<table>
<thead>
<tr>
<th><strong>Title</strong></th>
<th>Simulation of a linear permanent magnet vernier machine for direct-drive wave power generation</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Author(s)</strong></td>
<td>Li, W; Chau, KT</td>
</tr>
<tr>
<td><strong>Issued Date</strong></td>
<td>2011</td>
</tr>
<tr>
<td><strong>URL</strong></td>
<td><a href="http://hdl.handle.net/10722/158753">http://hdl.handle.net/10722/158753</a></td>
</tr>
<tr>
<td><strong>Rights</strong></td>
<td>International Conference on Electrical Machines and Systems Proceedings. Copyright © IEEE.; ©2011 IEEE. Personal use of this material is permitted. However, permission to reprint/republish this material for advertising or promotional purposes or for creating new collective works for resale or redistribution to servers or lists, or to reuse any copyrighted component of this work in other works must be obtained from the IEEE.; This work is licensed under a Creative Commons Attribution-NonCommercial-NoDerivatives 4.0 International License.</td>
</tr>
</tbody>
</table>
Simulation of a Linear Permanent Magnet Vernier Machine for Direct-drive Wave Power Generation

Wenlong Li and K.T. Chau
Department of Electrical and Electronic Engineering,
The University of Hong Kong, Hong Kong
E-mail: wlii@eee.hku.hk

Abstract — This paper proposes a linear permanent magnet (PM) vernier machine for direct-drive wave power generation. Firstly, the machine structure is proposed and its parameters are indentified by finite element analysis (FEA). Secondly, the mathematical modeling of wave power absorption system was established. The control strategy for maximizing absorbed wave power is discussed. Then, by using Matlab/Simulink, the wave power generator system is modeled and simulated. A vector control scheme is implemented which controls power flow between the generator and the load via a bi-directional AC/DC converter. The simulation results verify the feasibility of the proposed machine used for direct-drive wave power generation.

I. INTRODUCTION

With increasing concerns on crude oil exhaustion and environment deterioration, clean and renewable energy exploitation and its related industrials develop in an accelerated pace [1]-[9]. Renewable energy such as wind energy and wave energy features as a variable speed and intermittent power source. In order to harvest this kind of energy, various permanent magnet machines with special structure and distinct merits were developed, such as doubly salient permanent magnet (DSPM) machine [10]-[17], permanent magnet hybrid brushless (PMHB) machine [18]-[25], double-stator cup-rotor permanent magnet machine [26]-[29], doubly salient memory machine [30]-[33], transverse-flux permanent magnet (TFPM) machine [34], [35], magnetic-gearized permanent magnet brushless machine [36]-[47], etc. The last two types are aim to apply in a low-speed and hightorque density direct-drive applications which is more popular in recent years.

However, the complicated structure and the low power factor are two major drawbacks of the TFPM machine which result in a high initial cost and a low power efficiency. By integrated with a magnetic gear, the conventional high speed and high efficiency machine can satisfy the direct-drive application [38], [42], [46] and retain its merits at the same time. Nevertheless, the magnetic-gearized machine has two moving bodies and three air-gaps which is also not easy to fabricate. Based on the concept of field modulation in magnetic gears, a PM vernier machine has been proposed to solve this problem [48]. By using a toothed-pole structure, which is equivalent to the field modulation ring of the magnetic gear combined with the stator, this machine can adopt only one moving body and one air-gap to achieve the same performance as the magnetic geared machine, thus it will be very competitive for direct-drive application.

The purpose of this paper is to extend the concept of PM vernier machines to its linear morphology and examine its performance in direct-drive wave power generation. By using FEM, the parameters of the linear vernier machine are indentified. Then based on Matlab/Simulink, the wave power generation system operation is simulated. The output power of the system is maximized with an appropriate control strategy.

II. LINEAR VERNIER MACHINE

As shown in Fig. 1, the vernier structure usually involves a toothed-pole structure which can interact with a different pole-pair number magnetomotive force (MMF) on the rotor. When the armature winding is assumed to have a pole-pair number of \( P \), the fundamental MMF waveform of the armature excitation is given by:

\[
F_a = F_a \cos(P(\theta - \omega t + \theta_{a0})
\]

where \( F_a \) is the amplitude of the fundamental MMF waveform, \( \omega \) is the angular frequency of the current in the armature winding, and \( \theta_{a0} \) is the initial phase angle.

By omitting its DC offset component, the fundamental permeance of stator toothed-pole structure is:

\[
\lambda_i = \Lambda_i \cos(Z_{st} \theta + \theta_{a0})
\]

where \( \Lambda_i \) is the amplitude of the stator teeth permeance waveform, \( Z_{st} \) is the number of the stator teeth, and \( \theta_{a0} \) is the initial phase angle.

Thus, flux density in the air-gap due to interaction between armature excitation and the toothed-pole stator can be simply decided by the following equation:

\[
B_{ag} = F_a \times \lambda_i
\]

\[
= \Lambda_i F_a \left[ \cos((Z_{st} + P)\theta + \theta_{a0}) - P \omega t + \theta_{a0} \right] \times \\
\left[ \cos(Z_{st} - P)\theta + \theta_{a0} + P \omega t - \theta_{a0} \right]
\]

According to (3), it can be observed that the pole-pair number of field in air-gap has been changed by vernier structure. Thus, a steady force can be developed, if the PM pole-number \( Z_2 \) on the rotor satisfies the following relationship:

\[
Z_2 = \left| Z_{st} \pm P \right|
\]

When ac current with an angular frequency \( \omega \) runs in the armature windings, the resultant magnetic field of armature excitation rotates at a speed of \( \omega/P \), and the rotor speed is \( \omega/Z_2 \). By borrowing concept of gear ratio in magnetic gear, the
Two kinds of stator structure configuration is shown in Fig. 1, namely open-slot type and pole-split type [49]. The proposed machine adopts the latter one for a compact design as depicted in Fig. 2. It has a flat single-sided structure, which consists of 9 stator teeth splitting into 27 small teeth at the end, 24 active PM pole-pairs on the mover and 9 slots for housing 3-phase windings. The longitudinal-magnetized PMs are surface mounted on the mover back iron. The windings adopt a concentrated winding which can minimize end windings and ease the fabrication. The stator is artfully design that each inner stator tooth splits 3 small teeth which has the same function as flux modulation poles in magnetic gears.

In order to access the proposed machine performance, the finite element method (FEM) is applied for magnetic field calculation. Fig. 3 shows the no-load electromotive force (EMF) when the translator moves at a constant speed of 0.5 m/s. Fig.4 shows the cogging force of the proposed machine. It can be found that the cogging force is within 8% of the rated developed force which is very promising in direct-drive applications. The proposed machine parameters are listed in Table I.

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>LINEAR PERMANENT MAGNET VERNIER MACHINE PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Items</td>
<td>Value</td>
</tr>
<tr>
<td>Rated voltage (RMS)</td>
<td>60 V</td>
</tr>
<tr>
<td>Rated current (RMS)</td>
<td>5.6 A</td>
</tr>
<tr>
<td>Rated power</td>
<td>1 kVA</td>
</tr>
<tr>
<td>Phase number</td>
<td>3</td>
</tr>
<tr>
<td>PM remanence</td>
<td>1.2 T</td>
</tr>
<tr>
<td>PM coercivity</td>
<td>940 kA/m</td>
</tr>
<tr>
<td>Air-gap length</td>
<td>1 mm</td>
</tr>
<tr>
<td>Pole pitch</td>
<td>6.5 mm</td>
</tr>
<tr>
<td>Phase resistance</td>
<td>2.8 Ω</td>
</tr>
<tr>
<td>Direct-axis inductance</td>
<td>54.2 mH</td>
</tr>
<tr>
<td>Quadrature inductance</td>
<td>54.2 mH</td>
</tr>
<tr>
<td>Translator mass</td>
<td>3.2 kg</td>
</tr>
</tbody>
</table>

The Ocean is a great treasure trove on earth. The wave energy resource in the ocean is considered as a tremendous alternative energy source for people in the coming years. In those wave energy conversion techniques, the direct-drive wave energy converter which engages a linear electrical generator for electric power production attracts more and more attention. Since this technique can directly couple linear electrical generator to the marine device such as buoy, float, or
air-chamber for absorbing wave power along with the wave rise and fall, the energy efficiency is relatively higher than those indirect-drive approaches. Fig.3 shows two famous direct-drive wave energy converters which use the linear electrical generator for electricity generation. The first one is the Archimedes wave swing (AWS) which operates totally under the water [50]. The latter one is buoy-based wave energy converter. In this paper, the system adopts the buoy based one which is also called point absorber. Fig.4 shows the whole buoy-based direct-drive wave power generator system.

The generator translator motion equation is given by [51]:

$$F_e + F_r + F_f + F_{em} = m \frac{d^2x}{dt^2}$$

where $F_e$ is the incident wave force on the buoy, $F_r$ is the radiated force of buoy acting on the water, $F_f$ is the force due to friction between mechanical parts and the water, $F_{em}$ is the electromagnetic force of the linear generator, $m$ is the mass of the total moving part, and $x$ is the displacement of the moving part.

By multiplying the velocity to (5), the power equation of the system can be described as below:

$$P_e - P_r - P_f - P_{em} = m \frac{dx}{dt} \frac{d^2x}{dt^2}$$

The power $P_e$, $P_r$, $P_f$, and $P_{em}$ are developed by force $F_e$, $F_r$, $F_f$ and $F_{em}$, respectively. The power $P_r$ is the radiated power that returns to the sea from the buoy which is similar as the reactive power in electrical circuits. The power $F_f$ is consumed by friction and $P_{em}$ is the power absorbed by the generator and its load which is the key part of wave energy conversion.

In order to obtain the maximal absorbed power $P_{em}$, the radiated power $P_r$ and the power $P_f$ due to friction should be minimized when the incident wave power $P_e$ keeps as a constant. The absorbed wave power by the proposed linear machine can be expressed as:

$$P_{em} = \hat{F}_{em} \cdot \vec{v}_i$$

where $v_i$ is the velocity of the linear generator translator, and “...” denotes the variable is a complex variable.

According to (7), the generator force $F_{em}$ should be controlled in phase with the speed of the translator $v_i$, thus the absorbed power $P_{em}$ can be maximized [52]. It means that the current should be injected from the load part to satisfy the above condition.

IV. SIMULATION FOR WAVE POWER GENERATION WITH MATLAB/SIMULINK

As discussed in section III, the generator force $F_{em}$ should be controlled with the translator speed $v_i$ for maximizing the wave power absorption. In order to regulate the generator force of the generator, a bi-directional AC/DC converter is deployed between the generator and the load.

The voltage, flux linkage and force equations of the linear generator in $d$-$q$ reference frame are given as below:

$$u_d + R_a \cdot i_d + \frac{d\lambda_d}{dt} - \omega \cdot \lambda_q = 0$$

(8)

$$u_q + R_a \cdot i_q + \frac{d\lambda_q}{dt} + \omega \cdot \lambda_d = 0$$

(9)

$$\lambda_d = L_d \cdot i_d - \lambda_{pm}$$

(10)

$$\lambda_q = L_q \cdot i_q$$

(11)

$$F_{em} = \frac{3\pi}{2\tau_{pm}} [i_q \cdot (L_q - L_d) - \lambda_{pm} \cdot i_d]$$

(12)

where $u_d$, $u_q$, $i_d$, $i_q$, $\lambda_d$ and $\lambda_q$ are the terminal voltage, current, flux linkage of the direct-axis and quadrature-axis, respectively, $R_a$ is the armature winding resistance, $\omega$ is the translator velocity in radian per second, $\lambda_{pm}$ is the flux linkage due to permanent magnet, $\tau_{pm}$ is the pole-pitch of permanent magnets on the translator.

The mathematical model of the linear generator is built by Matlab/Simulink according to (8)-(12) with the parameters listed in Table I. In order to control the generator force, the space vector control strategy is adopted which need to maintain the direct-axis current as zero. Thus, according to (12), the generator force is only a function of the quadrature-axis current [53]. The quadrature-axis current reference signal can be decided based on (7) and (12) as following:

$$i^*_q = \frac{c v_i}{\lambda_{pm} 3\pi}$$

(13)

where $c$ is a constant depend on the system.

Fig. 6 illustrates the whole system control block diagram. The proposed linear vernier machine is connected to a rechargeable battery system via a bi-directional AC/DC converter. The control system uses only current loop control to achieve the maximal power absorption. From encoder signal, the translator velocity $v_i$ and its position can be estimated. With the translator velocity information, the reference signal of quadrature-axis current $i^*_q$ can be calculated. With the position information, an abc/dq0 transformation for the direct-axis and quadrature-axis current reference signal can be achieved. By comparing the actual current signal with the current reference signal, the error signals are put to a hysteresis current regulator for generating a set of control pulse signal. With these firing signals, the power switches are turned on and off at the right time for tracing the reference signal.

Fig. 7 shows the translator velocity waveform when a sinusoidal external force acts on the system. Fig. 8 depicts the 3-phase no-load voltage waveforms. When the proposed linear generator is connected to the rechargeable battery system via the bi-directional AC/DC converter, the power extraction of the proposed generator can be maximized by aforementioned
Fig. 6. System control diagram.

Fig. 7. The translator speed waveform.

Fig. 8. 3-phase no-load voltage waveforms.

Fig. 9. The generator force waveform.

Fig. 10. The direct-axis current waveform.
vector control strategy. The generator force $F_{em}$ waveform is shown in Fig. 9. It can be observed that the generator force $F_{em}$ is almost controlled in phase with the translator speed, thus the maximal wave power absorption can be resulted. Fig. 10 and Fig. 11 show the controlled direct-axis and quadrature-axis current waveforms which both trace the reference signals very well. Fig. 12 and Fig. 13 depict the active power and reactive power generated by the propose generator. It can be found that the generated power can achieve a peak value of 1 kW with the maximal power absorption control strategy.

V. CONCLUSION

This paper proposes a low-speed and high force density linear permanent magnet vernier machine for the direct-drive wave power generation. By using FEM, the machine performance and its parameters are calculated. For maximizing the absorbed wave power, conditions for the generator operation are discussed. At last, the proposed machine and the control strategy are simulated by Matlab/Simulink. The simulation results verify the feasibility of the proposed machine and its control strategy for maximal wave power absorption.

ACKNOWLEDGMENT

This work was supported by a grant (Project No. HKU710710E) from the Hong Kong Research Grants Council, Hong Kong Special Administrative Region, China.

REFERENCES
