems I from 2008 to 2009. He is a Member of the IEEE.

K.M. Tsui (kmtsiu@eee.hku.hk) received the B.Eng., M. Phil., and Ph.D. degrees in electrical and electronic engineering from the University of Hong Kong, in 2001, 2004, and 2008, respectively. He is currently working as postdoctoral fellow in the Department of Electrical and Electronic Engineering at the same university. His main research interests are in array signal processing; high-speed AD converter architecture; biomedical signal processing; digital signal processing; multirate filter bank and wavelet design; and digital filter design, realization, and application.

H.C. Wu (andrewcwkw@eee.hku.hk) received the B.Eng. degree in electrical engineering from the University of New South Wales, Australia, in 2008 and the M.Sc degree in electrical and electronic engineering from the University of Hong Kong in 2009. He is currently a Ph.D. student in the Department of Electrical and Electronic Engineering at the University of Hong Kong. His main research interests are in pattern recognition, bioinformatics, digital signal processing, and time-series analysis.

Yunhe Hou (yhhou@eee.hku.hk) received his B.E. (1999) and Ph.D. (2005) degrees from Huazhong University of Science and Technology, China. He worked as a postdoctoral research fellow at Tsinghua University from 2005 to 2007. He was a visiting scholar at Iowa State University and a research scientist at University College Dublin, Ireland, from 2008 to 2009. He was also a visiting scientist with the Laboratory for Information and Decision Systems, Massachusetts Institute of Technology, Cambridge in 2010. He is currently an assistant professor at the University of Hong Kong. He is a Member of the IEE.

Yik-Chung Wu (ycwu@eee.hku.hk) received the B.Eng. degree in electrical and electronic engineering in 1998 and the M.Phil. degree in 2001 from the University of Hong Kong. He received the Ph.D. degree from Texas A&M University, College Station, in 2005. From 2005 to 2006, he was with the Thomson Corporate Research, Princeton, New Jersey, as a member of technical staff. He has been an assistant professor at the University of Hong Kong since 2006. He was a visiting scholar at Princeton University in 2011. His research interests are in general area of signal processing and communication systems. He is currently an associate editor of IEEE Communications Letters.

Felix F. Wu (ffwu@eee.hku.hk) is the Philip Wong Wilson Wong Professor in electrical engineering at the University of Hong Kong, where he served as pro vice chancellor (vice president) from 1997 to 2001. He is also a Professor Emeritus at the University of California, Berkeley, where he has been on the faculty since 1974. He is a Fellow of the IEEE.